

Optimiranje memorijskog rasporeda “offline” binarnog stabla

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Optimiranje rasporeda obilaženja matrice

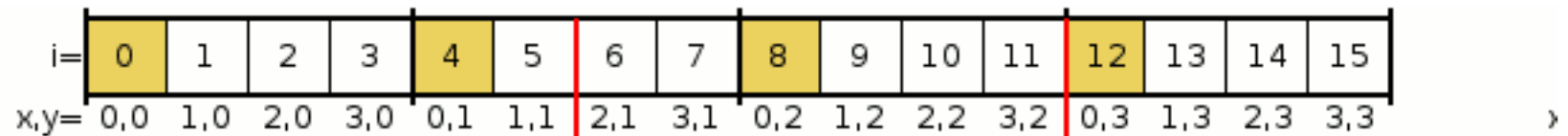


Image data laid out in one-dimensional memory

Cache Miss:
Load new data
from slow source

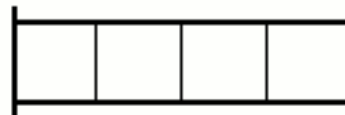
	x=0	1	2	3
y=0	0	1	2	3
1	4	5	6	7
2	8	9	10	11
3	12	13	14	15

Image data laid out
in two dimensions



x,y

One byte of pixel data



One row of pixels

Stablo I memorija

Dinamički alocirano stablo (new ili malloc)

Statički alocirano stablo (statički blok memorije)

Locality

Temporal locality

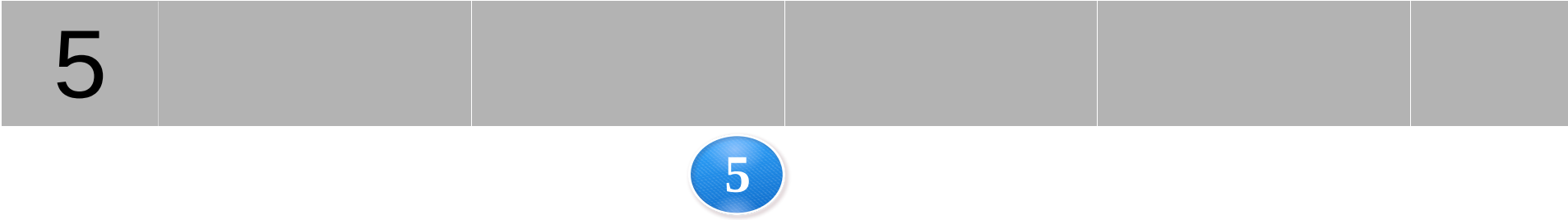
Spatial locality

Dinamički alocirano stablo

- 1) Raspored memorije ovisi o ubacivanjima
- 2) Stablo nije u kompaktnom bloku memorije
- 3) new (malloc) overhead

Dinamički alocirano stablo

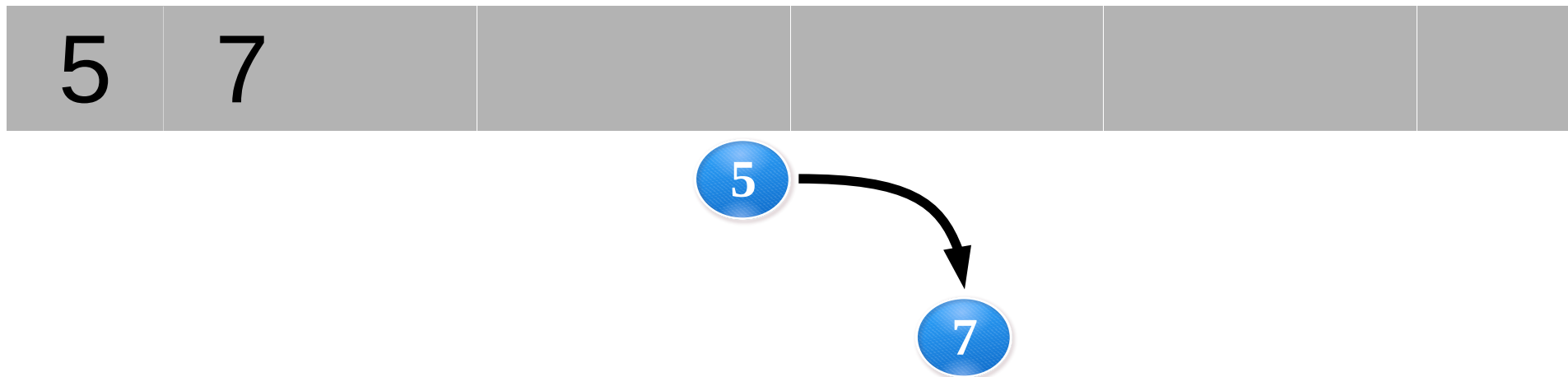
5



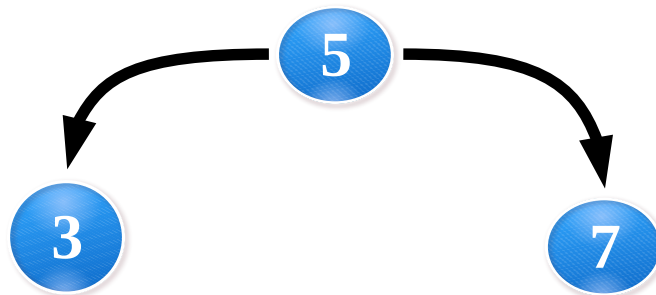
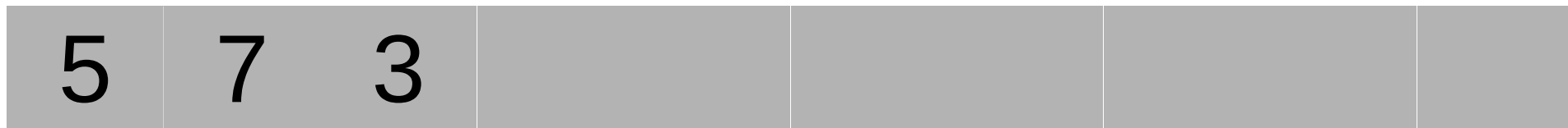
5					
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5

Dinamički alocirano stablo

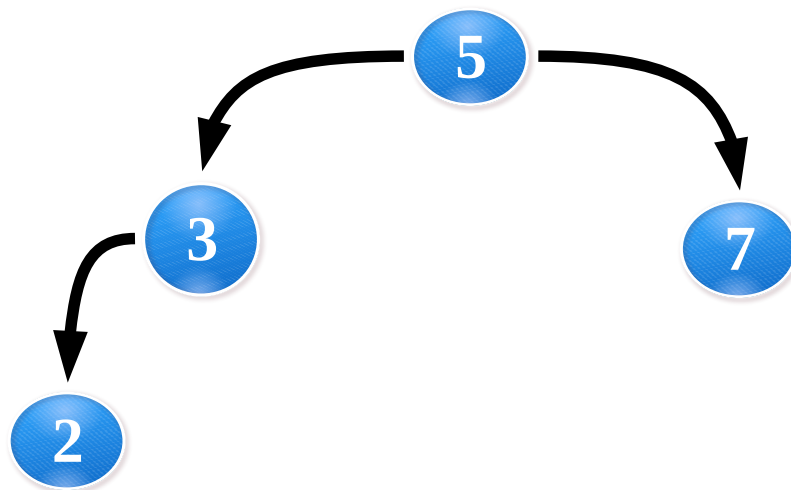


Dinamički alocirano stablo



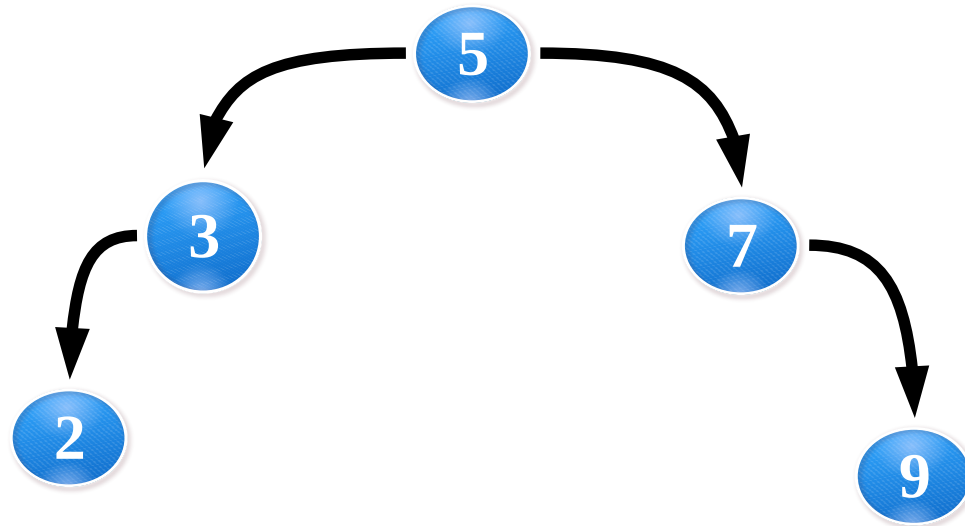
Dinamički alocirano stablo

5	7	3	2				
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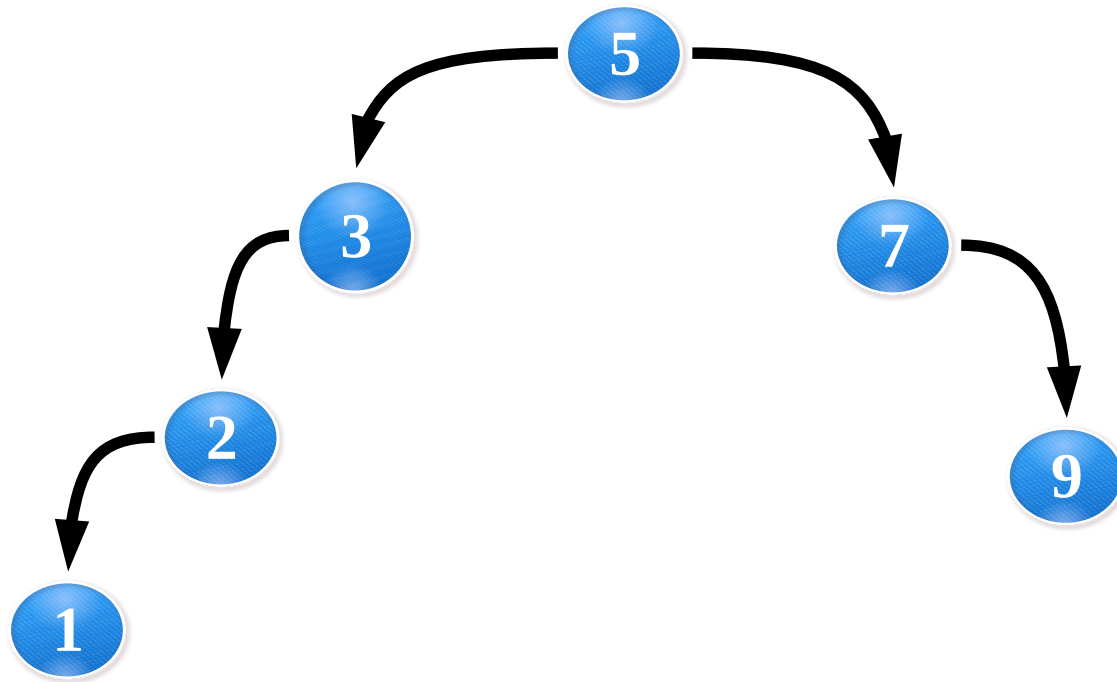
Dinamički alocirano stablo

5	7	3	2	9			
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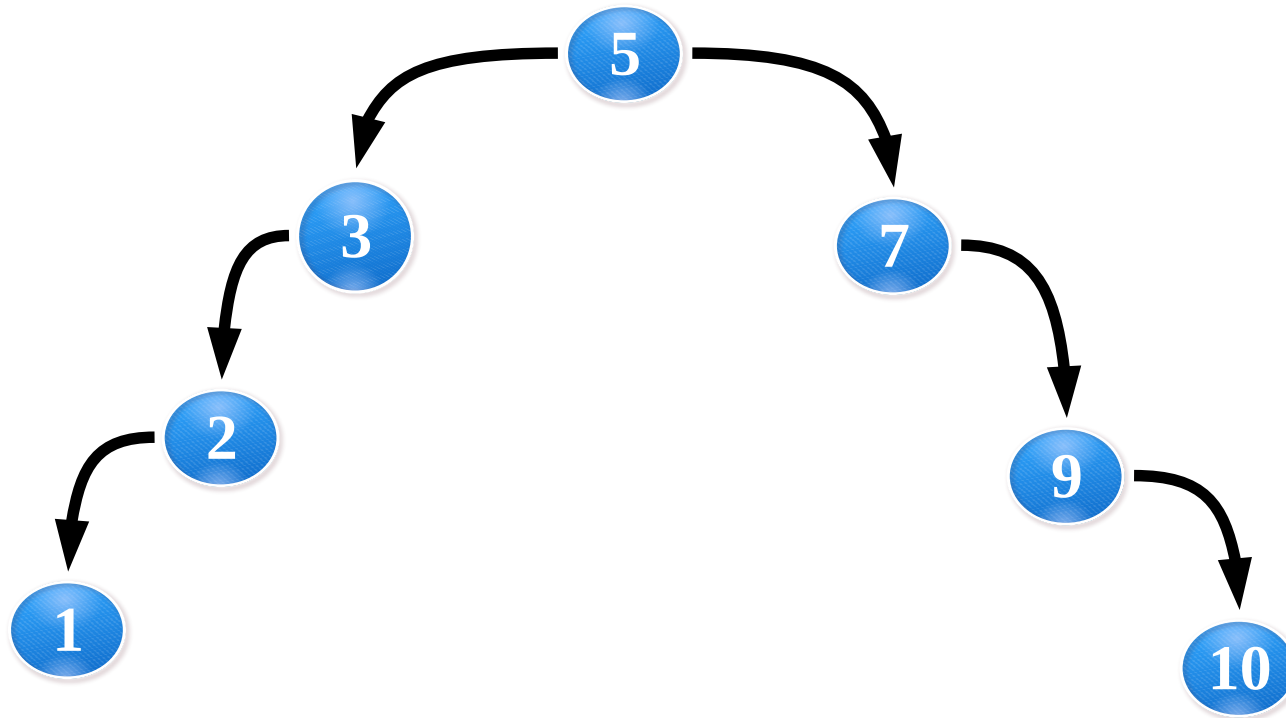
Dinamički alocirano stablo

5	7	3	2	9	1		
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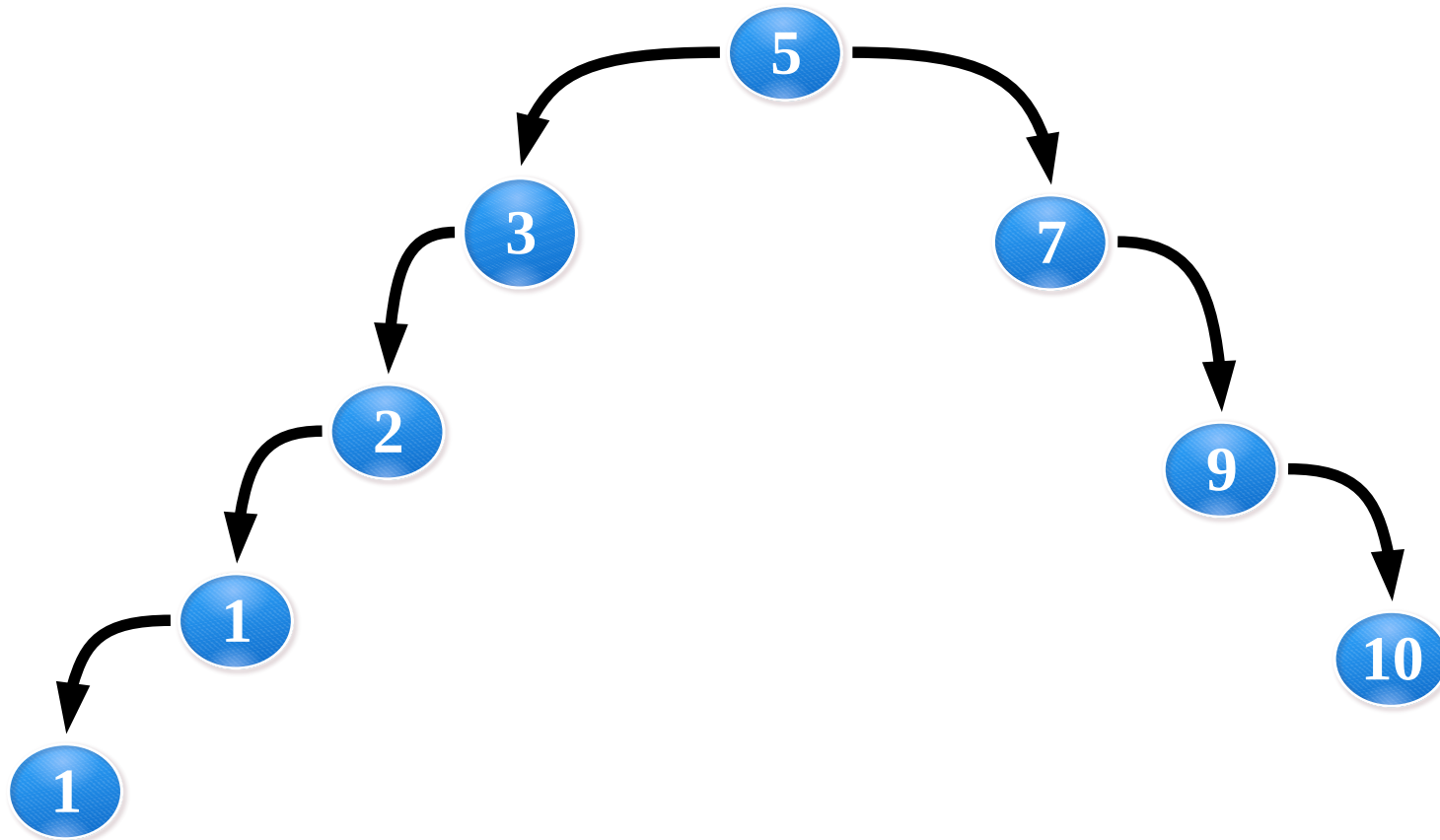
Dinamički alocirano stablo

5	7	3	2	9	1	10		
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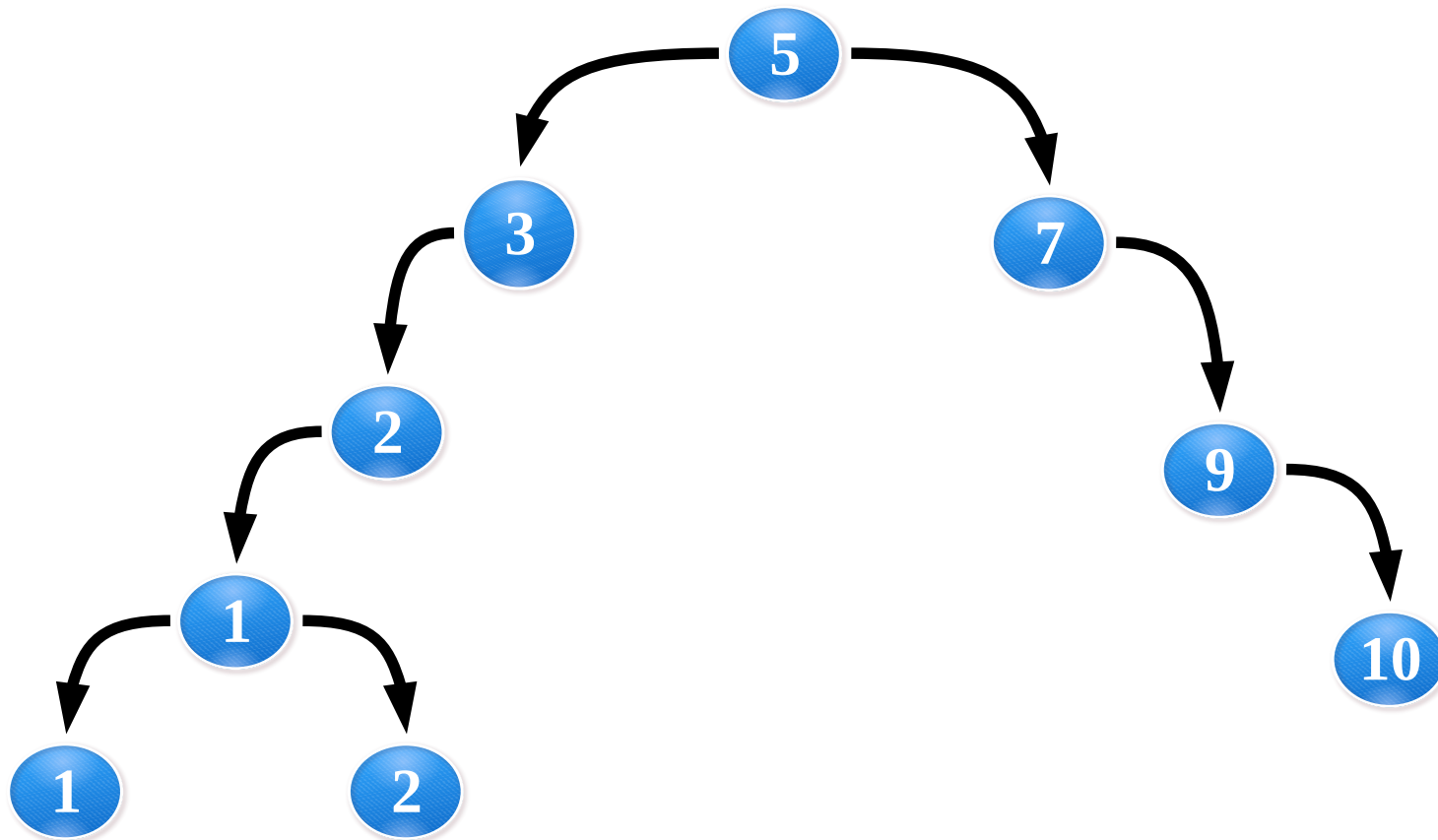
Dinamički alocirano stablo

