# Similarity learning

metric embedding of complex data

Siniša Šegvić UniZg-FER

# Plan

- motivation for similarity learing
- siamese models
- triplet loss
- implementation details and evaluation
- □ applications: stereoscopic vision, self-supervision

#### INTRODUCTION: LIMITS OF STANDARD CLASSIFICATION

Classification models may become impractical when:

- □ there are no defined classes, or the classes are unknown
- the number of classes is too large

Application examples:

- stereoscopic correspondence
- self-supervised learing
- □ tracking, associative search biometric verification





[bicanic19fusion]

Deep Learning  $1 \rightarrow$  Introduction 3/45

### INTRODUCTION : LIMITS OF STANDARD CLASSIFICATION

The presented applications can be conveniently addressed by leveraging similarity between examples

Left pair: different. Right pair: similar



[chopra05cvpr]

The idea: embed the data into the appropriate vector space

- □ standard metrics (L2, ...) model the similarity between the data
- short name: metric embeddings

### INTRODUCTION: METRIC EMBEDDINGS

Before going forward, we must ask ourselves:

□ why wouldn't we just measure the the similarity in the input space?

Answers:

- because distances in high dimensional vector spaces do not make sense (the curse of dimensionality)
- because vector representations of complex data is usually not appropriate for comparing different samples

### INTRODUCTION : METRIC EMBEDDINGS - AN EXAMPLE

We look at distances between digits in the MNIST dataset

- □ L2 distance between the first and second digit: 121.4
- □ L2 distance between the first and third digit: 133.2
- □ L2 distance between the second and third digit: 114.9



[lecun98pieee]

Conclusion: there is no strong connection between the distance in the original space and data similarity

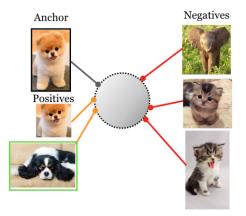
#### INTRODUCTION : METRIC EMBEDDINGS - AN EXAMPLE

```
import torch
import torchvision
mnist = torchvision.datasets.MNIST('data', download=True)
print(mnist.targets[:10])
# tensor([5, 0, 4, 1, 9, 2, 1, 3, 1, 4])
print(torch.sqrt(torch.sum((mnist.data[2]-mnist.data[3])**2,
      dtype=torch.float)))
# tensor(121.4)
print(torch.sqrt(torch.sum((mnist.data[2]-mnist.data[9])**2,
      dtype=torch.float)))
# tensor(133.2)
print(torch.sqrt(torch.sum((mnist.data[3]-mnist.data[9])**2,
      dtype=torch.float)))
# tensor(114.9)
import cv2
cv2.imwrite('m2.png', mnist.data[2].numpy())
cv2.imwrite('m3.png', mnist.data[3].numpy())
cv2.imwrite('m9.png', mnist.data[9].numpy())
                                                Deep Learning 1 \rightarrow Introduction (4) 7/45
```

### INTRODUCTION : METRIC EMBEDDINGS - THE GOAL

Embed the data into a (relatively) low-dimensional space where standard metrics may model the similarity between the data

If we normalize the representations (e.g. by placing them inside the hypersphere), we may use scalar product to measure the similarity



### INTRODUCTION : METRIC EMBEDDINGS - ADVANTAGES

We may associate data even when some of the classes are unknown during training

It is more difficult for the model to overfit:

- □ classification: O(N) learning samples
- □ similarity:  $O(N^2)$ ,  $O(N^3)$  or  $O(N^B)$  learning samples.

Useful representations may also be trained in the self-supervised context where we expect the sample to be similar to its own perturbation, and different from other examples; e.g. SimCLR [chen20icml].

Metric embeddings may sometimes help with standard supervised tasks [khosla20neurips].

#### METRICS: TERMS

We consider the set *X* and the mapping  $d: X \times X \rightarrow R$ .

We refer to d as a metric, while (X, d) represent the metric space iff :

1. 
$$d(a, b) \ge 0$$
  $\forall a, b \in X$  (positivity),

2. 
$$d(a, b) = 0 \iff a = b \quad \forall a, b \in X$$
 (zero-rule),

3. 
$$d(a, b) = d(b, a) \quad \forall a, b \in X \text{ (symmetry)},$$

4. 
$$d(a, b) \le d(a, c) + d(c, b) \quad \forall a, b, c \in X$$
 (triangle inequality).

This definition fits well with the concept of data similarity.

Some of these axioms are redundant, e.g. positivity and symmetry are a direct results of triangle inequality and the zero-rule.

In practice we usually learn a pseudo-metric that relaxes the zero-rule  $\Box d(a, b) \neq 0$  is hard to ensure  $\forall a \neq b$ , so we only require d(a, a) = 0Deep Learning 1  $\rightarrow$  metrics 10/45

#### METRICS: STANDARD CHOICES

Euclidian metrics:

$$d_E(a,b) = \sqrt{(a-b)^\top (a-b)} \sim (a-b)^\top (a-b)$$

If the data is normalized, the scalar product is equal to the cosine similarity and results in the same ranking as a Euclidian metric:

$$d_{E}(a, b) \sim (a - b)^{\top}(a - b)$$
$$\sim a^{\top}a - 2 \cdot a^{\top}b + b^{\top}b = 2 - 2 \cdot a^{\top}b$$
$$\sim -a^{\top}b$$

Mahalanobis metric (M is equal to the inverse of data covariance):

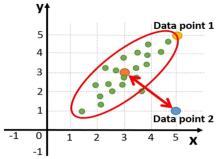
$$d_M(a,b) \sim (a-b)^\top \cdot M \cdot (a-b)$$

Deep Learning  $1 \rightarrow \text{metrics } 11/45$ 

# METRICS: MAHALANOBIS

The Mahalanobis isohypse is marked in red:

- according to Mahalanobis, the yellow sample is much closer to the orange sample than the blue sample
- we can hypothesize that the blue sample does not belong to the green class
- □ the Euclidian metric does not support such reasoning.



Deep Learning  $1 \rightarrow$  metrics (2) 12/45

### METRICS: MAHALANOBIS

Matrix M is real and symmetric  $\Rightarrow$  it may be diagonalized:  $M = W^{\top}W$ 

Mahalanobis metric may be interpreted as a shallow embedding into a Euclidian metric space W:

$$d_{M}(a, b) \sim (a - b)^{\top} \cdot M \cdot (a - b)$$
  
 
$$\sim (W \cdot (a - b))^{\top} \cdot (W \cdot (a - b))$$
  
 
$$\sim (W \cdot a - W \cdot b)^{\top} \cdot (W \cdot a - W \cdot b))$$
  
 
$$\sim d_{E}(Wa, Wb)$$

There are analogous shallow approaches that consider association of the data with symbolic classes (Fisher LDA).

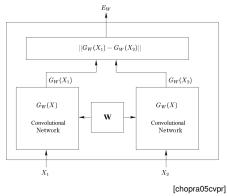
The next logical step: replace *W* with a **deep model**  $f_{\theta}$ :

□ what makes sense today, did not make sense in 2005...

# SIAMESE TRAINING : THE IDEA

Train a model  $G_W$  that embeds data X into a space where the Euclidian metric  $E_W$  reflects the (dis)similarity between samples

Siamese learning involves two instances of a parametric module G.



The two instances share parameters W, while their gradients are accumulated through the two instances.  $Deep Learning 1 \rightarrow Siamese training 14/45$ 

### SIAMESE TRAINING : LOSS

Siamese learning involves some variant of the contrastive loss.

Contrastive loss depends on whether the inputs belong to the same "class":

$$L(\theta) = \sum_{y_q = y_p} L_{\text{pos}}(\theta | x_q, x_p) + \sum_{y_q \neq y_n} L_{\text{neg}}(\theta | x_q, x_n)$$

The loss  $L_{pos}$  forces the examples from the same class to come closer:

$$L_{\text{pos}}(\theta | x_q, x_p) = \| f_{\theta}(x_q) - f_{\theta}(x_p) \|^2$$

The loss  $L_{neg}$  forces foreign examples to move from each other:

$$L_{\mathsf{neg}}(\theta|x_q, x_n) = [\max(0, m - \|f_{\theta}(x_q) - f_{\theta}(x_n)\|)]^2$$