5	7	3	2	9	1	10	1	
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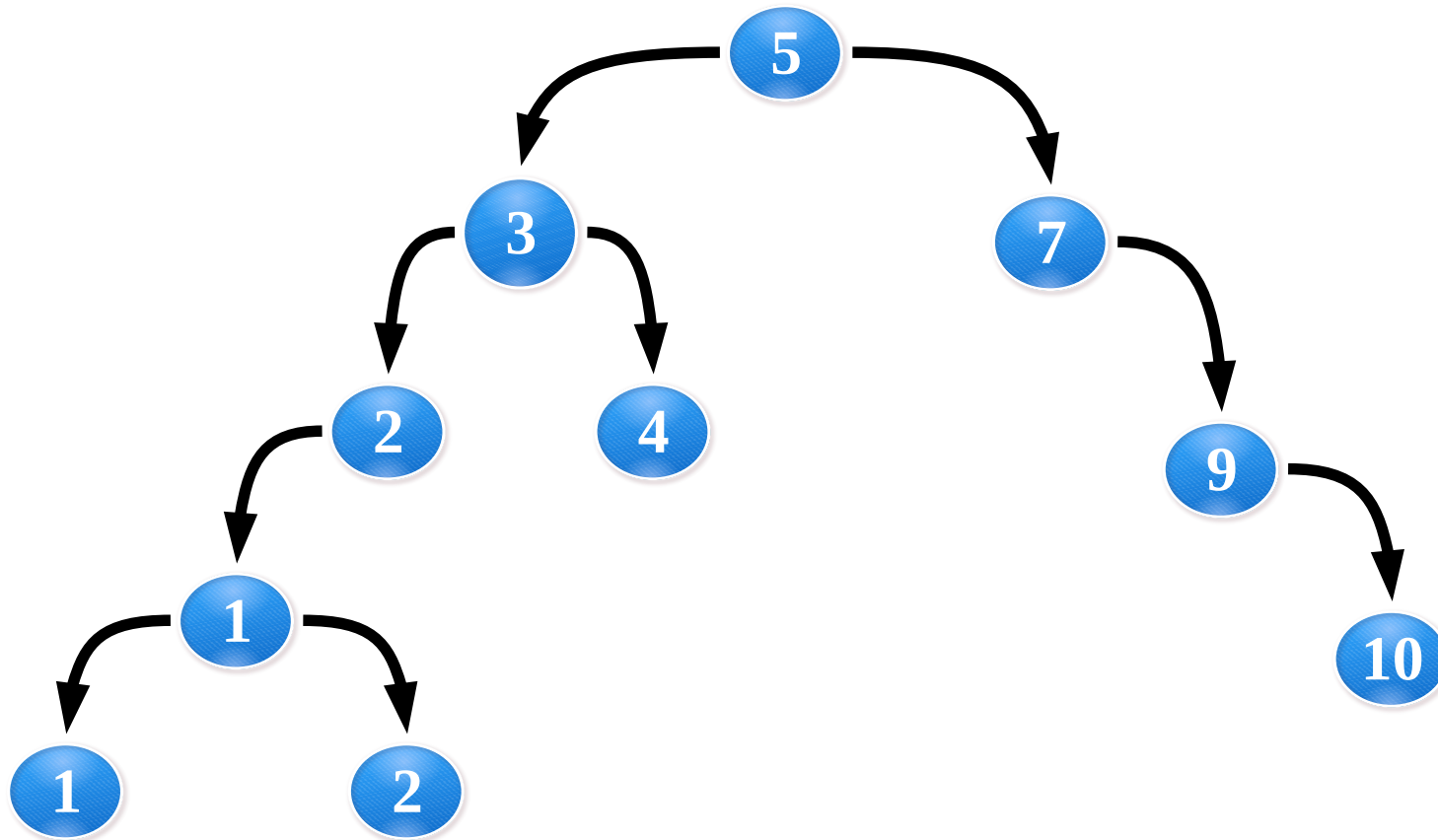
Dinamički alocirano stablo

5	7	3	2	9	1	10	1	2
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Dinamički alocirano stablo

5	7	3	2	9	1	10	1	2	4
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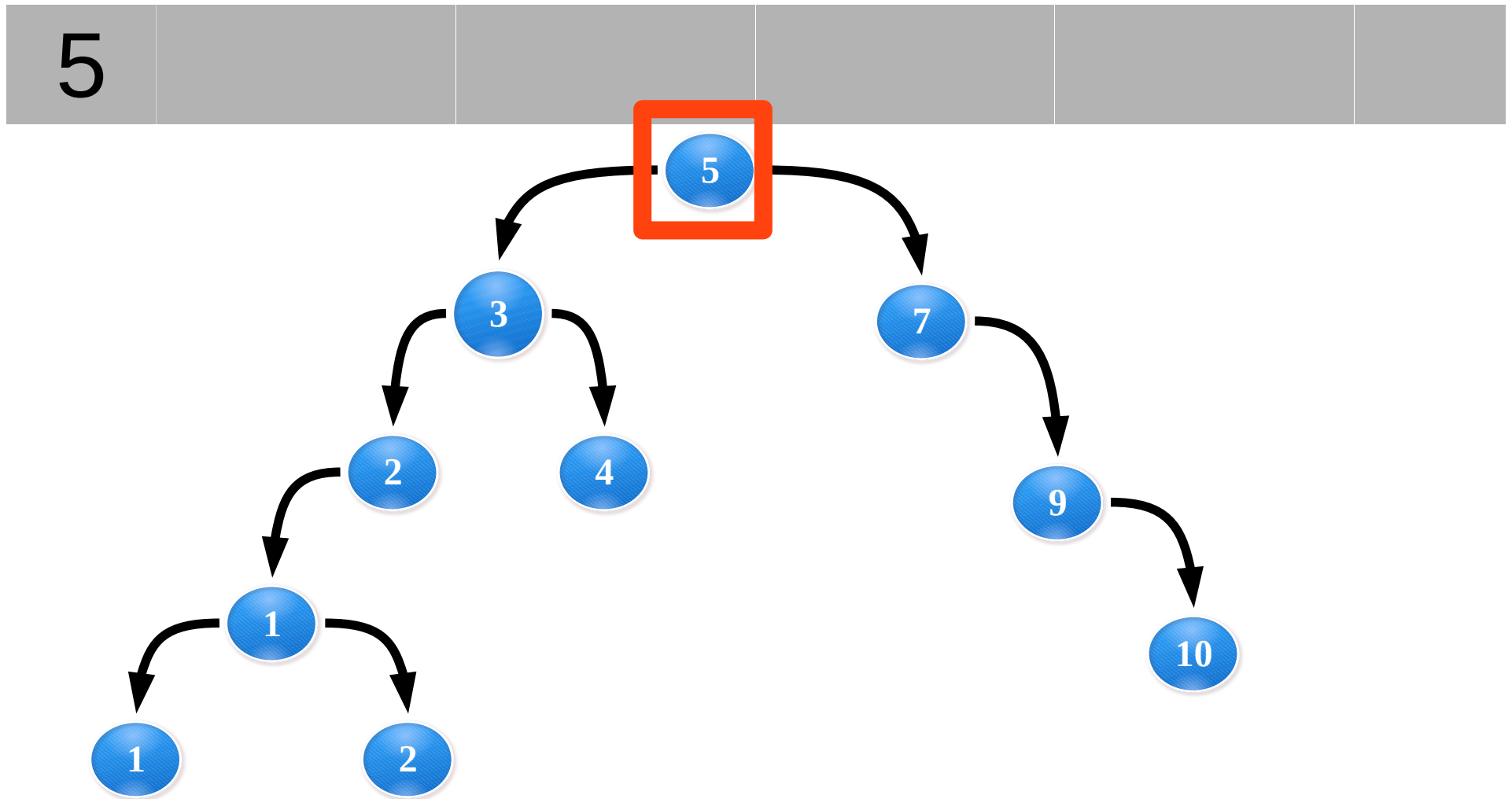
Dinamički alocirano stablo

```
72 template <class T>
73 void BinaryTree<T>::insertElement(BinaryNode<T>* current, const T& elem) {
74     if ((*current).data < elem)
75     {
76         if (current->right == NULL)
77         {
78             current->right = new BinaryNode<T>(elem);
79             return;
80         }
81         insertElement(current->right, elem);
82     }
83     else
84     {
85         if (current->left == NULL)
86         {
87             current->left = new BinaryNode<T>(elem);
88             return;
89         }
90         insertElement(current->left, elem);
91     }
92 }
93 }
94 }
95 }
```

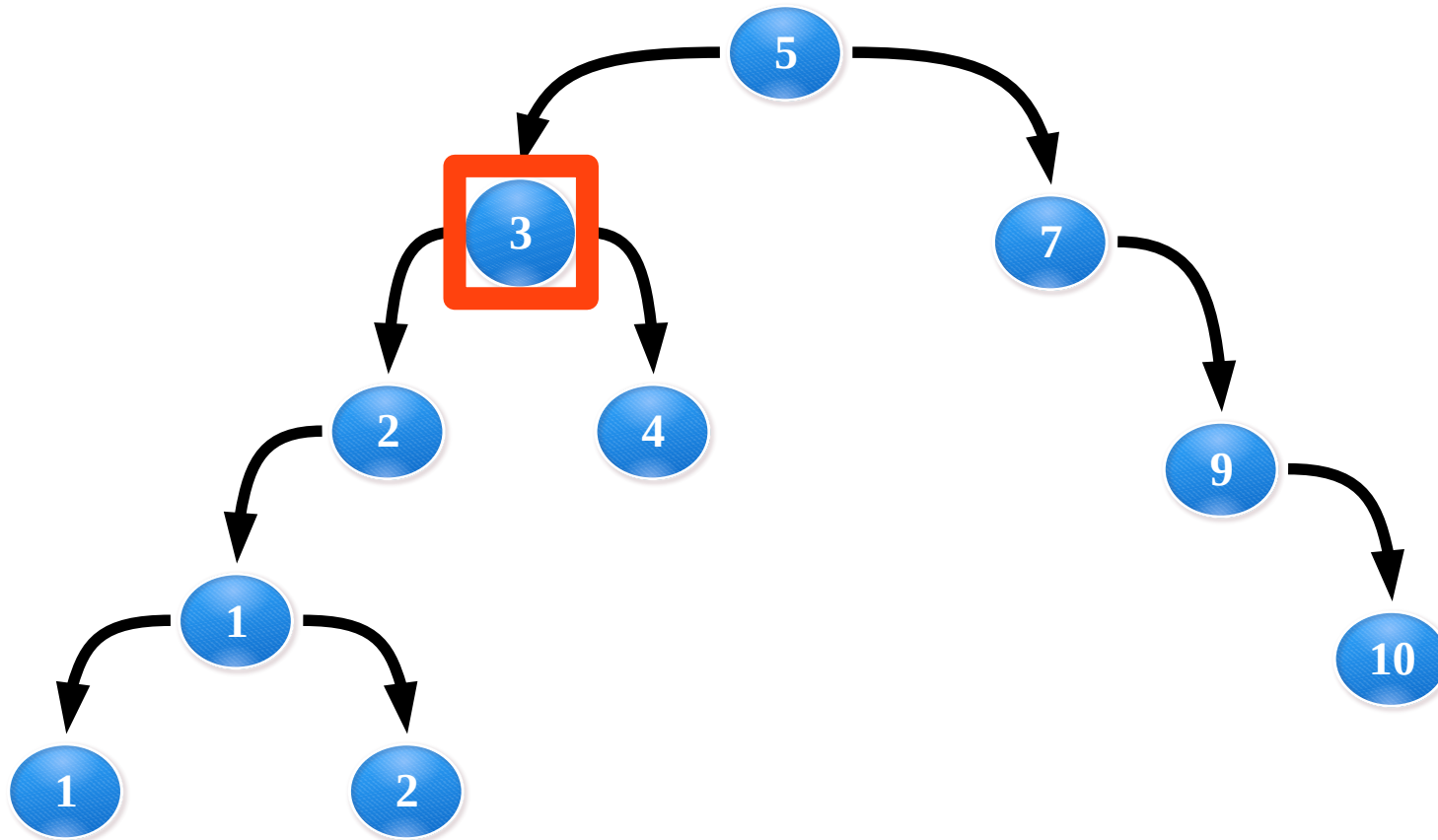
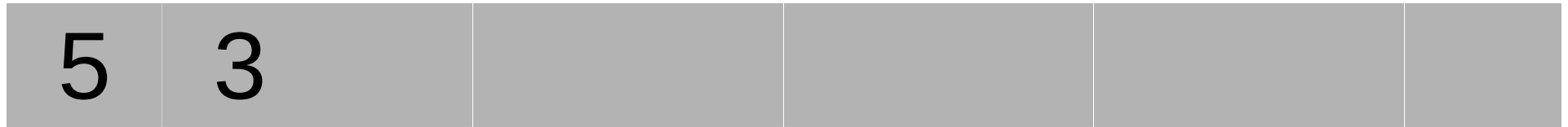
Statički alocirano stablo

- 1) Blok memorije (spatial locality)
- 2) Raspored elemenata (spatial locality)
- 3) Nema new (malloc) overhead-a

Statički alocirano stablo (DFS lijevo)

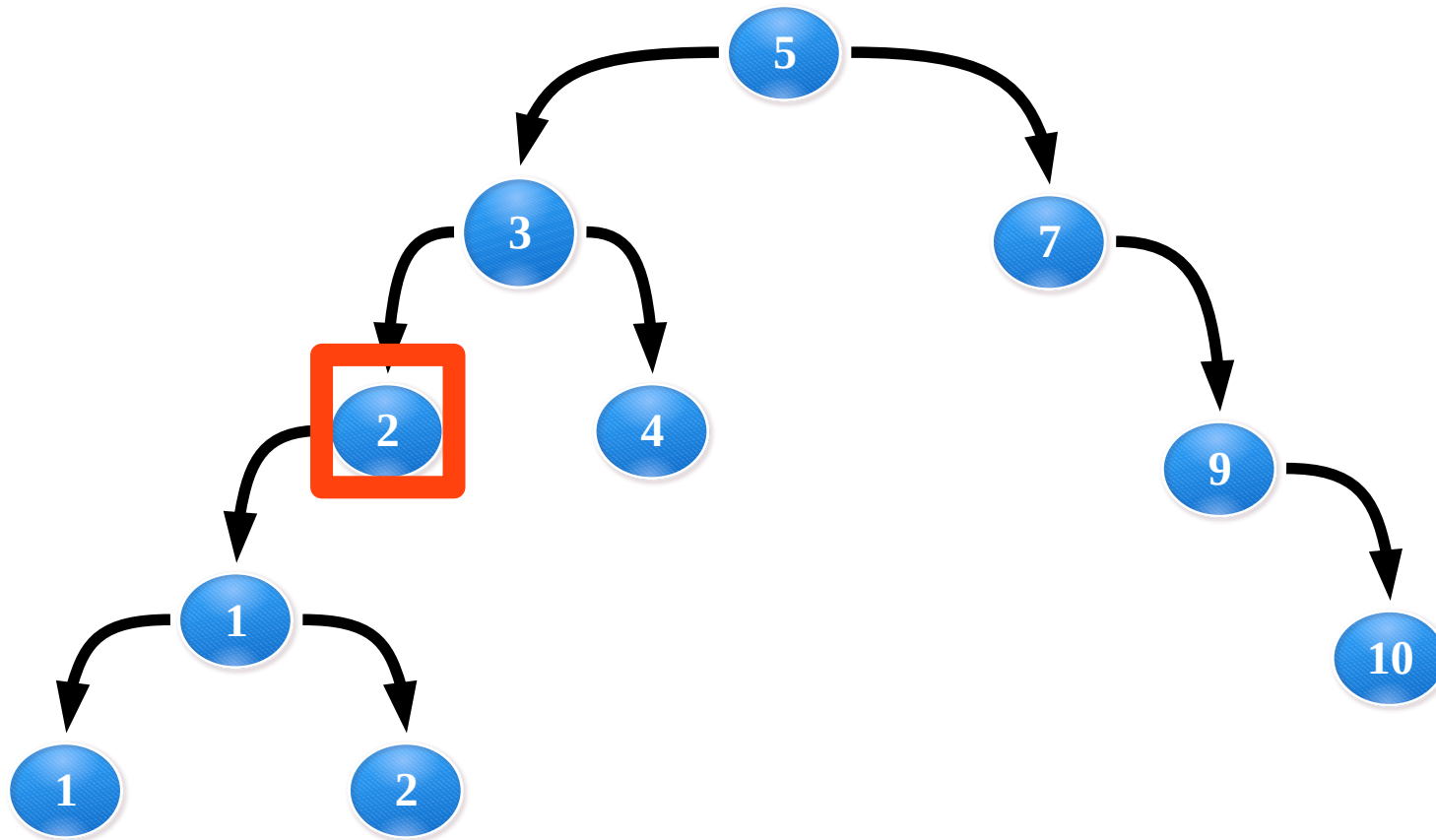


Statički alocirano stablo (DFS lijevo)



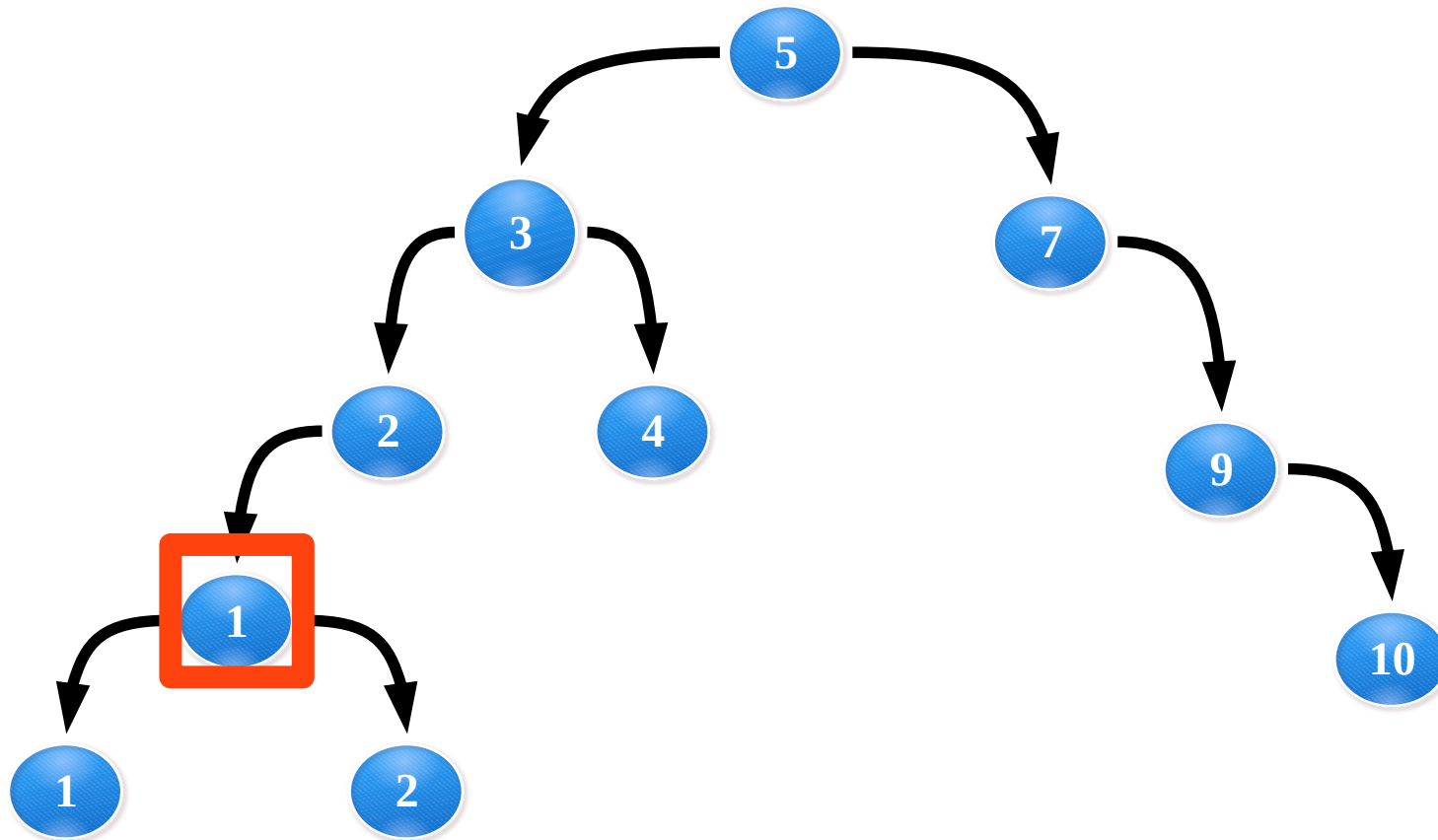
Statički alocirano stablo (DFS lijevo)