Deep Learning  $1 \rightarrow$  Siamese training 15/45

### SIAMESE TRAINING : GRADIENTS

Consider the gradients of losses  $L_{pos}$  and  $L_{neg}$  with respect to metric embeddings  $z_q = f_{\theta}(x_q)$ :

$$\frac{\partial L_{\text{pos}}}{\partial z_p} = 2 \cdot (z_p - z_q)$$
$$\frac{\partial L_{\text{neg}}}{\partial z_n} = -2 \cdot \max(0, m - ||z_q - z_n||) \cdot \frac{z_n - z_q}{||z_n - z_q||}$$

These gradients encourage the positive pairs to move closer, and the negative pairs to move away from each other.

The repellence stops when the distance becomes greater than the margin m.

# SIAMESE TRAINING: GRADIENTS (2)

Homework:

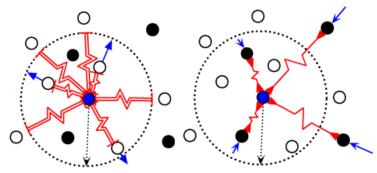
- □ derive the gradients of the contrastive loss  $\frac{\partial L_{\text{pos}}}{\partial f_{n}}$  i  $\frac{\partial L_{\text{neg}}}{\partial f_{n}}$ ;
- □ compare the gradient  $\frac{\partial L_{\text{neg}}}{\partial f_n}$  with the gradient of an alternative formulation:

$$L_{\mathsf{neg2}}(\theta|x_q, x_p) = \max(0, m^2 - \|f_\theta(x_q) - f_\theta(x_p)\|^2)$$

# SIAMESE TRAINING: GRADIENTS (3)

We may illustrate the decribed dynamics using a system of mechanical springs (where the force of the spring is proportional to the distance)

- black and white circles represent positive and negative examples with respect to the blue sample
- the negatives outside of radius m do not feel the repellent push from the blue sample



Deep [hgagging6\_vp] Siamese training (4) 18/45

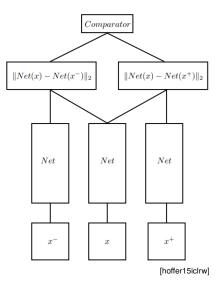
### TRIPLET LEARNING: THE IDEA

In Siamese training, we compare the same sample x with both negative and positive examples.

Embeddings for such samples need to be calculated twice.

The problem is addressed with triplet learning:

 the anchor is compared to the positive example x<sup>+</sup> and the negative example x<sup>-</sup>.



The three model instances share parameters and contribute to loss gradients in equal measure.

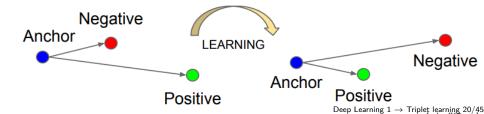
### TRIPLET LEARNING: LOSS

Triplet learning typically uses the triplet loss.

The triplet loss merges the two components of contrastive loss into a single expression:

$$L(\theta) = \sum_{i} \max(0, \|f_{\theta}(x_{ia}) - f_{\theta}(x_{ip})\| - \|f_{\theta}(x_{ia}) - f_{\theta}(x_{in})\| + \alpha)$$

The triplet loss brings the anchor and the positive example closer while increasing the distance between the anchor and the negative:

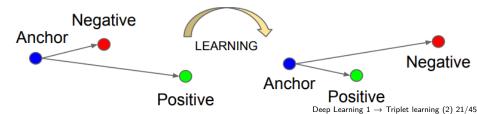


### **TRIPLET LEARNING : GRADIENTS**

Consider the gradients of the triplet loss with respect to embeddings  $f_a = f_{\theta}(x_{ia}), f_p = f_{\theta}(x_{ip})$  and  $f_n = f_{\theta}(x_{in})$ :

$$\begin{aligned} \frac{\partial L}{\partial f_p} &= \left[ \left\| f_a - f_p \right\| + \alpha > \left\| f_a - f_n \right\| \right] \cdot \frac{f_p - f_a}{\left\| f_p - f_a \right\|} \\ \frac{\partial L}{\partial f_n} &= \left[ \left\| f_a - f_p \right\| + \alpha > \left\| f_a - f_n \right\| \right] \cdot \frac{f_a - f_n}{\left\| f_a - f_n \right\|} \end{aligned}$$

These gradients test whether  $||f_p - f_a||$  is less than  $||f_n - f_a|| - \alpha$ .  $\Box$  if not, the gradients attract  $f_p$  and repel  $f_n$ :



# DETAILS: SOFT RELU

Classic triplet loss ingnores triplets where the triplet condition is met.

The advantage of this approach is that it prevents overfitting: when the data is sufficiently well positioned --- the training stops

On the other hand, such approach may be too cautious and hurt generalization

It is sometimes possible to avoid this pitfall by replacing the hard hinge loss  $ReLU(x) = [x]_+$  with its relaxed version:

 $softplus(x) = ln(1 + e^x)$ 

### DETAILS: SCALAR PRODUCT VERSION

As before, we denote embeddings with respect to  $x_p$ ,  $x_p$ ,  $x_n$  as:

$$f_{a} = f_{\theta}(x_{ia})$$
$$f_{p} = f_{\theta}(x_{ip})$$
$$f_{n} = f_{\theta}(x_{in})$$

If we normalize the latent representations  $||f_a|| = ||f_p|| = ||f_n|| = 1$ , we may express the loss with cosine similarity:

$$L(\theta) = \sum_{i} \max(0, f_{\theta}(x_{ia})^{\top} f_{\theta}(x_{in}) - f_{\theta}(x_{ia})^{\top} f_{\theta}(x_{ip}) + \alpha)$$

Deep Learning  $1 \rightarrow$  Details 23/45

### DETAILS: TRIPLET FORMATION

A simplified expression for the basic triplet loss [hermans17arxiv]:

$$L_3(\theta) = \sum_{y_a = y_p \neq y_n} [\alpha + D_{ap} - D_{an}]_+$$

Training triplet formation is an important implementation detail

- □ the main problem is training efficiency
- □ the number of triplets increases with  $O(N \cdot \overline{N_p} \cdot \overline{N_n})$

It may be worthwile to try the hard triplet loss (eng. batch-hard [hermans17arxiv]) that finds the most difficult negative and positive for a given anchor:

$$L_{BH}(\theta) = \sum_{a} [\alpha + \max_{y_a = y_p} D_{ap} - \min_{y_a \neq y_p} D_{an}]_+$$

Deep Learning  $1 \rightarrow$  Details (2) 24/45

### DETAILS: N PAIRS

Assume that we have a batch with N pairs of data [sohn16neurips]:

- $\square$  all pairs share an anchor:  $x_a$
- $\Box$  only one pair is positive:  $(x_a, x_p)$
- $\square$  all remaining pairs are negative (*N* 1 of them): (**x**<sub>a</sub>, **x**<sub>ni</sub>)

We define the loss so that it increases when the anchor is similar to negatives and decreases when it is similar to positives:

$$\mathcal{L}_{\mathsf{N}\text{-pairs}}(\mathbf{x}_{a}, \mathbf{x}_{p}, \{\mathbf{x}_{ni}\}) = \log\left(1 + \sum_{i=1}^{N-1} e^{f_{\theta}(\mathbf{x}_{a})^{\top} f_{\theta}(\mathbf{x}_{ni}) - f_{\theta}(\mathbf{x}_{a})^{\top} f_{\theta}(\mathbf{x}_{p})}\right)$$

If n=2,  $\mathcal{L}_{N\text{-pairs}}$  is very similar to the triplet loss with a scalar product.