5	3	2				
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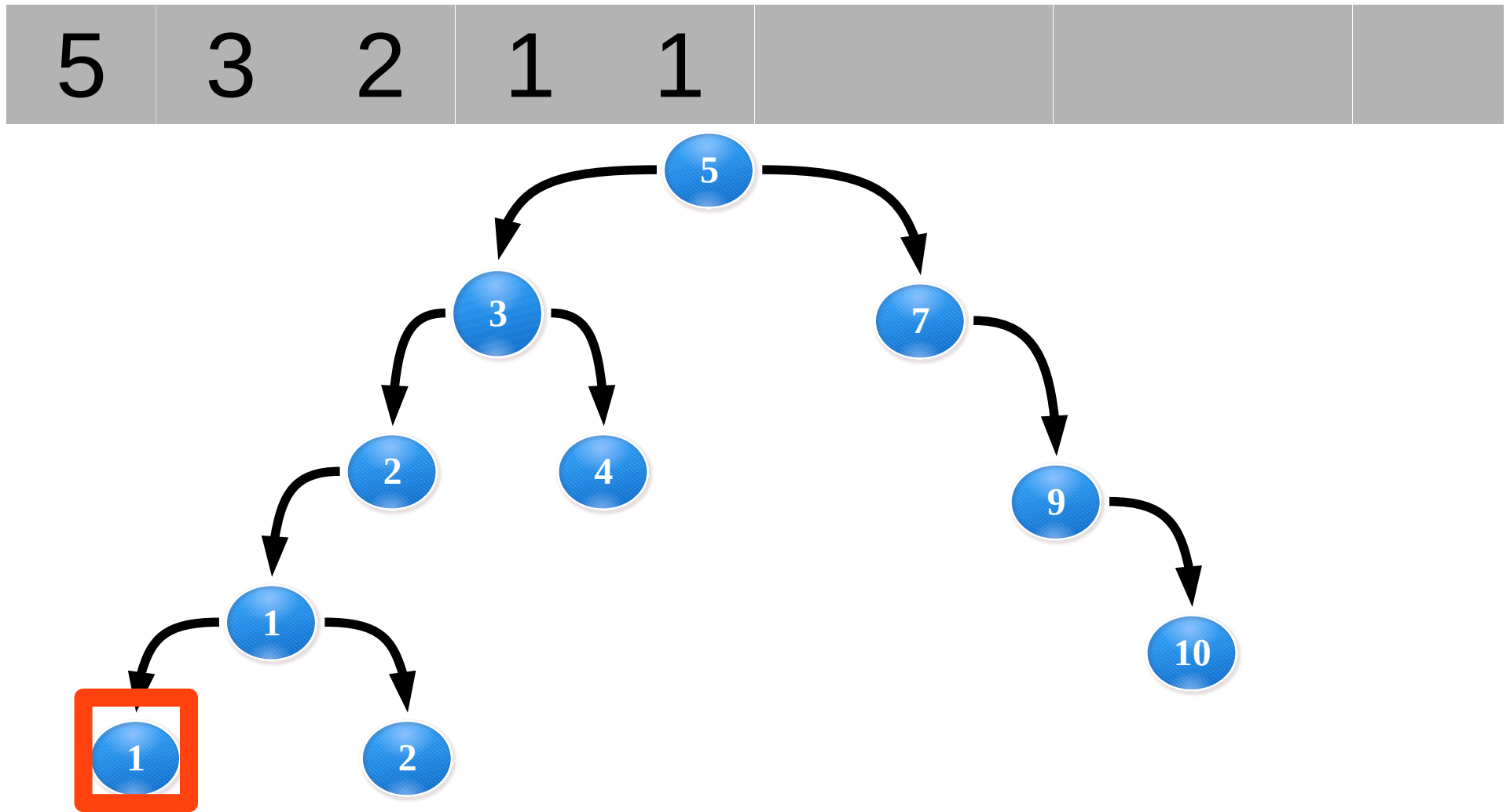


Statički alocirano stablo (DFS lijevo)

5	3	2	1			
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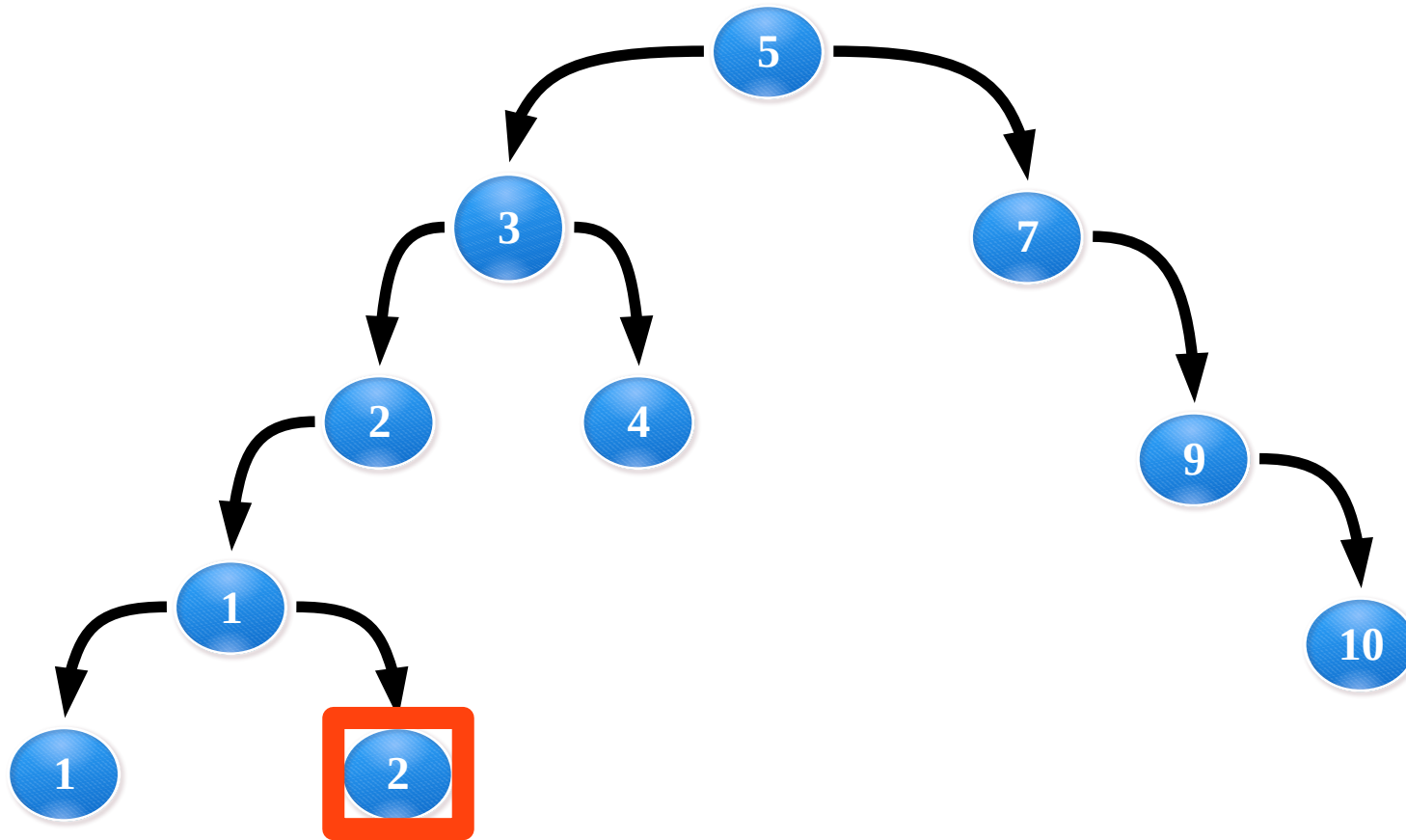


Statički alocirano stablo (DFS lijevo)



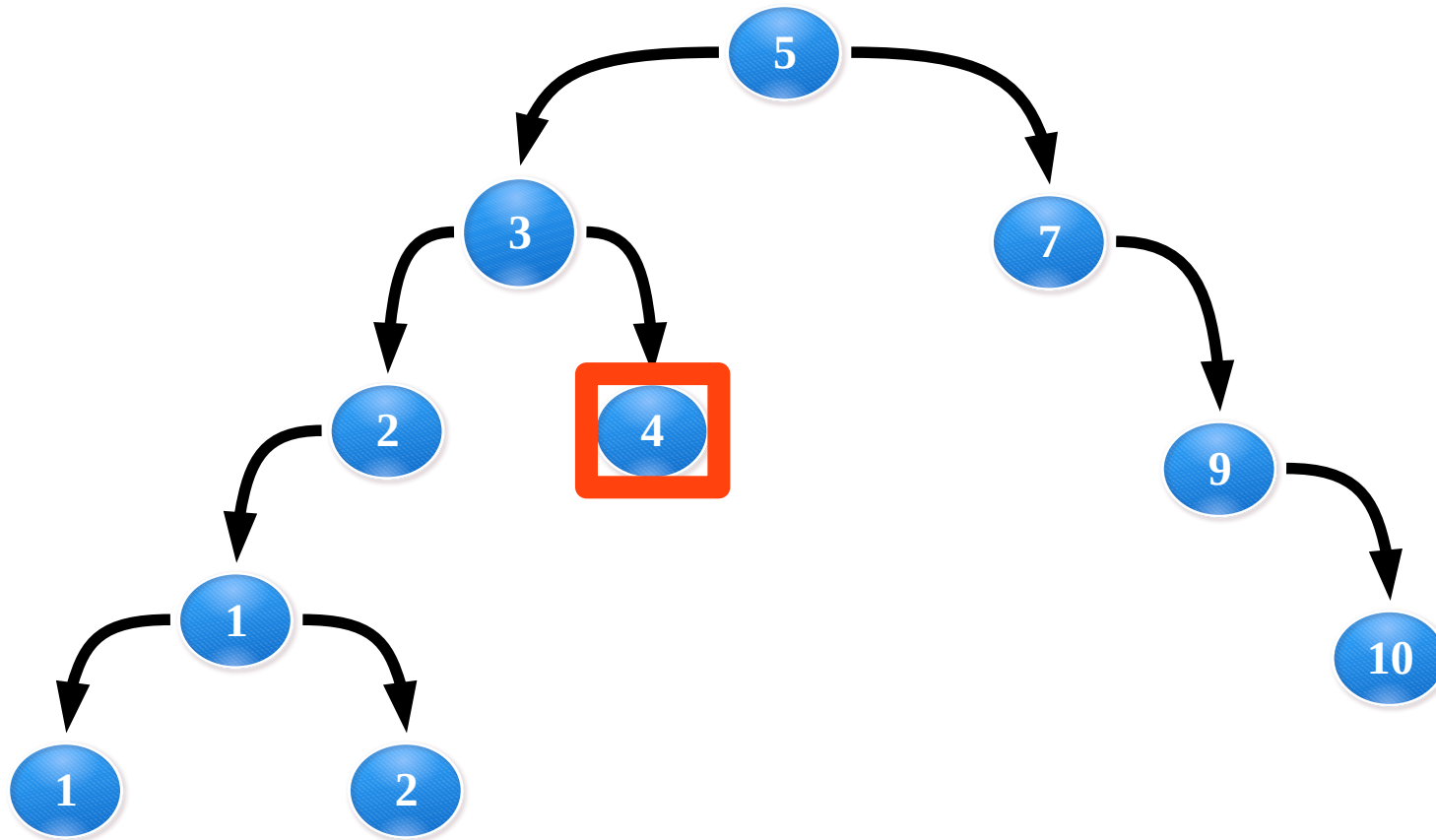
Statički alocirano stablo (DFS lijevo)

5	3	2	1	1	2		
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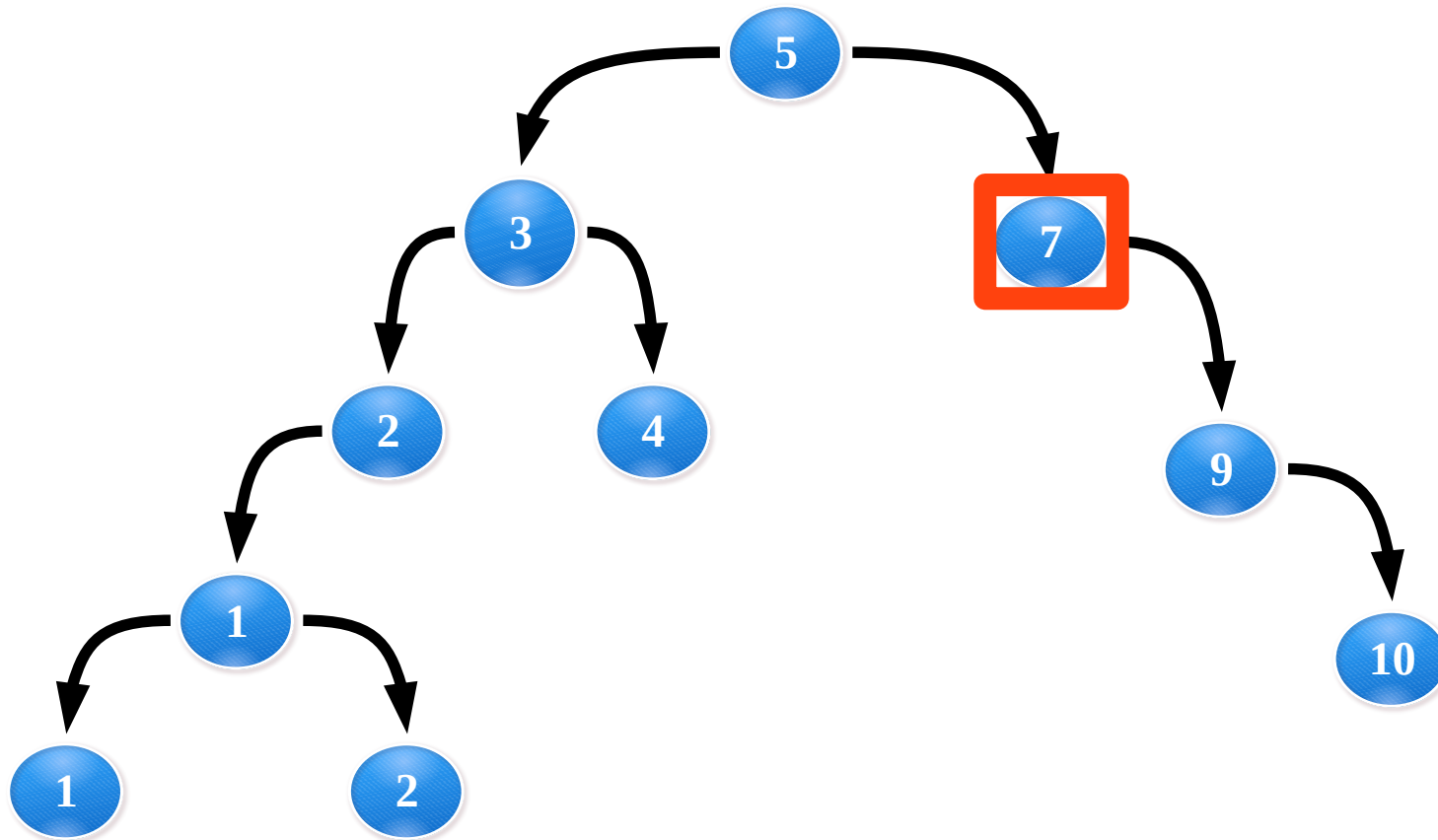
Statički alocirano stablo (DFS lijevo)

5	3	2	1	1	2	4		
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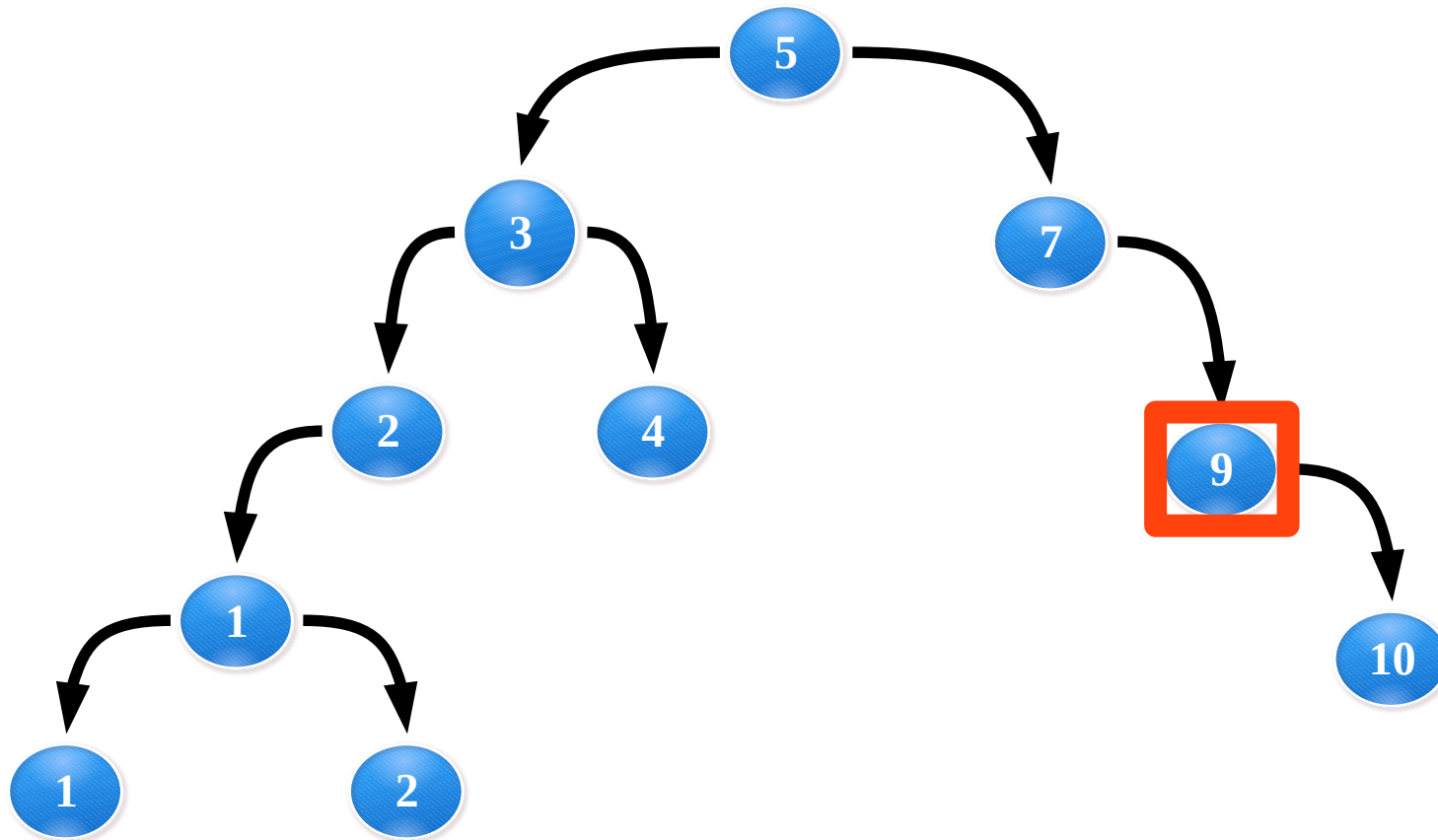
Statički alocirano stablo (DFS lijevo)

5	3	2	1	1	2	4	7		
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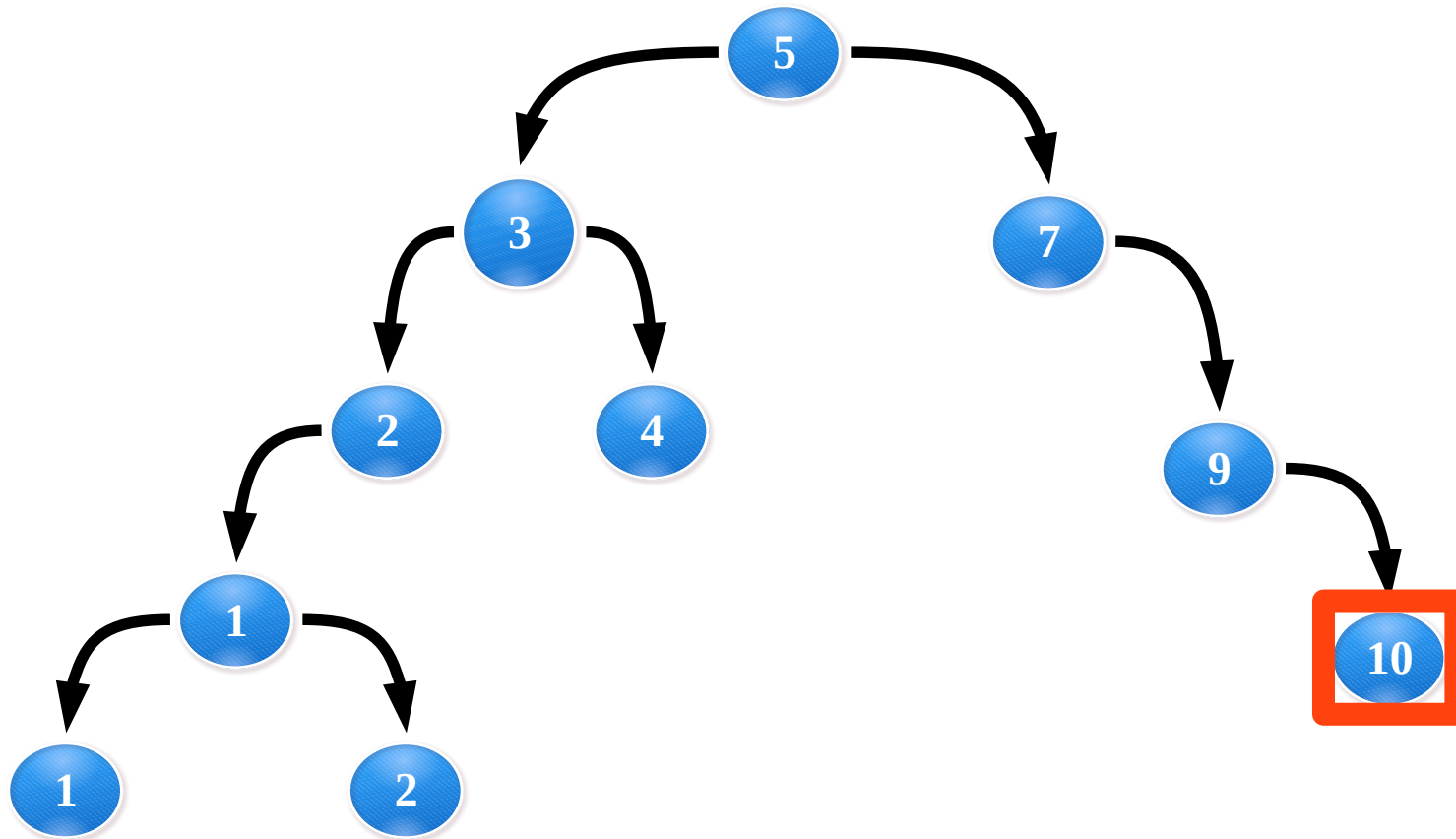
Statički alocirano stablo (DFS lijevo)