# DETAILS: N PAIRS (2)

After a few simple steps  $\mathcal{L}_{\text{N-pairs}}$  may be reduced to the following form:

$$\begin{aligned} \mathcal{L}_{\text{N-pairs}}(\mathbf{x}_{a}, \mathbf{x}_{p}, \{\mathbf{x}_{ni}\}) &= \\ &= -\log \frac{\exp(f_{\theta}(\mathbf{x}_{a})^{\top} f_{\theta}(\mathbf{x}_{p}))}{\exp(f_{\theta}(\mathbf{x}_{a})^{\top} f_{\theta}(\mathbf{x}_{p})) + \sum_{i=1}^{N-1} \exp(f_{\theta}(\mathbf{x}_{a})^{\top} f_{\theta}(\mathbf{x}_{ni}))} \\ &= -\log \frac{\exp(f_{\theta}(\mathbf{x}_{a})^{\top} f_{\theta}(\mathbf{x}_{p}))}{\sum_{i=1}^{N} \exp(f_{\theta}(\mathbf{x}_{a})^{\top} f_{\theta}(\mathbf{x}_{a}))} \end{aligned}$$

We can see that  $\mathcal{L}_{N\text{-pairs}}$  is equivalent to standard cross entropy with a softmax over a vector of similarities between data pairs.

N-pairs loss is equivalent to the infoNCE loss [vandenoord18arxiv]:

infoNCE obtains the same equation by optimizing mutual information.

# DETAILS: N PAIRS (3)

The N-pairs loss may be generalized to a case where we have several positive and negative examples in a group  $\{\mathbf{x}_i, y_i\}_{i=1}^{B}$  (eng. soft nearest neighbours) [frosst19icml]:

$$\mathcal{L}_{\mathsf{snn}} = -\frac{1}{B} \sum_{i=1}^{B} \log \frac{1}{|\{y_j = y_i, j \neq i\}|} \frac{\sum_{j \neq i, y_j = y_i} e^{f_{\theta}(\mathbf{x}_i)^\top f_{\theta}(\mathbf{x}_j)/\tau}}{\sum_{y_i \neq y_k} e^{f_{\theta}(\mathbf{x}_i)^\top f_{\theta}(\mathbf{x}_k)/\tau}}$$

 $\hfill\square$  the hyper-parameter  $\tau$  (temperature) modulates output entropy.

A stricter variant of this loss requires that **every** positive within the group is more similar than the negatives [khosla20neurips]:

$$\mathcal{L}_{\mathsf{sum-out}} = -\frac{1}{B} \sum_{i=1}^{B} \frac{1}{|\{y_j = y_i, j \neq i\}|} \sum_{j \neq i, y_j = y_i} \log \frac{e^{f_{\theta}(\mathbf{x}_i)^{\top} f_{\theta}(\mathbf{x}_j)/\tau}}{\sum_{y_i \neq y_k} e^{f_{\theta}(\mathbf{x}_i)^{\top} f_{\theta}(\mathbf{x}_k)/\tau}}$$

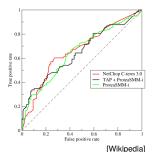
□ this generalizes better even though  $\mathcal{L}_{snn} > \mathcal{L}_{sum-out}$  (Jensen) Deep Learning 1 → Details (5) 27/45

### DETAILS: EVALUATION

The trained similarity measures induce the ranking:

- □ we fix the sample  $x_a$ , sort all other examples according to decreasing similarity:  $s_{ai} = -d(f_{\theta}(x_a), f_{\theta}(x_i))$
- if the ranking generalizes perfectly (this is usually not the case) then all the positives are ranked before negatives

Rank quality is measured by the area under the PR and ROC curves  $\Box$  the larger the area  $\Rightarrow$  the better the model



AUROC corresponds to probability that a random positive ranks above a random negative.

Unsuitable for non-balanced problems:

□ for such problems we prefer AUPR. Deep Learning  $1 \rightarrow \text{Details (6) } 28/45$ 

### **DETAILS: EVALUATION (2)**

Here is how we calculate per-threshold metrics:

 $\square$  we set the threshold at each index i and thus obtain P<sub>i</sub> positive

 $(s_{ax} <= s_{ai})$  and N<sub>i</sub> negative  $(s_{ax} > s_{ai})$  predictions

we use the labels to get the counts of:

- $\Box$  true positives TP<sub>i</sub>
- □ false positives FP<sub>i</sub>
- □ false negatives FN<sub>i</sub>
- □ and true negatives TN<sub>i</sub>

now we determine the relevant metrics wrt the threshold i:

 $\Box \text{ recall } \mathbf{R}_i = \mathsf{TPR}_i = \mathsf{TP}_i / (\mathsf{TP}_i + \mathsf{FN}_i)$ 

 $\square \text{ precision } P_i = TP_i / (TP_i + FP_i)$ 

□ false positive rate =  $FPR_i = FP_i/(TN_i+FP_i)$ 

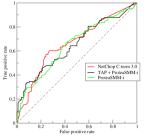
# DETAILS: EVALUATION (3)

We form the curves as follows:

- □ the precision-recall curve (PR) is made up of points  $(R_i, P_i)$
- receiver operating characteristic curve (ROC) is made up of points (FPR<sub>i</sub>,TPR<sub>i</sub>)

Rank quality is measured by the area under the PR and ROC curves

- $\hfill\square$  the larger the area  $\Rightarrow$  the better the model
- □ this is a threshold-independent metric of binary classification



F1 4 /\*1 \* 1\* 1

Deep Learning  $1 \rightarrow \text{Details}$  (8) 30/45

### DETAILS: EXERCISE

We are given samples  $x_1$  until  $x_5$ .

```
Their labels are Y=[1, 0, 0, 1, 1]
```

Distances from the sample  $x_1$  to the other samples are:

 $d(x_1, X) = [0.0, 5.0, 2.0, 3.0, 1.0]$ 

Determine the area under the precision-recall curve (AUPR for short) for the predictions in the sample  $x_1$ 

Note: AUPR is often referred to as average precision (AP)

### DETAILS: EXERCISE - SOLUTION

We rank the data as:  $[x_5^{(1)}, x_3^{(0)}, x_4^{(1)}, x_2^{(0)}]$ 

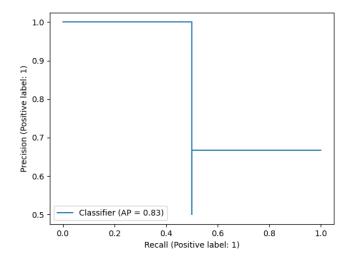
We set the threshold on each datapoint and measure precision P=TP/(TP+FP) and recall R=TP/(TP+FN):

| positive predictions | TP | FP | FN | Р   | R   |
|----------------------|----|----|----|-----|-----|
| $x_5, x_3, x_4, x_2$ | 2  | 2  | 0  | 0.5 | 1.0 |
| $x_5, x_3, x_4$      | 2  | 1  | 0  | 0.7 | 1.0 |
| $x_5, x_3$           | 1  | 1  | 1  | 0.5 | 0.5 |
| $x_5$                | 1  | 0  | 1  | 1.0 | 0.5 |

No threshold gives us R=0. We therefore add a point (R=0, P=precision for the lowest R).

If there are more P-s for the same R — we choose the best one.

### DETAILS : EXERCISE - GRAPH



Solution: AUPR = (0.5-0)×1 + (1-0.5)×0.66 = 0.83

Deep Learning  $1 \rightarrow$  Details (11) 33/45

### DETAILS : EXERCISE - CODE

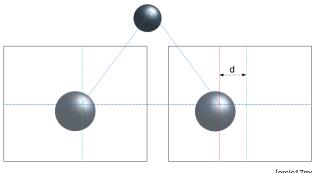
```
import numpy as np
from sklearn.metrics import average_precision_score
from sklearn.metrics import PrecisionRecallDisplay
import matplotlib.pyplot as plt
```

```
y_true = np.array([0, 0, 1, 1])
y_scores = np.array([-5, -2, -3, -1])
print(average_precision_score(y_true, y_scores))
```

PrecisionRecallDisplay.from\_predictions(y\_true, y\_scores)
plt.show()

#### STEREO: EXERCISE

For each pixel in  $I_{\text{left}}$  we search for a correspondence in  $I_{\text{right}}$ :



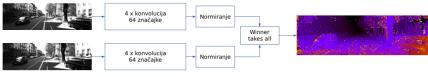
[orsic17ms]

Assume the calibrated case: correspondences in the same row

- we estimate a dense field of horizontal offsets ("disparities")
- if we know the disparity, the field of view, and the baseline distance, then we can reconstruct the scene depth in meters

#### STEREO: IDEA

Embed pixels from both images into the metric space with a convolutional model  $f_{\theta} : \mathbb{R}^{3 \times H \times W} \to \mathbb{R}^{F \times H \times W}$ , F=64 [zbontar15cvpr].



[orsic17ms]

Form a dense cost volume of shape  $D \times H \times W$ :

$$\Box V_{ijd} = \cot(f_{\theta}(I_L)_{i,j}, f_{\theta}(I_R)_{i,j+d})$$

Determine the best disparity for each pixel (winner takes all):

$$\Box D_{ij} = \arg\min_d V_{ijd}$$

#### STEREO: DETAILS

The triplet loss is expressed as a scalar product over normalized metric embedidngs of crops of  $9 \times 9$ :

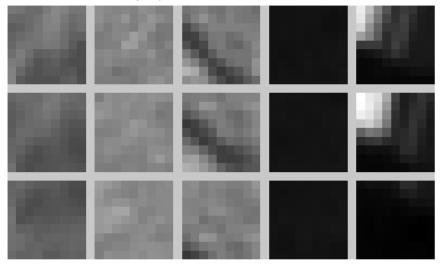
- $\Box$  three instances of model  $f_{\theta}$  share parameters
- each instance holds activations and calculates the gradients
- we get a total gradient for each parameter by aggregating the contributions of all model instances

Model  $f_{\theta}$  is equivariant:  $4 \times \text{conv3x3 w/o pooling}$ :

- □ input training samples have dimensions 128×3×9×9
- no padding during training (but use it during inference)
- $\Box$  embeddings have a dimensionality of 64,  $f_{\theta}: \mathbb{R}^{3 \times 9 \times 9} \rightarrow \mathbb{R}^{64}$
- $\hfill\square$  image pixels are normalized to  $\mathit{N}(0,\mathbf{I})$  during training and inference
- □ inference is done on whole images  $2 \times 3 \times H \times W$

#### STEREO: TRIPLETS

Columns show training triplets:





Deep Learning  $1 \rightarrow$  stereo (3) 38/45

#### STEREO: EXPERIMENTS

KITTI Datasets [geiger13ijrr]:

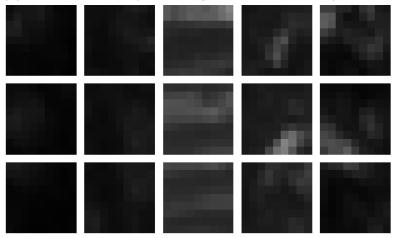
- □ 200 rectified images 1382 x 512
- □ training dataset: 80% slika (ostatak skup za validaciju)
- □ true disparities are measured with LIDAR in 30% of pixels
- □ dense disparities on cars were acquired by fitting CAD models



[orsic17ms]

#### STEREO: ERRORS

Many pixels visible in only one image due to "stereoscopic shadow":





The rows show i) anchor, ii) correspondence, iii) most similar negative.

Deep Learning  $1 \rightarrow$  stereo (5) 40/45

#### STEREO: ACCURACY

Stereoscopic methods on KITTI are evaluated according to percentage of true disparities with tolerance of  $\pm$ 1-3 pixels.

Experimental accuray is solid, though it is worse than SOTA:

| Model                    | Točnost - treniranje | Točnost - testiranje |
|--------------------------|----------------------|----------------------|
| Sive ulazne slike        | 84.99%               | 82.32%               |
| Sive ulazne slike - BN   | 74.51%               | 71.61%               |
| Ulazne slike u boji      | <b>85.50</b> %       | <b>82.84</b> %       |
| Ulazne slike u boji - BN | 74.40%               | 71.33%               |
|                          |                      | [orsic17ms]          |

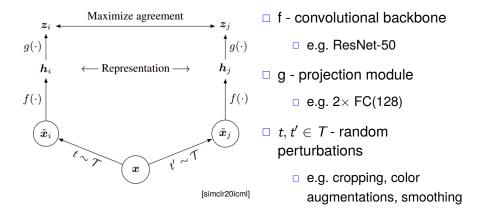
Advantage of metric approaches: resilience to overfitting.