5	3	2	1	1	2	4	7	9	
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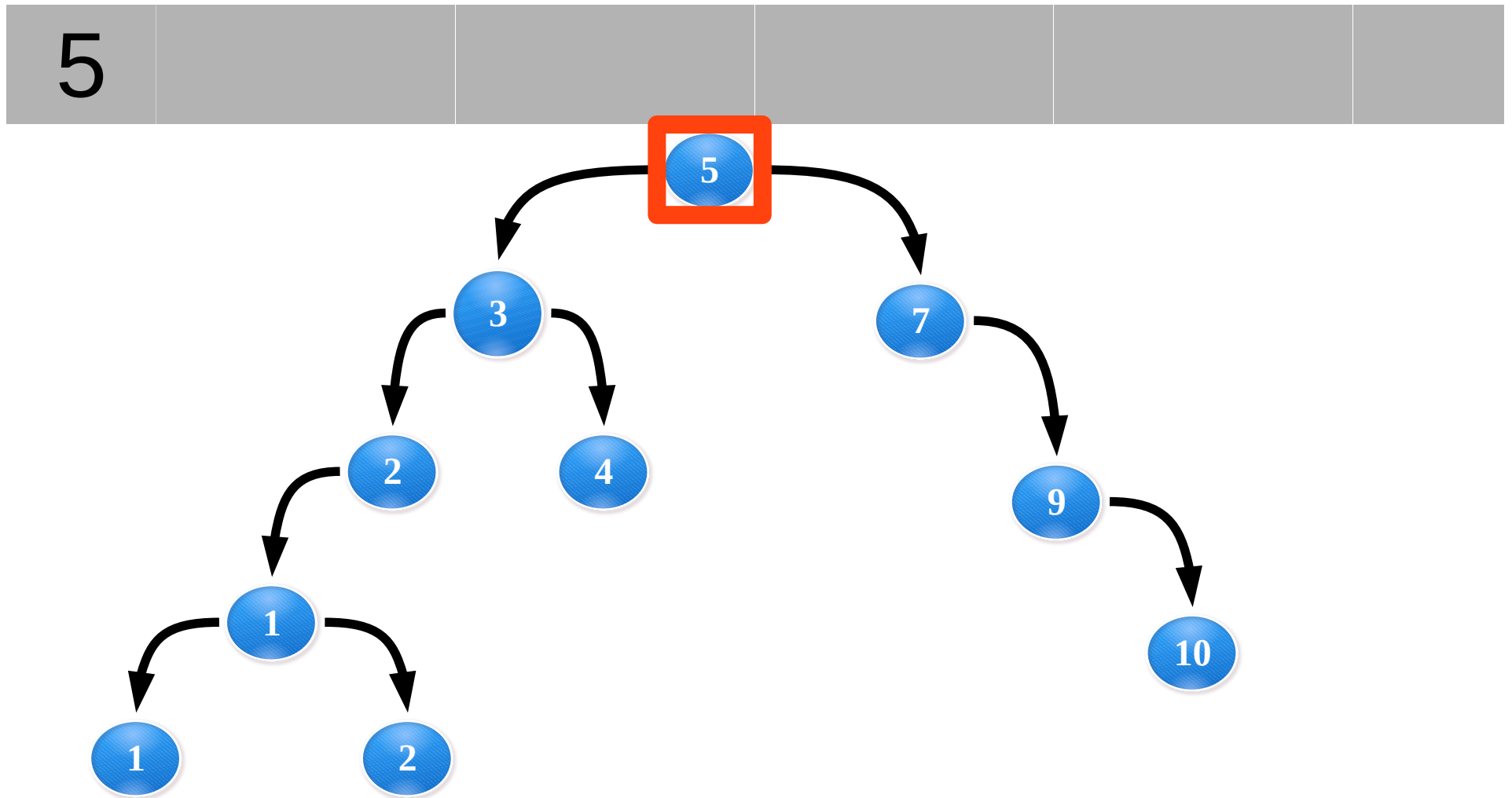


Statički alocirano stablo (DFS lijevo)

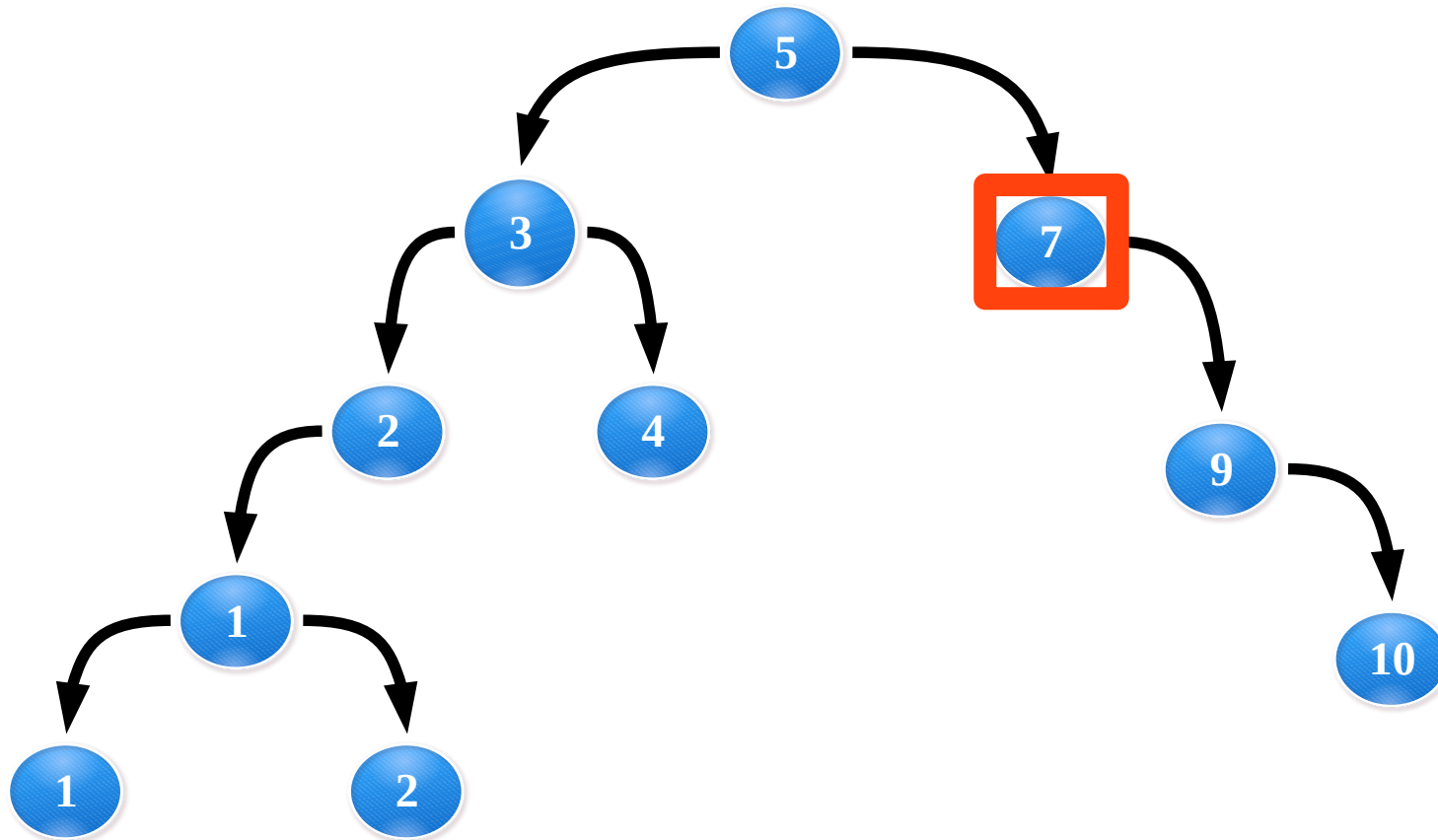
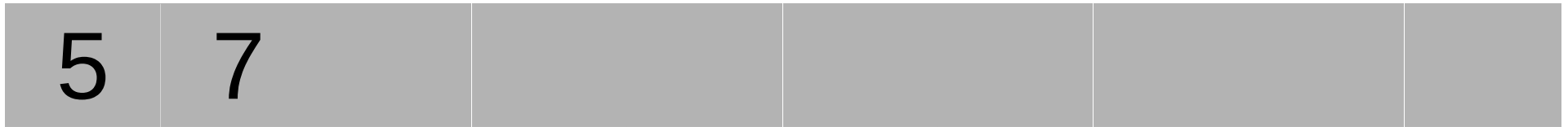
5	3	2	1	1	2	4	7	9	10
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Statički alocirano stablo (DFS desno)

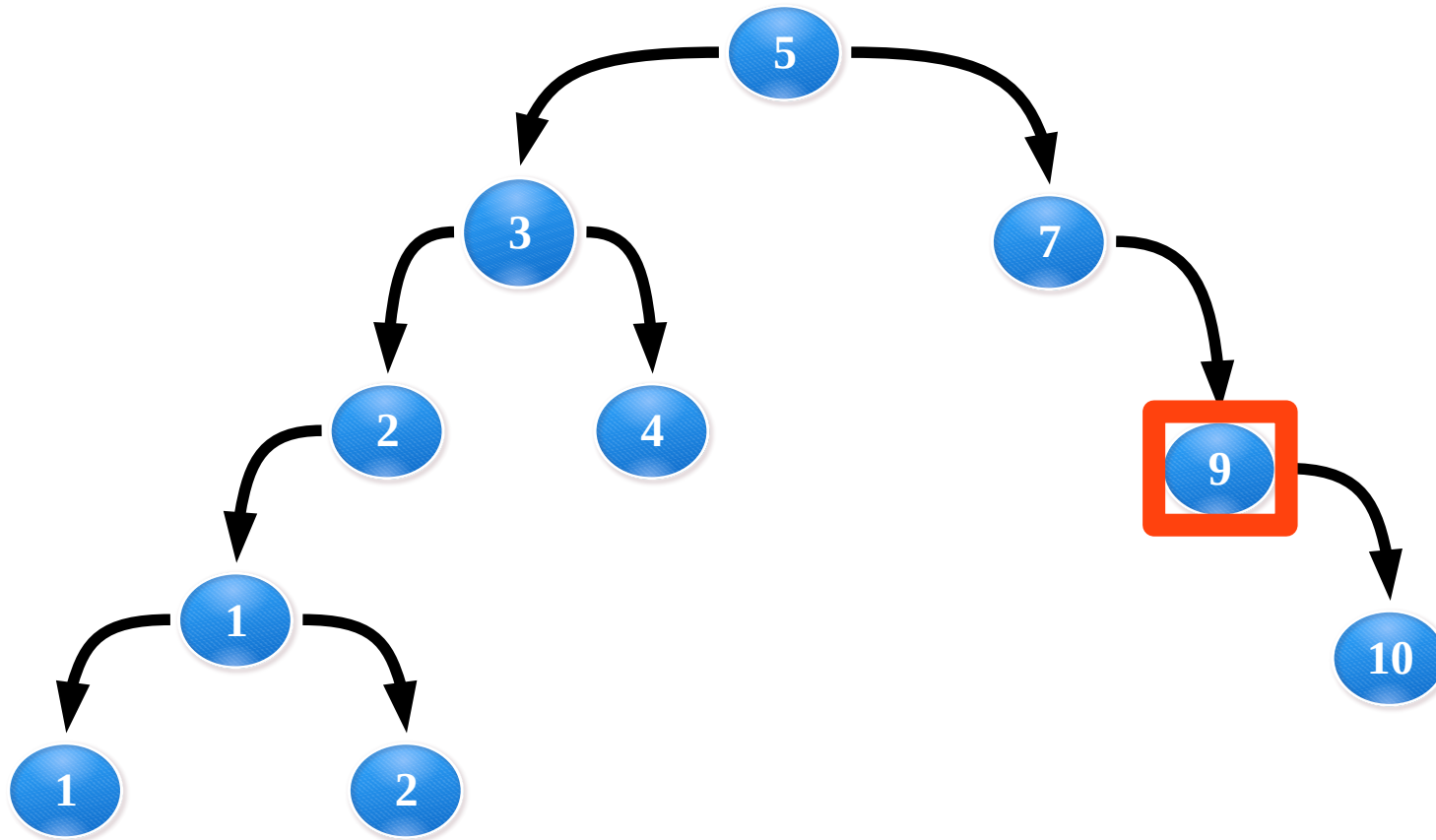


Statički alocirano stablo (DFS desno)



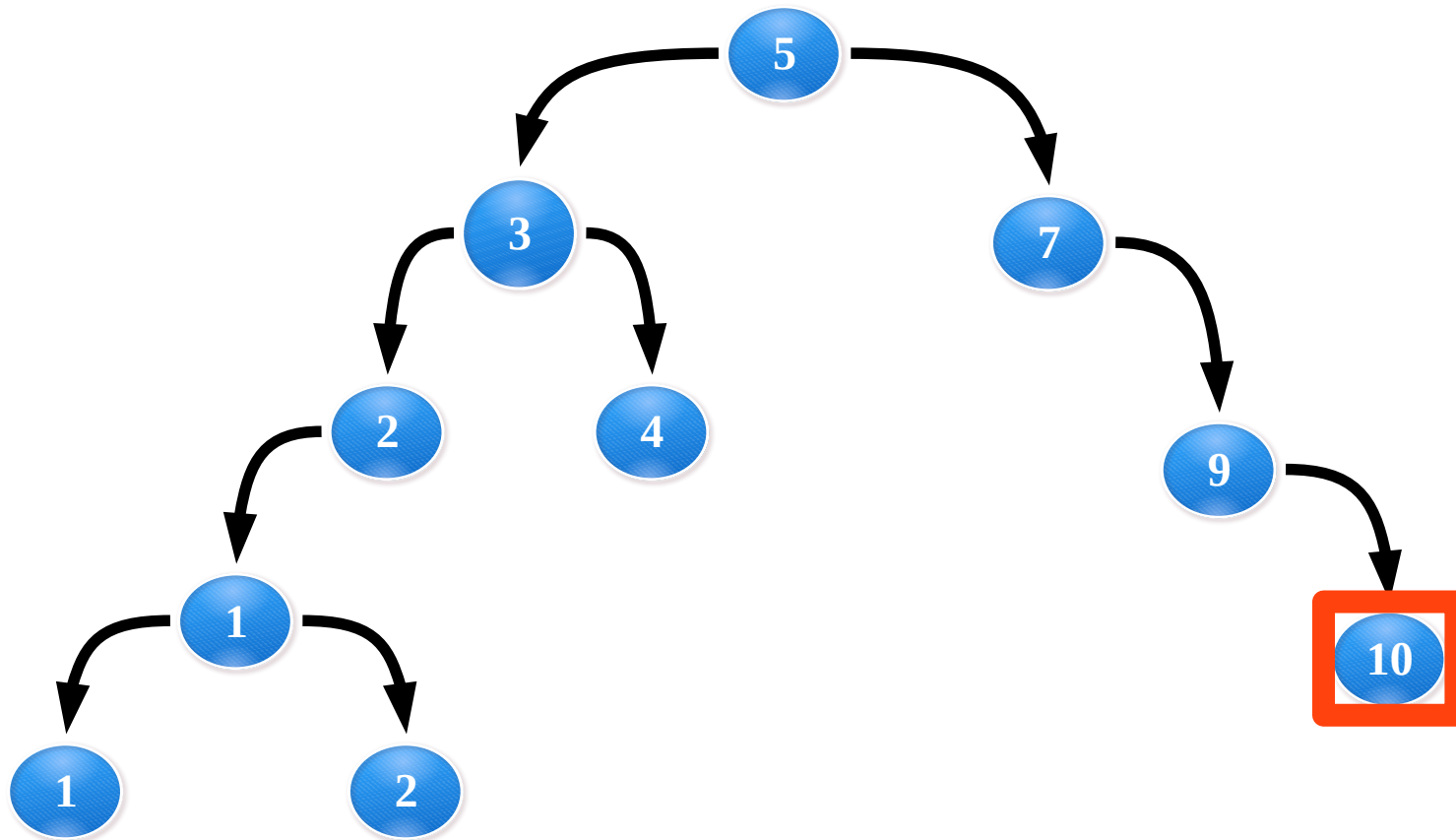
Statički alocirano stablo (DFS desno)

5	7	9				
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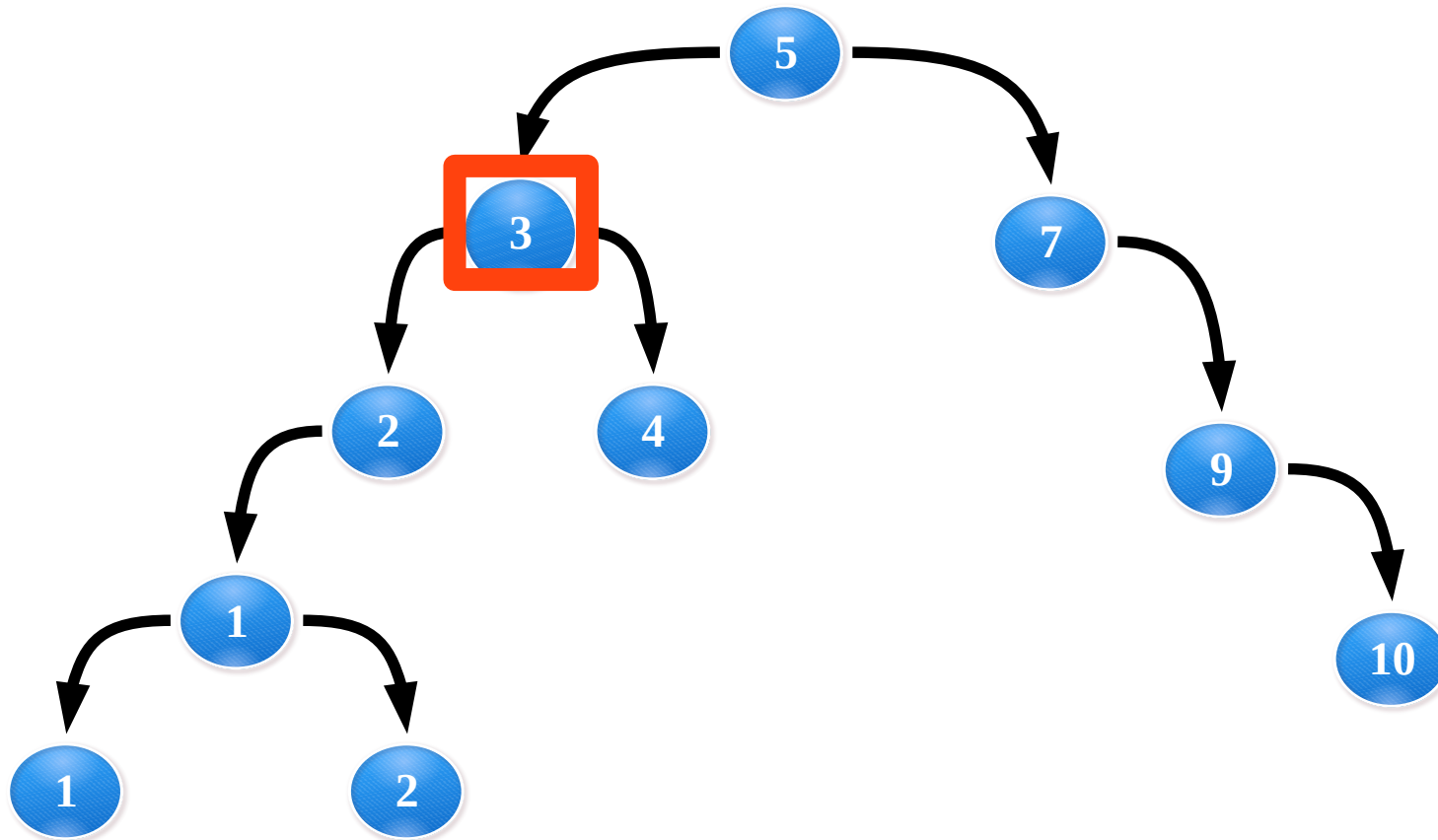
Statički alocirano stablo (DFS desno)

5	7	9	10			
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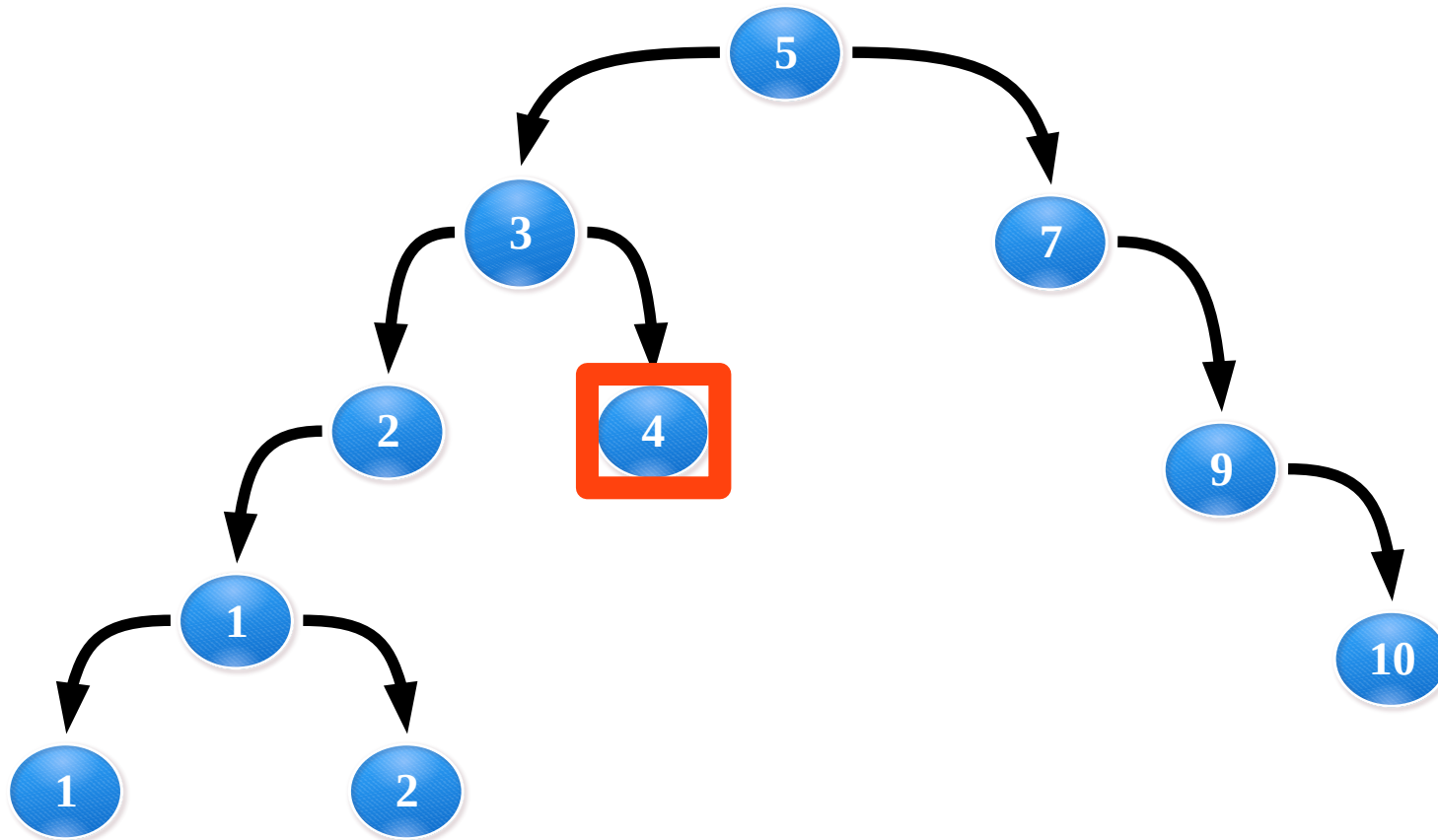
Statički alocirano stablo (DFS desno)

5	7	9	10	3			
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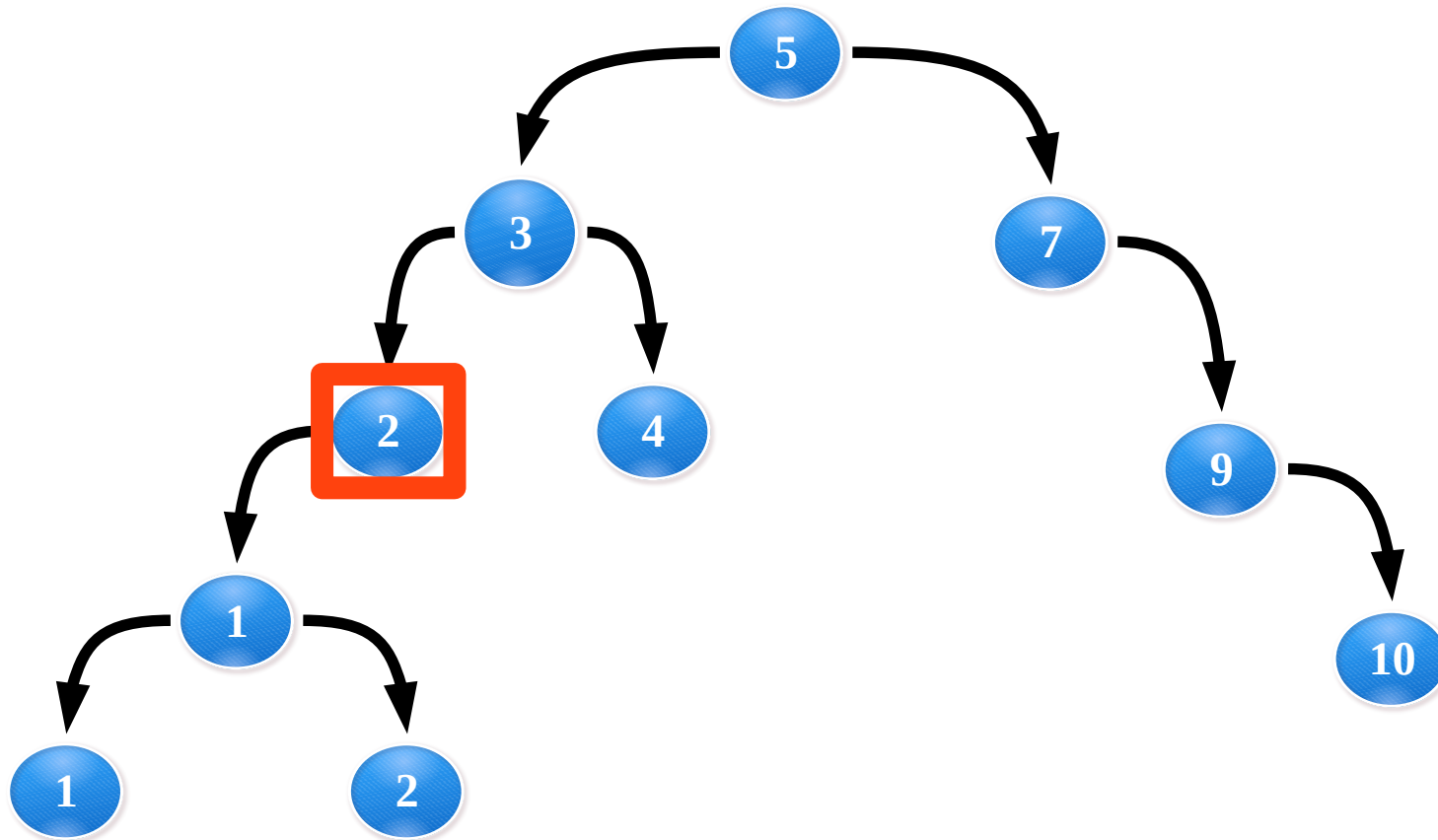
Statički alocirano stablo (DFS desno)

5	7	9	10	3	4		
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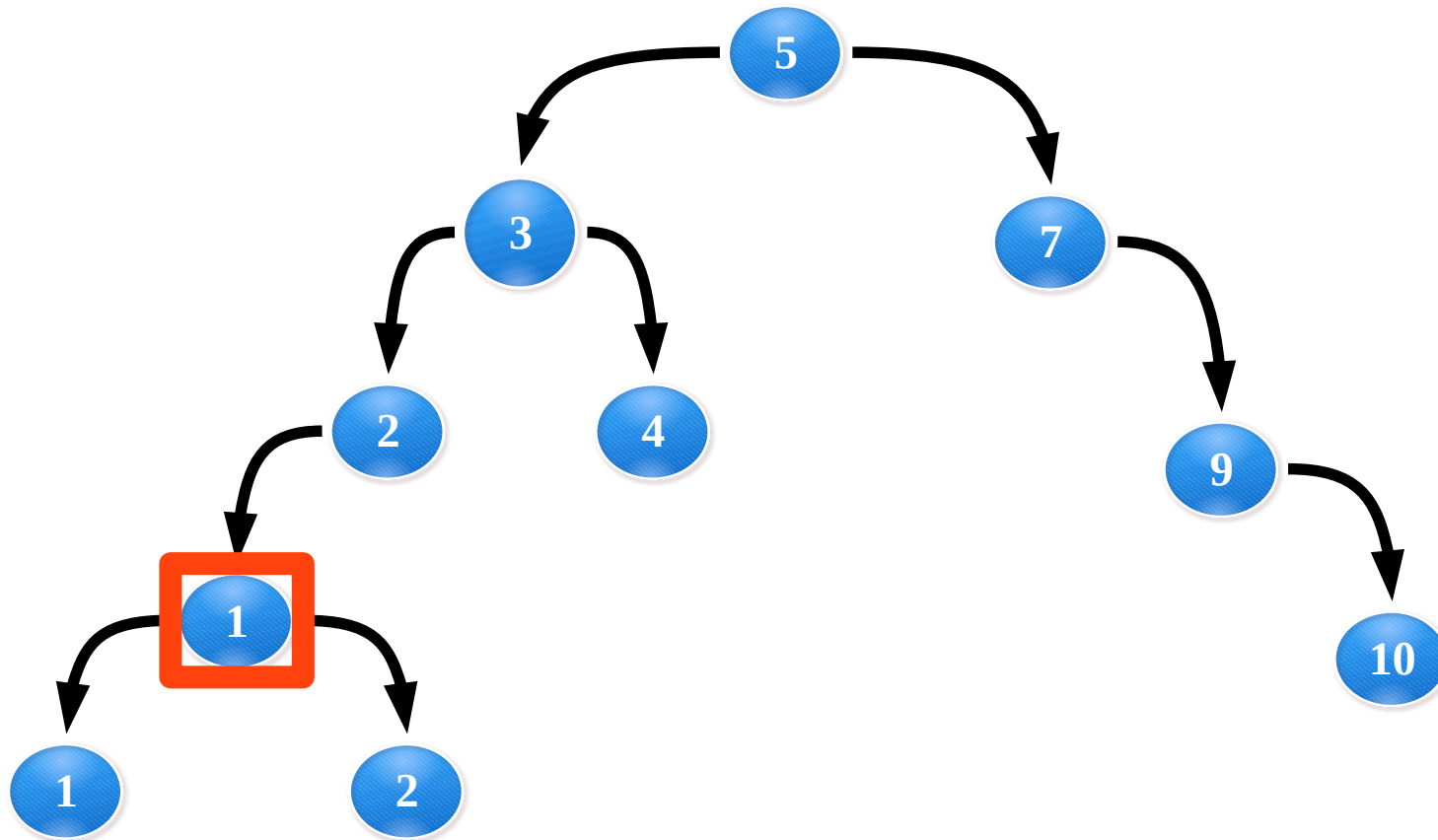
Statički alocirano stablo (DFS desno)

5	7	9	10	3	4	2		
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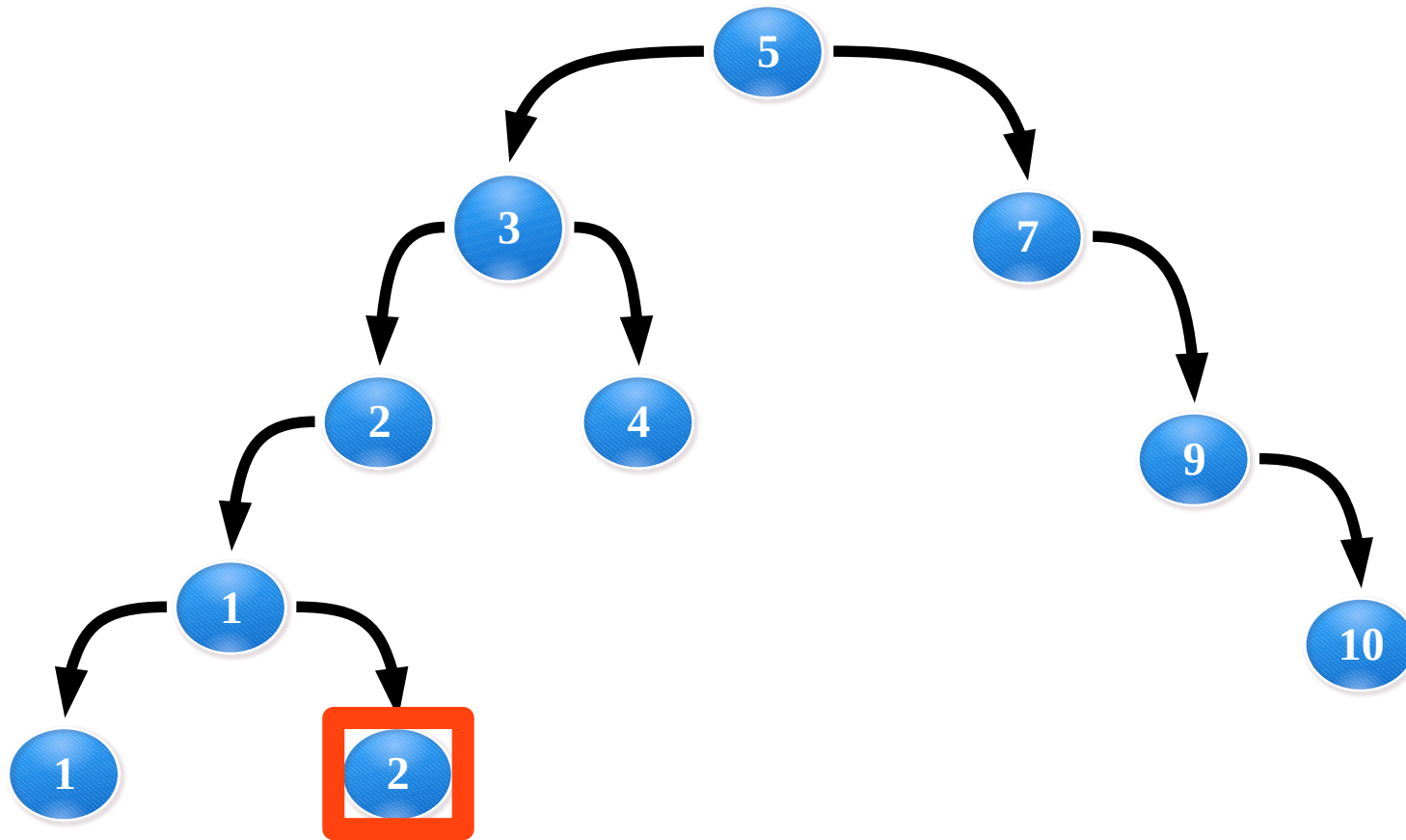
Statički alocirano stablo (DFS desno)

5	7	9	10	3	4	2	1	
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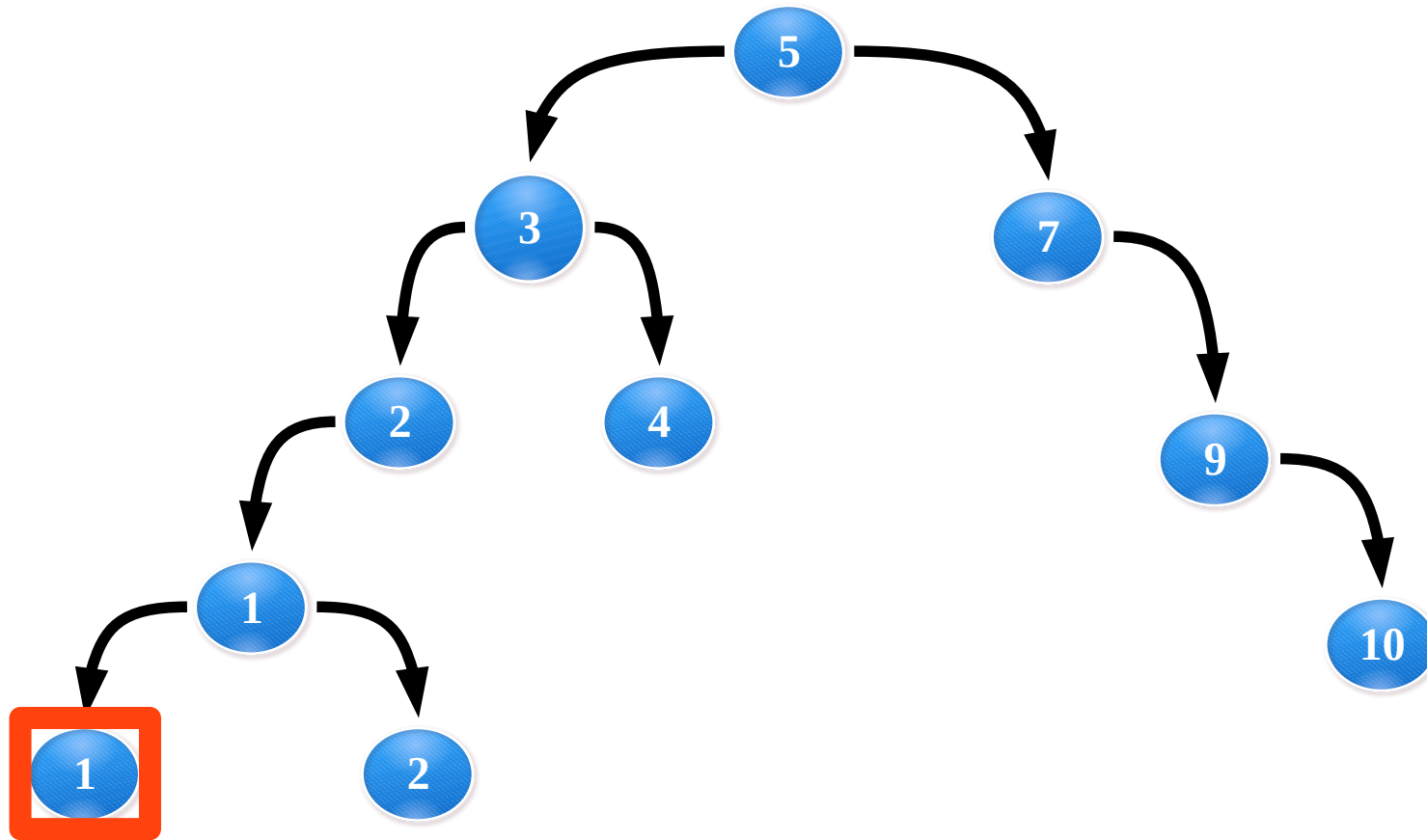
Statički alocirano stablo (DFS desno)

5	7	9	10	3	4	2	1	2	
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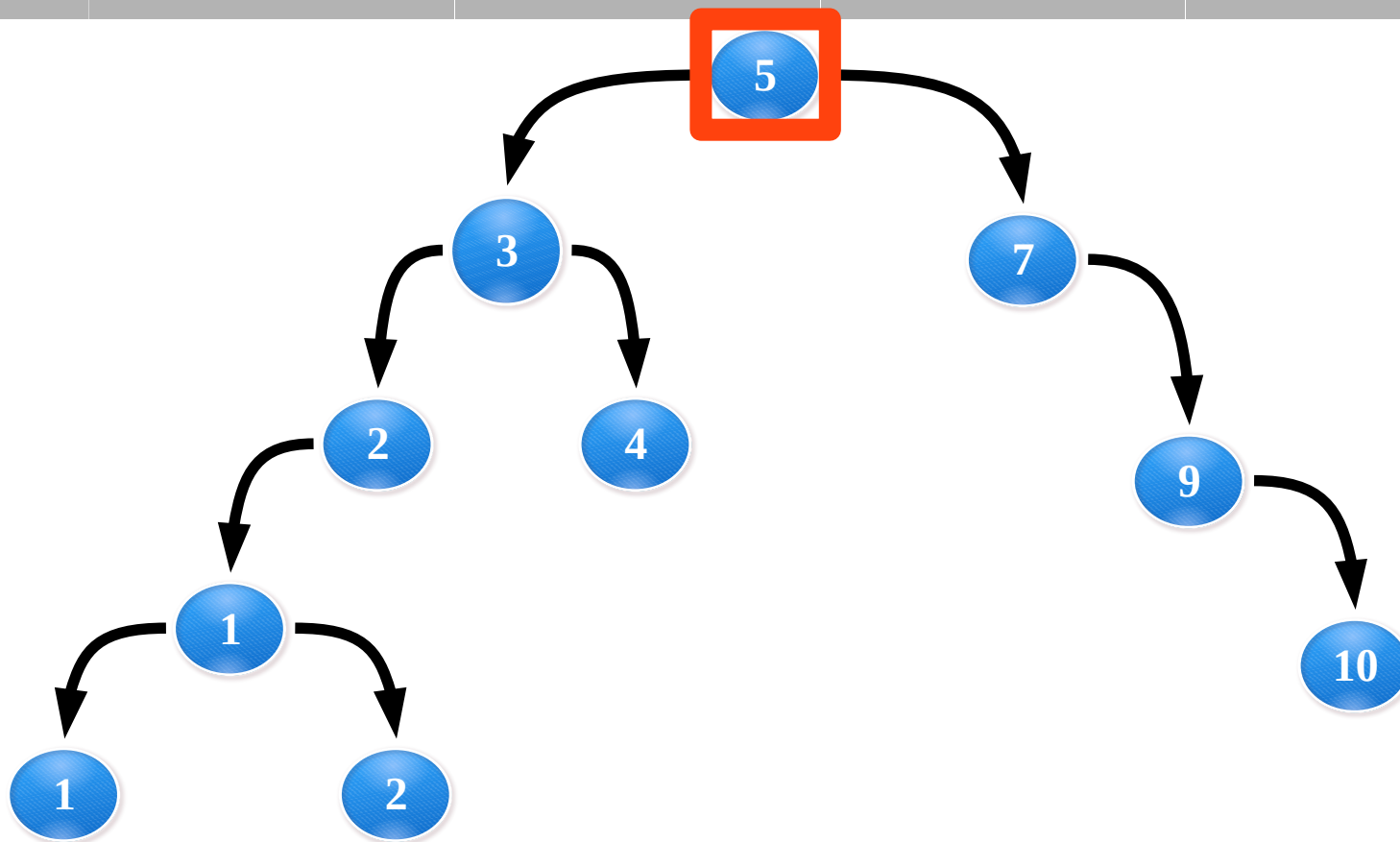
Statički alocirano stablo (DFS desno)