Recent work uses other strategies to solve remaining challenges:

- training on unlabeled video [liu20cvpr]
- □ filling the areas without correspondences by analyzing the context

#### SELF-SUPERVISION: TASK

We wish to train useful representation without semantic labels.



Advantages: we may learn without labels, better knowledge transfer!

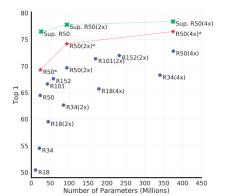
Drawbacks: long training, big batches, trivial solutions?

Deep Learning  $1 \rightarrow$  self-supervision 42/45

### SELF-SUPERVISION : SIMCLR

SimCLR: Simple Contrastive Learning of visual Representations

- □ N-pairs loss: for each positive pair we have 2(B-1) negatives
- □ inference: discard g, use f for knowledge transfer
- linear probe: fine-tune f for multi-class logistic regression
- applications: pre-training + fine-tuning, semi-supervised learning



- larger models and large groups (4096) learn better
- SimCLRv2 + linear almost as good as supervised learning
- □ To achive the best results wee need more training epochs (10px) and large

# SELF-SUPERVISION: SIMCLR (2)

Algorithm 1 SimCLR's main learning algorithm.

**input:** batch size N, constant  $\tau$ , structure of  $f, g, \mathcal{T}$ . for sampled minibatch  $\{x_k\}_{k=1}^N$  do for all  $k \in \{1, ..., N\}$  do draw two augmentation functions  $t \sim T$ ,  $t' \sim T$ # the first augmentation  $\tilde{\boldsymbol{x}}_{2k-1} = t(\boldsymbol{x}_k)$ # representation  $h_{2k-1} = f(\tilde{x}_{2k-1})$  $z_{2k-1} = q(h_{2k-1})$ # projection # the second augmentation  $\tilde{\boldsymbol{x}}_{2k} = t'(\boldsymbol{x}_k)$  $\boldsymbol{h}_{2k} = f(\tilde{\boldsymbol{x}}_{2k})$ # representation  $\boldsymbol{z}_{2k} = q(\boldsymbol{h}_{2k})$ # projection end for for all  $i \in \{1, \dots, 2N\}$  and  $j \in \{1, \dots, 2N\}$  do  $s_{i,j} = \mathbf{z}_i^\top \mathbf{z}_j / (\|\mathbf{z}_i\| \|\mathbf{z}_j\|)$  # pairwise similarity end for define  $\ell(i, j)$  as  $\ell(i, j) = -\log \frac{\exp(s_{i, j}/\tau)}{\sum_{k=1}^{2N} \mathbb{1}_{[k \neq i]} \exp(s_{i, k}/\tau)}$  $\mathcal{L} = \frac{1}{2N} \sum_{k=1}^{N} \left[ \ell(2k-1,2k) + \ell(2k,2k-1) \right]$ update networks f and q to minimize  $\mathcal{L}$ end for **return** encoder network  $f(\cdot)$ , and throw away  $g(\cdot)$ 

[simclr20icml]

The loss has 2N terms:

- N: mini-batch size
- □ each term is  $\ell_{NP}(i, j)$ 
  - $\Box$  i = 2r 1: anchor
  - $\Box$  *j* = 2*r* : positive
  - $\Box$   $k \neq i, j$ : negatives
- $\Box$   $\ell_{NP}(i, j)$ : n-pairs loss
  - expressed in terms
     of similarities s<sub>ij</sub>, s<sub>ik</sub>
- the negative data {k}
   correspond to the
   remaining samples in
   the mini-group

# CONCLUSION

Quantifying similarity is one of the basic tasks of machine learning.

We use metric embeddings when it is not practical to use classification:

- the number of classes is too large or unknown in advance
- there is only a limited quantity of labeled data

We realize metric embeddings as deep models trained with a suitable contrastive loss.

Applications:

- □ person tracking, face verification, stereo
- □ training with a small number of labeled examples (few-shot)
- self-supervised learning
- out-of-distibution detection.