5	7	9	10	3	4	2	1	2	1
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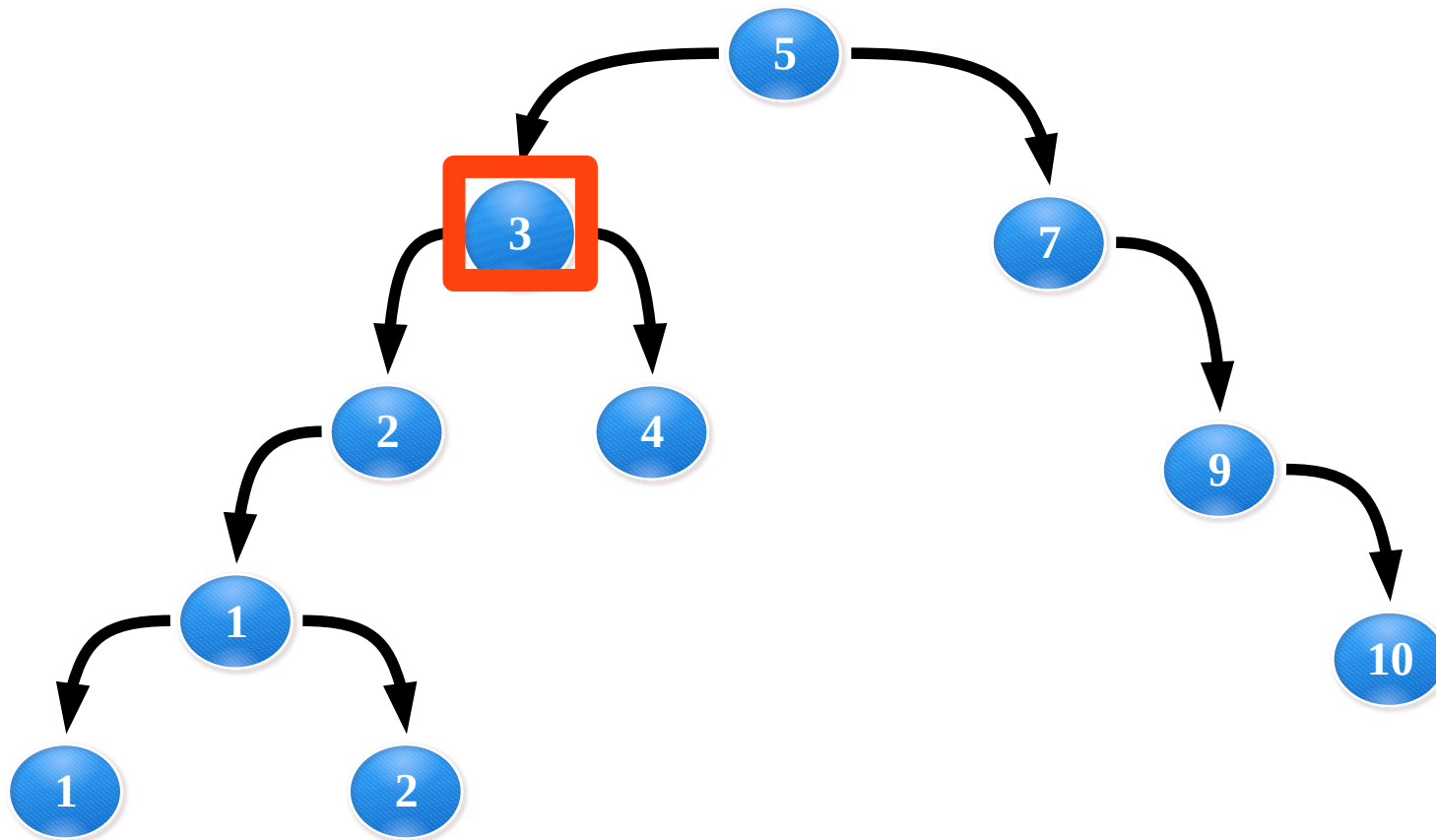
Statički alocirano stablo (BFS)

5



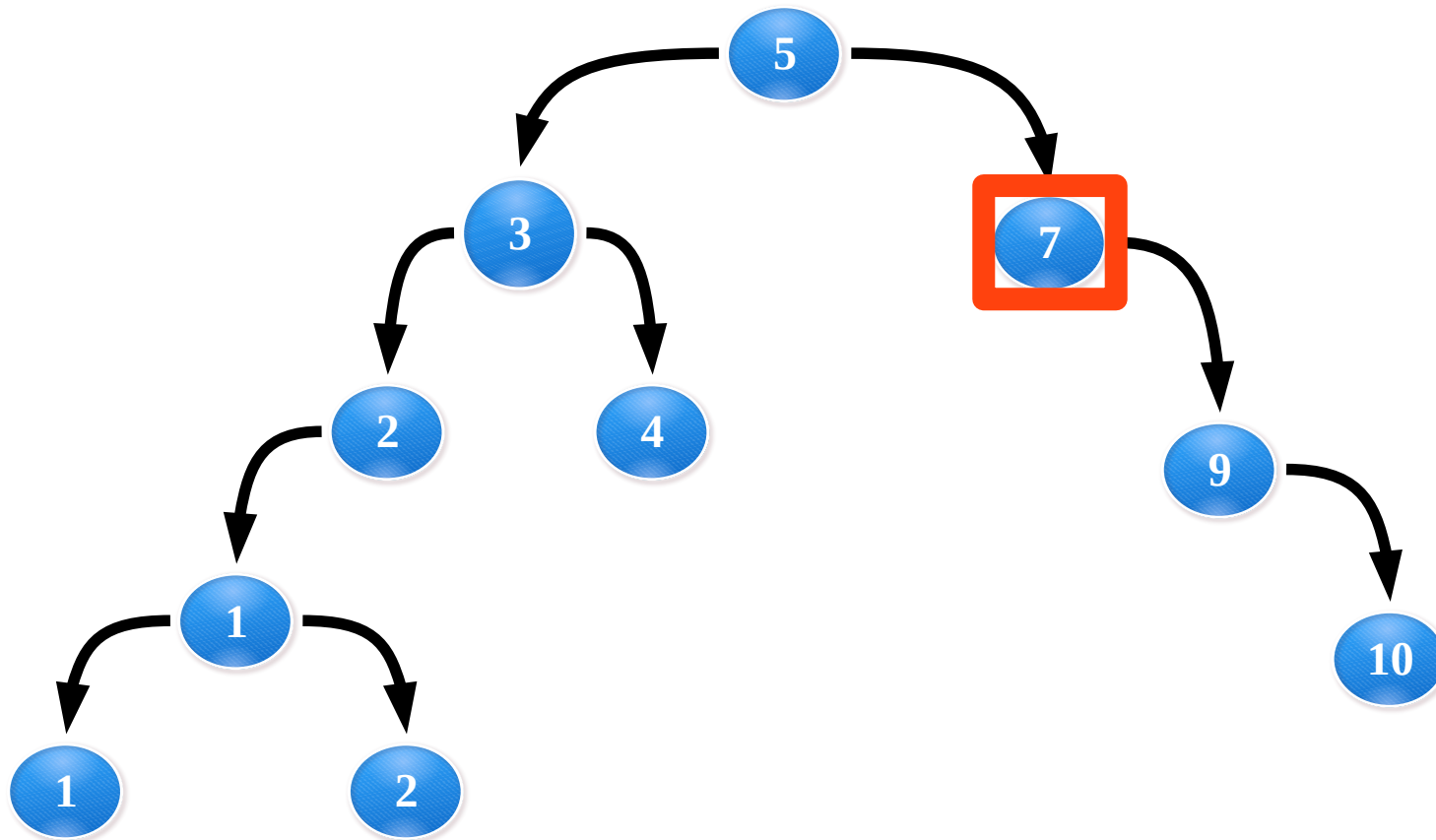
Statički alocirano stablo (BFS)

5	3				
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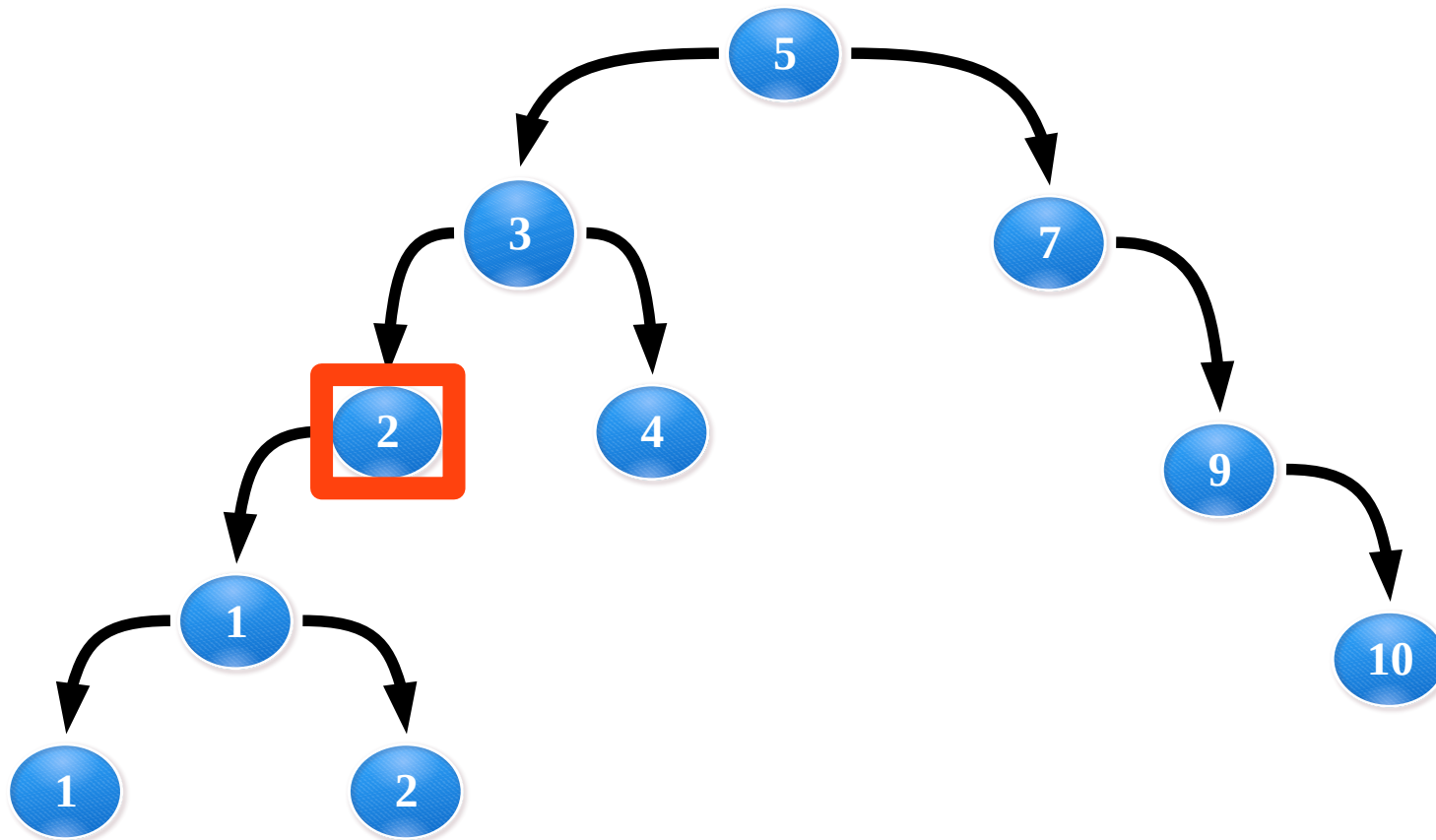
Statički alocirano stablo (BFS)

5	3	7				
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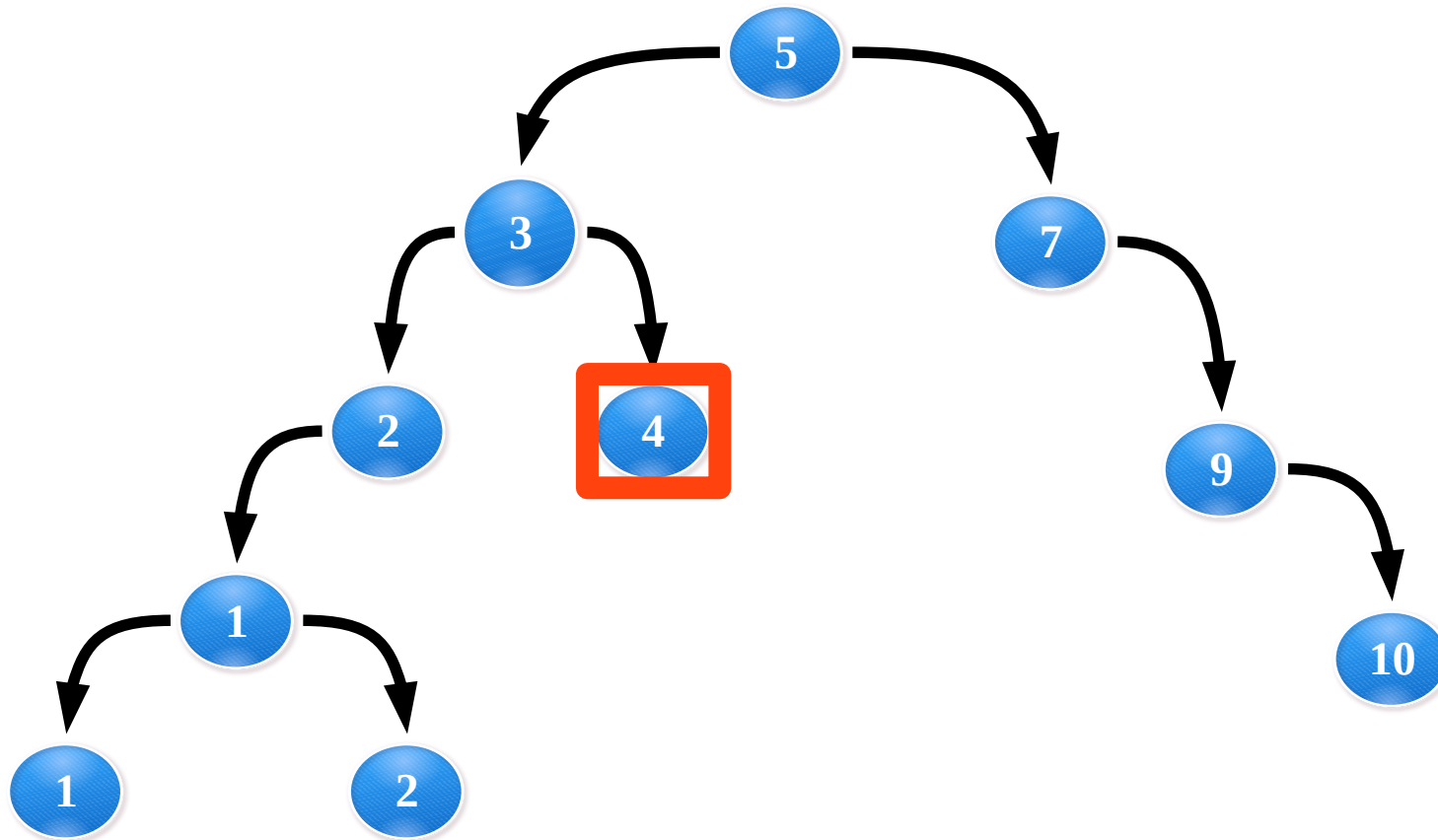
Statički alocirano stablo (BFS)

5	3	7	2			
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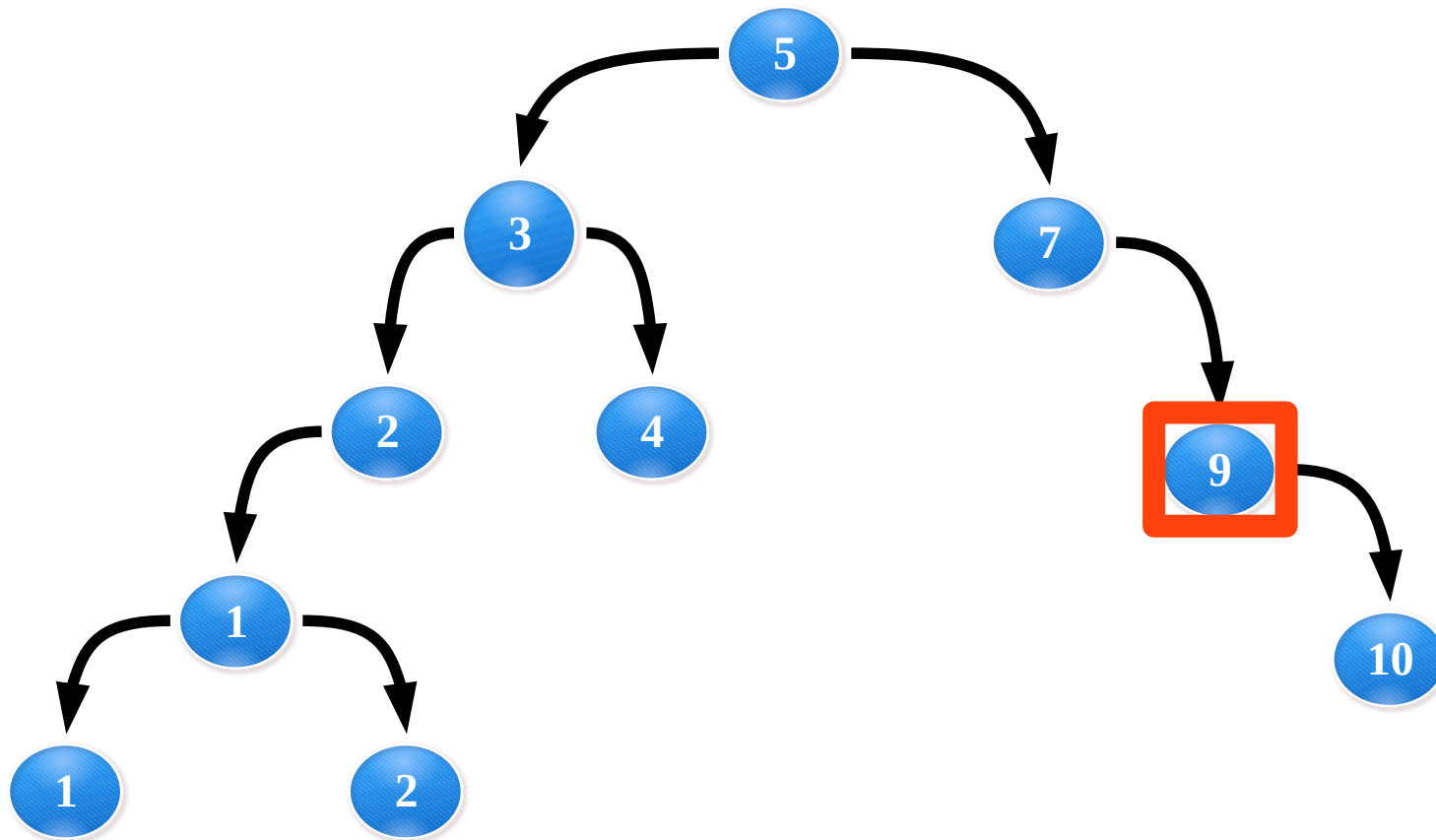
Statički alocirano stablo (BFS)

5	3	7	2	4			
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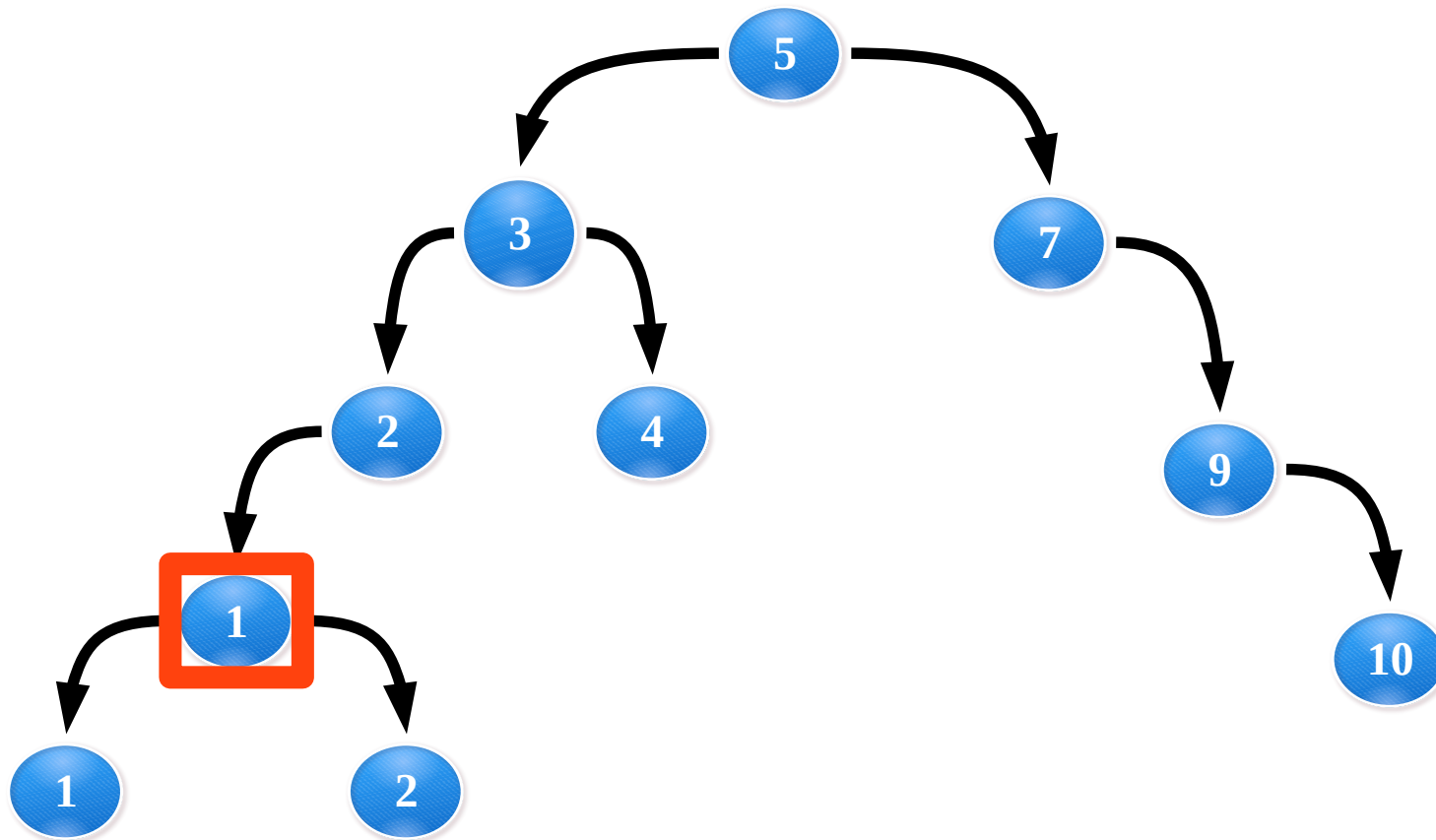
Statički alocirano stablo (BFS)

5	3	7	2	4	9		
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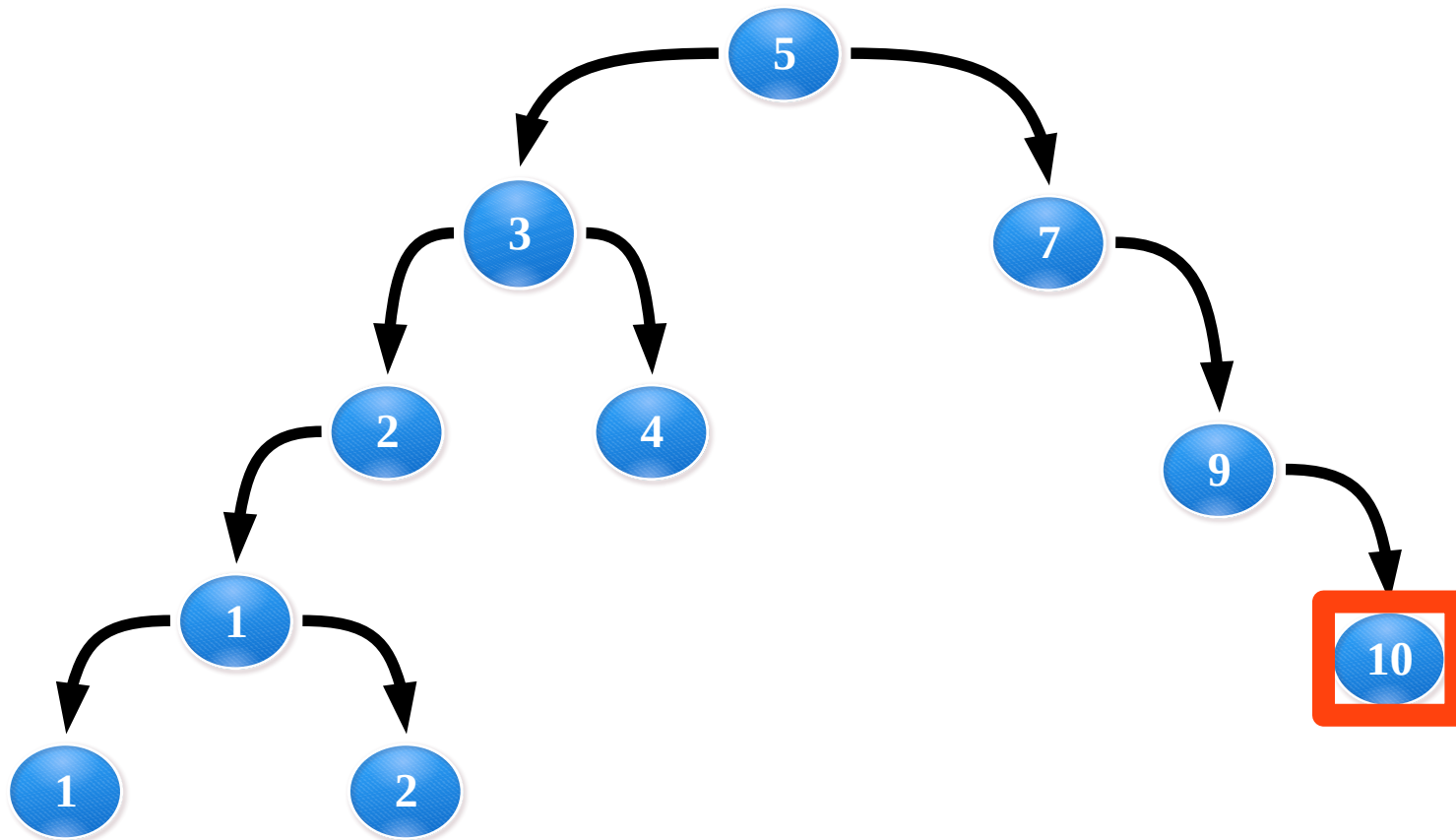
Statički alocirano stablo (BFS)

5	3	7	2	4	9	1		
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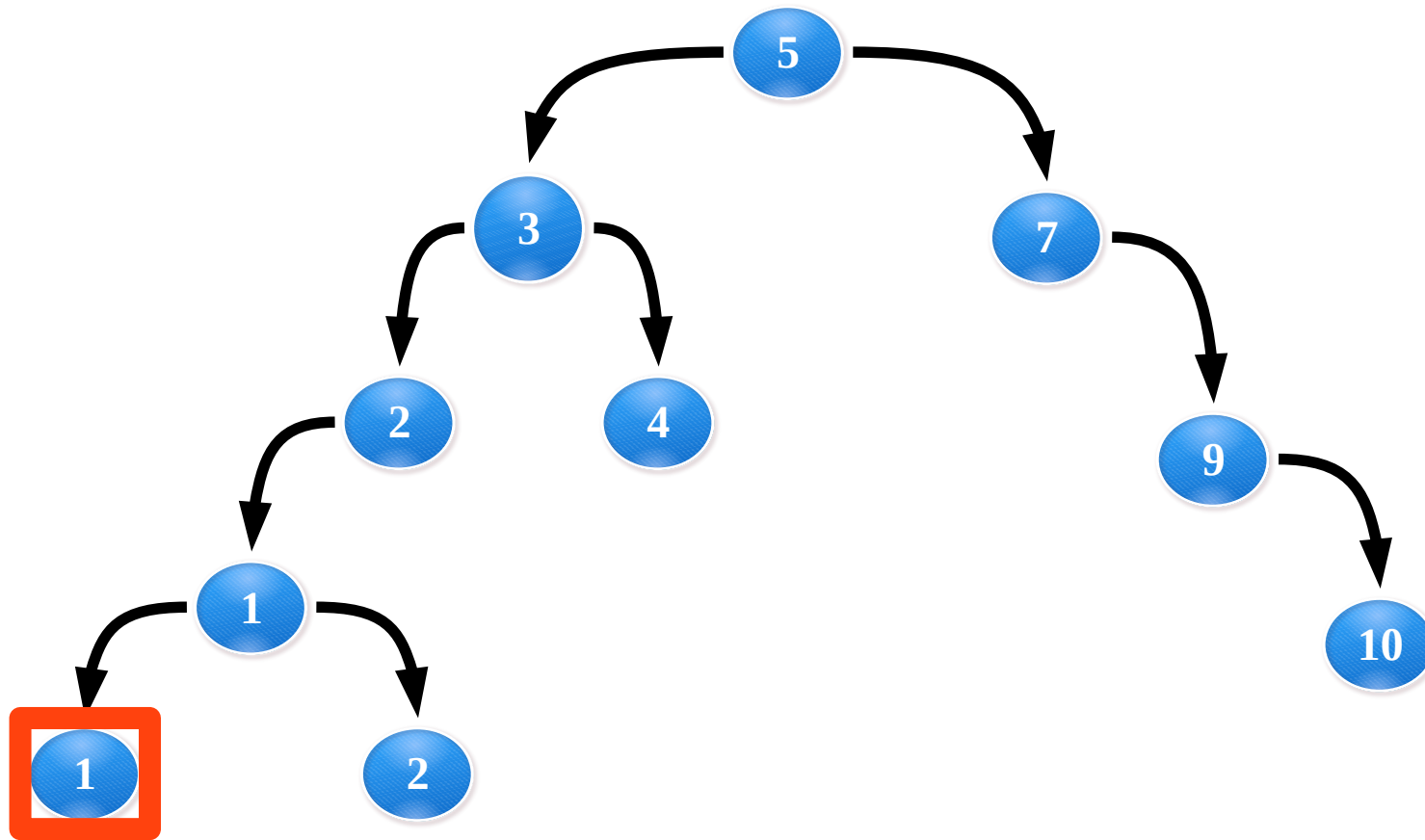
Statički alocirano stablo (BFS)

5	3	7	2	4	9	1	10	
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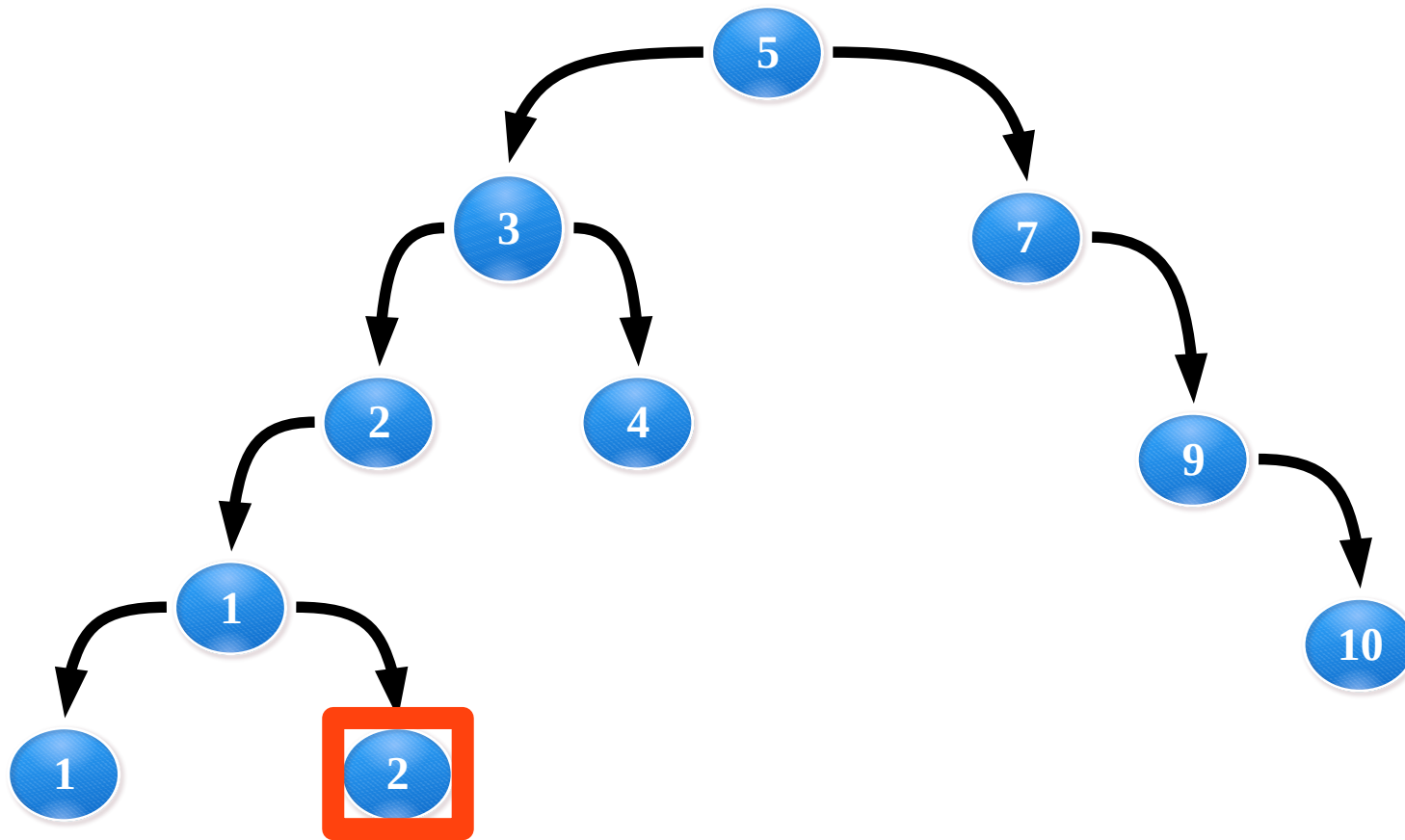
Statički alocirano stablo (BFS)

5	3	7	2	4	9	1	10	1	
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Statički alocirano stablo (BFS)

5	3	7	2	4	9	1	10	1	2
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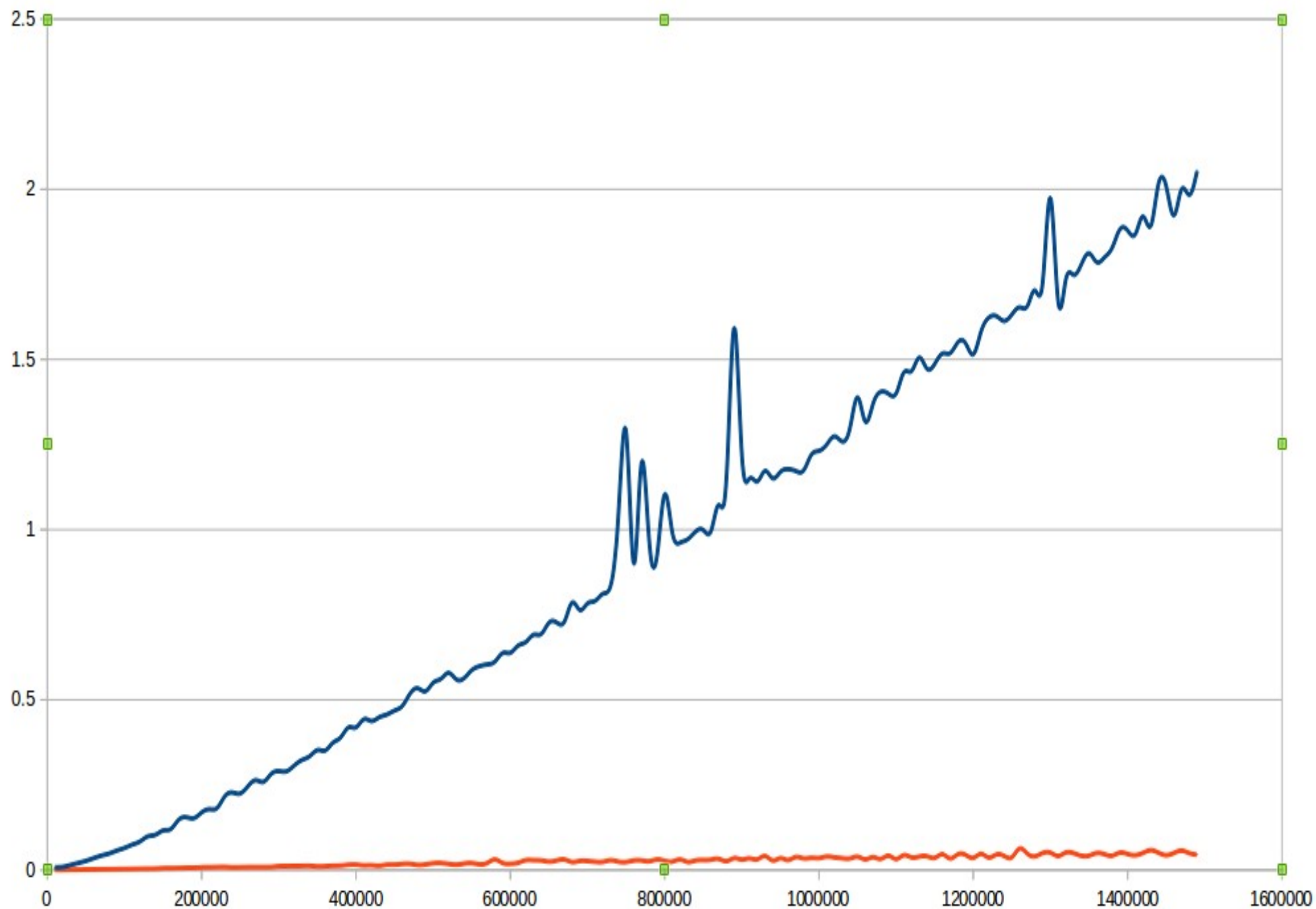
Statički alocirano stablo

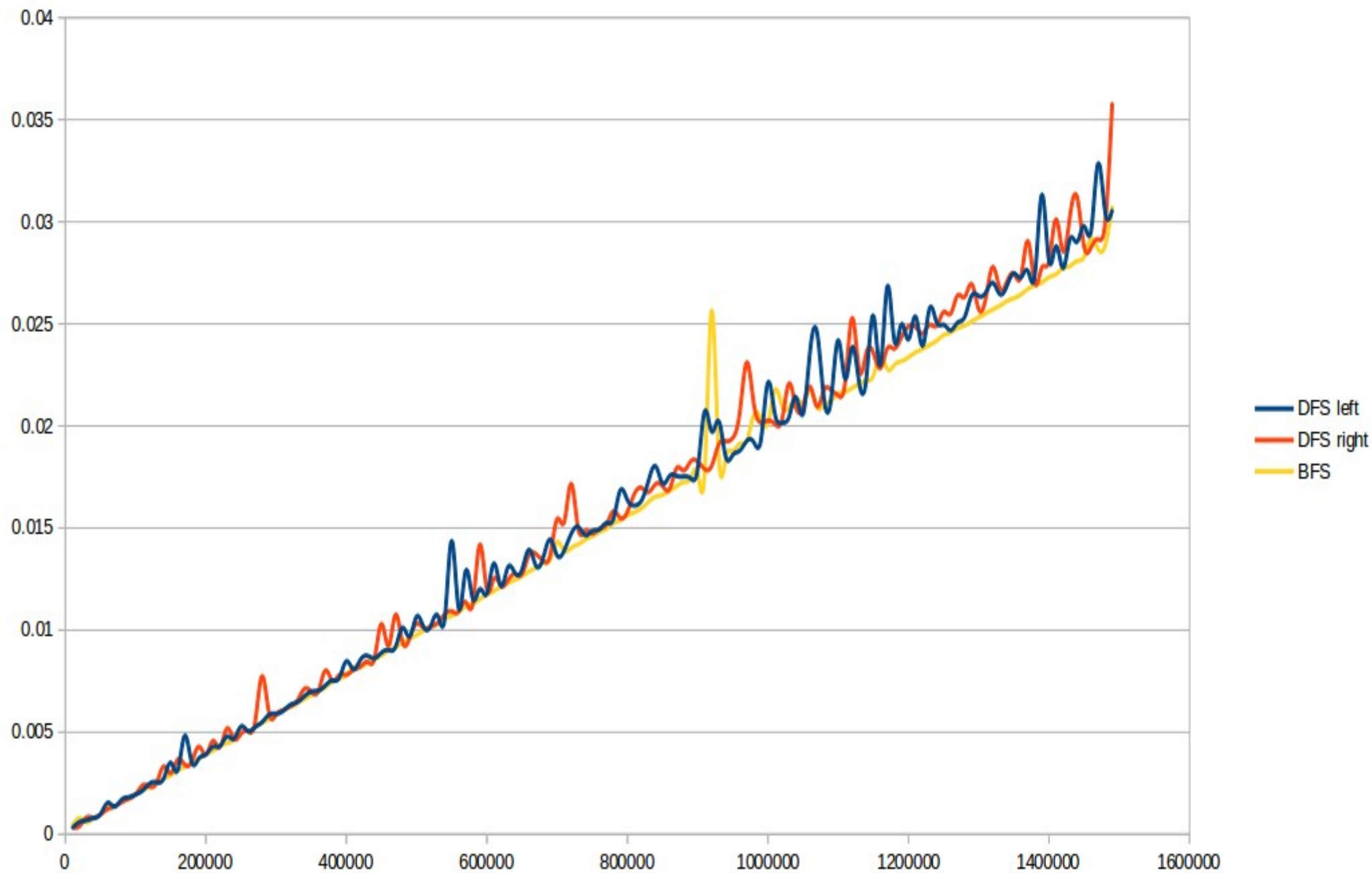
```
81 template <class T>
82 int CacheOptimizedStaticTree<T>::createCacheOptimizedStaticTree(
83                                     BinaryNode<T>* node, int current) {
84     if (node == NULL) return current-1;
85     BinaryNode<T> current_node(node->data);
86     tree.push_back(current_node);
87     int left = createCacheOptimizedStaticTree(node->left, current+1);
88     if (left == current) {
89         current_node.left = NULL;
90     } else {
91         current_node.left = &tree[left];
92     }
93     int right = createCacheOptimizedStaticTree(node->right, left+1);
94     if (right == left) {
95         current_node.right = NULL;
96     } else {
97         current_node.right = &tree[right];
98     }
99     return current;|
100 }
```

Search

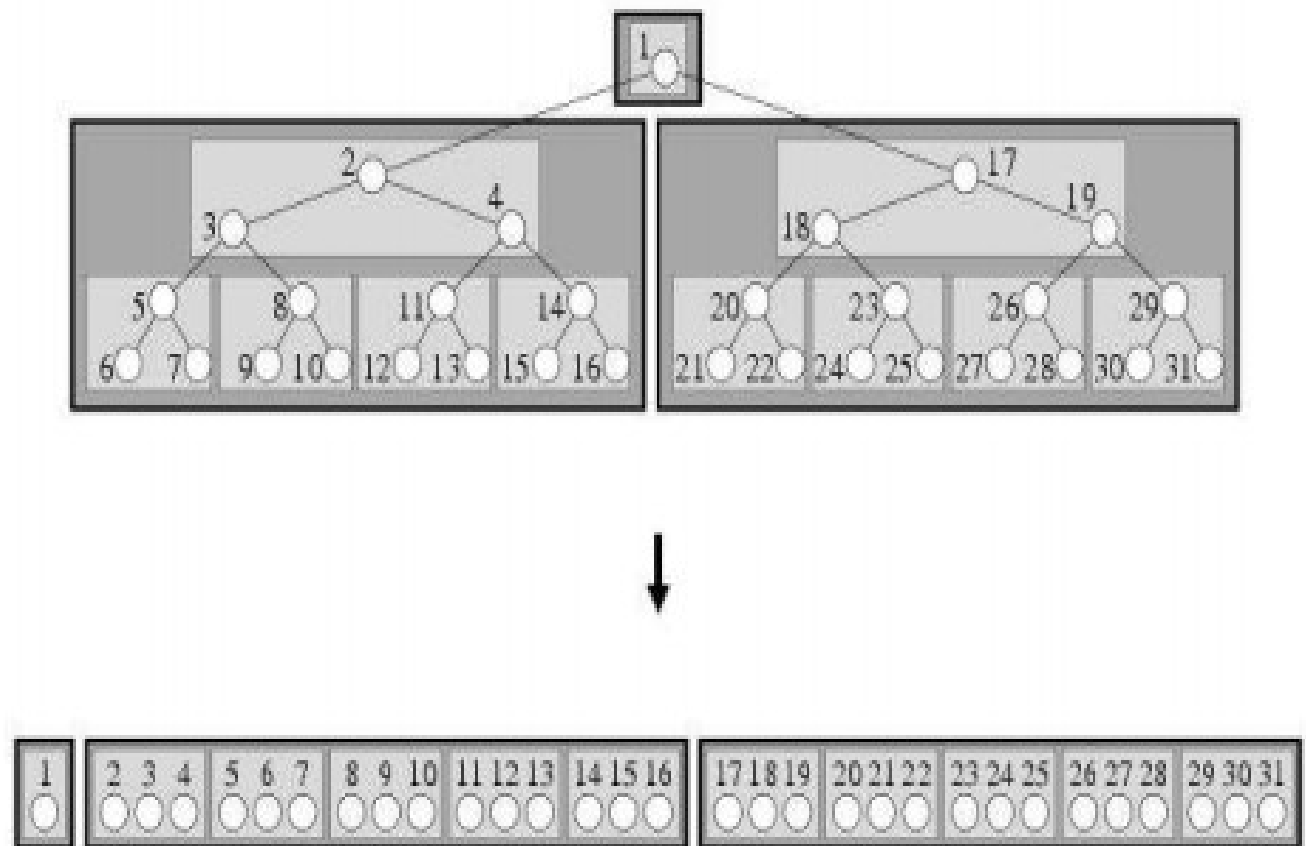
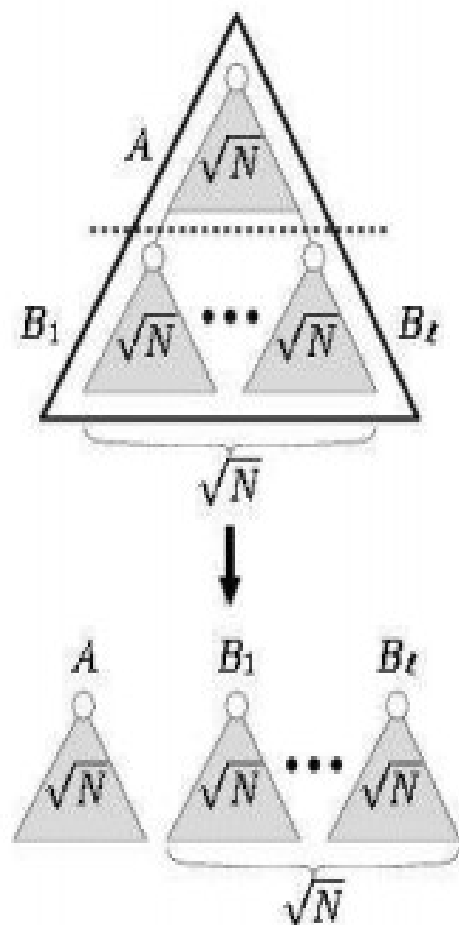
```
template <class T>
bool CacheOptimizedStaticTree<T>::contains(T elem) const{
    if (isEmpty()) return false;
    BinaryNode<T> node = tree[0];

    while(true) {
        if(node.data == elem) return true;
        else if (node.data < elem) {
            if (node.left == NULL) return false;
            node = *node.left;
        }
        else {
            if (node.right == NULL) return false;
            node = *node.right;
        }
    }
}
```

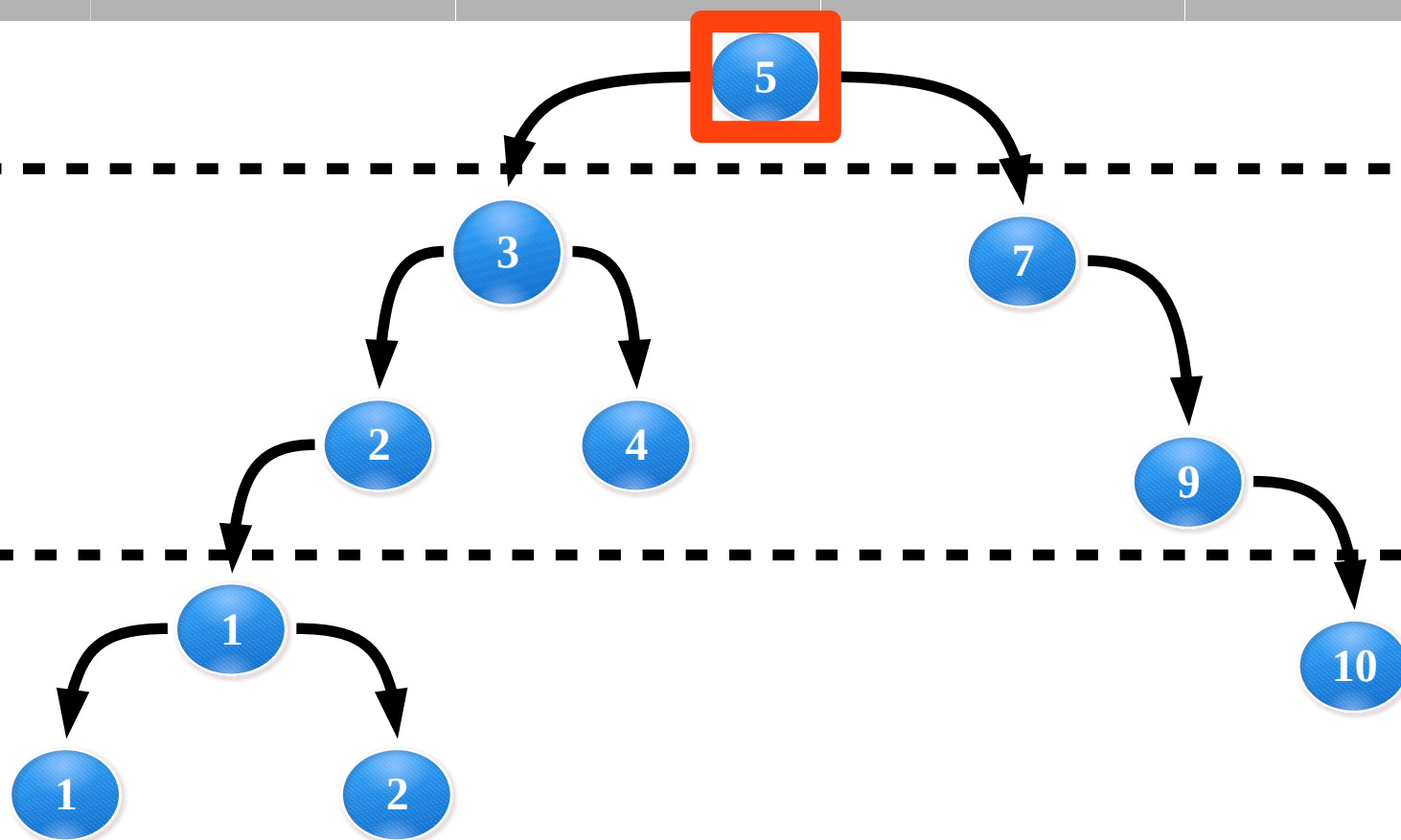




van Emde Boas raspored

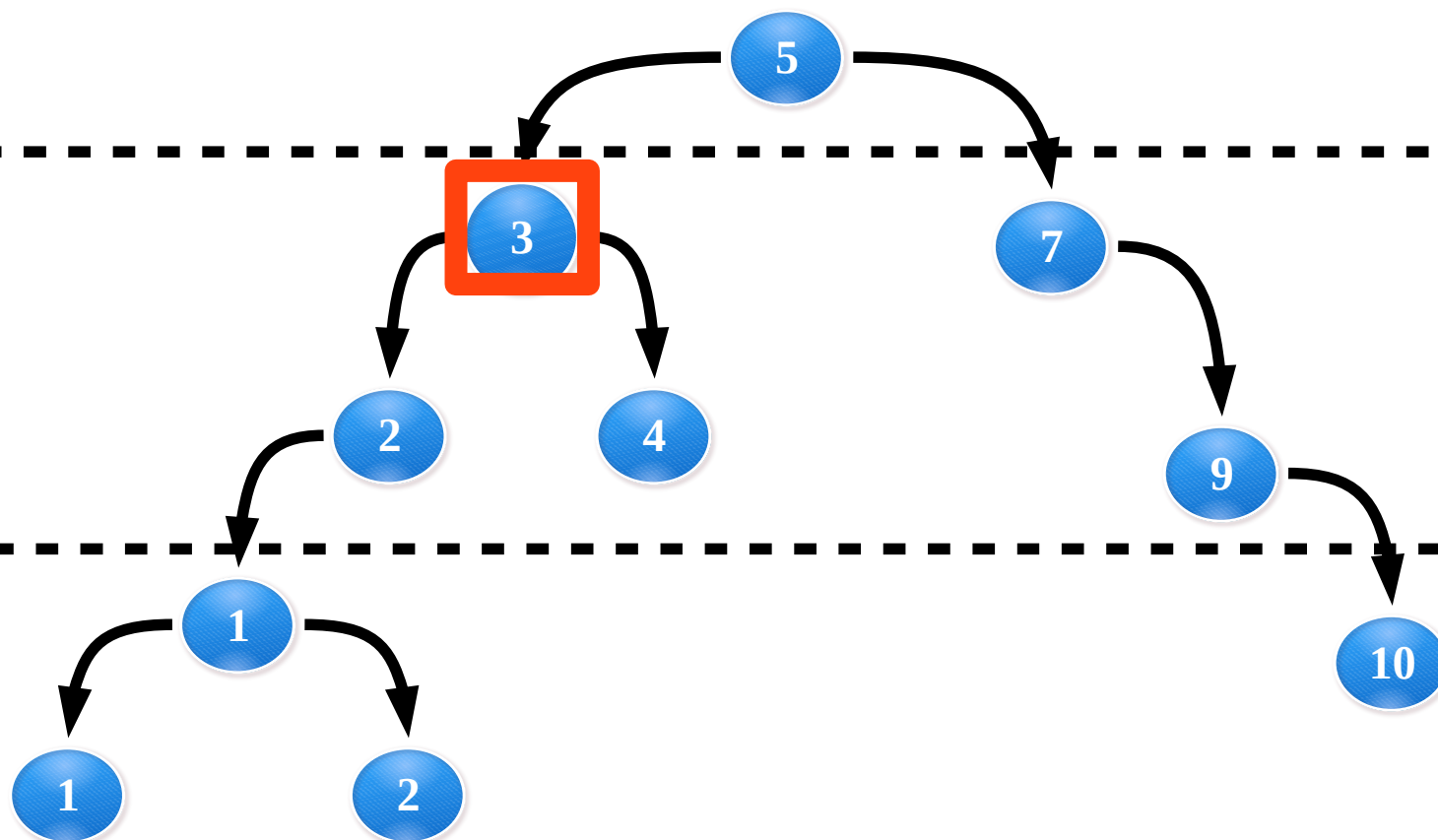


Statički alocirano stablo (Emde)



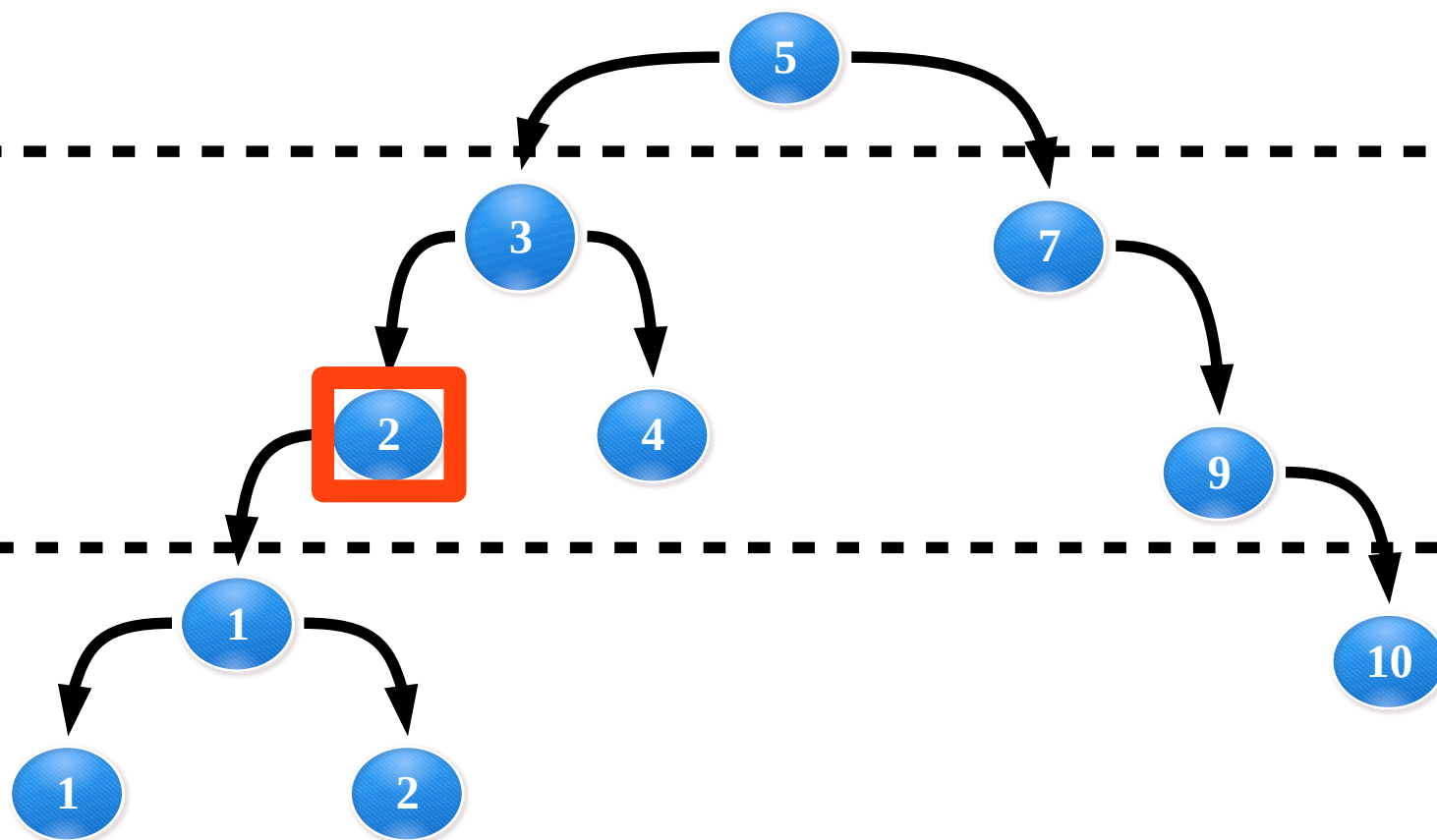
Statički alocirano stablo (Emde)

5	3				
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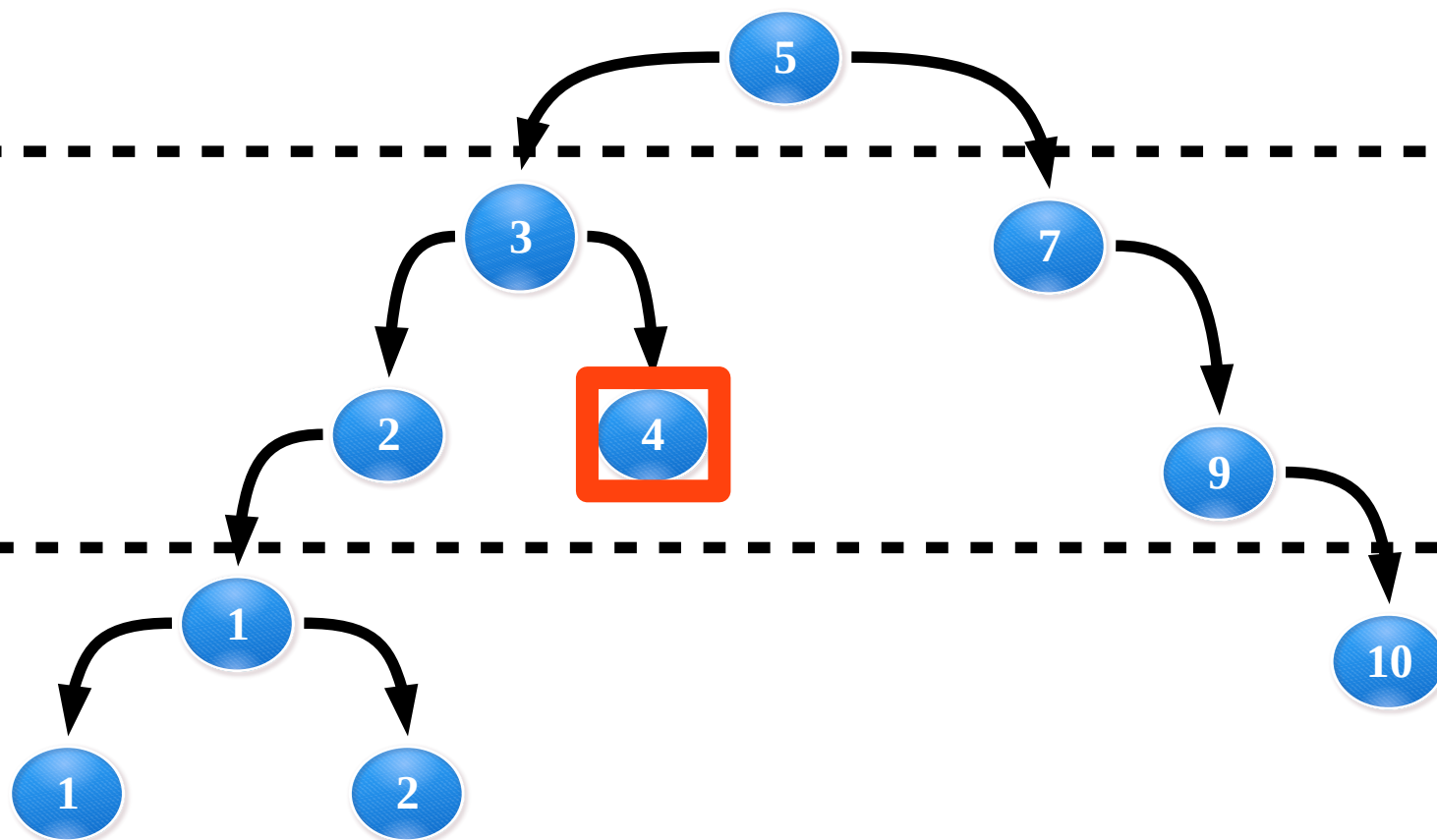
Statički alocirano stablo (Emde)

5	3	2				
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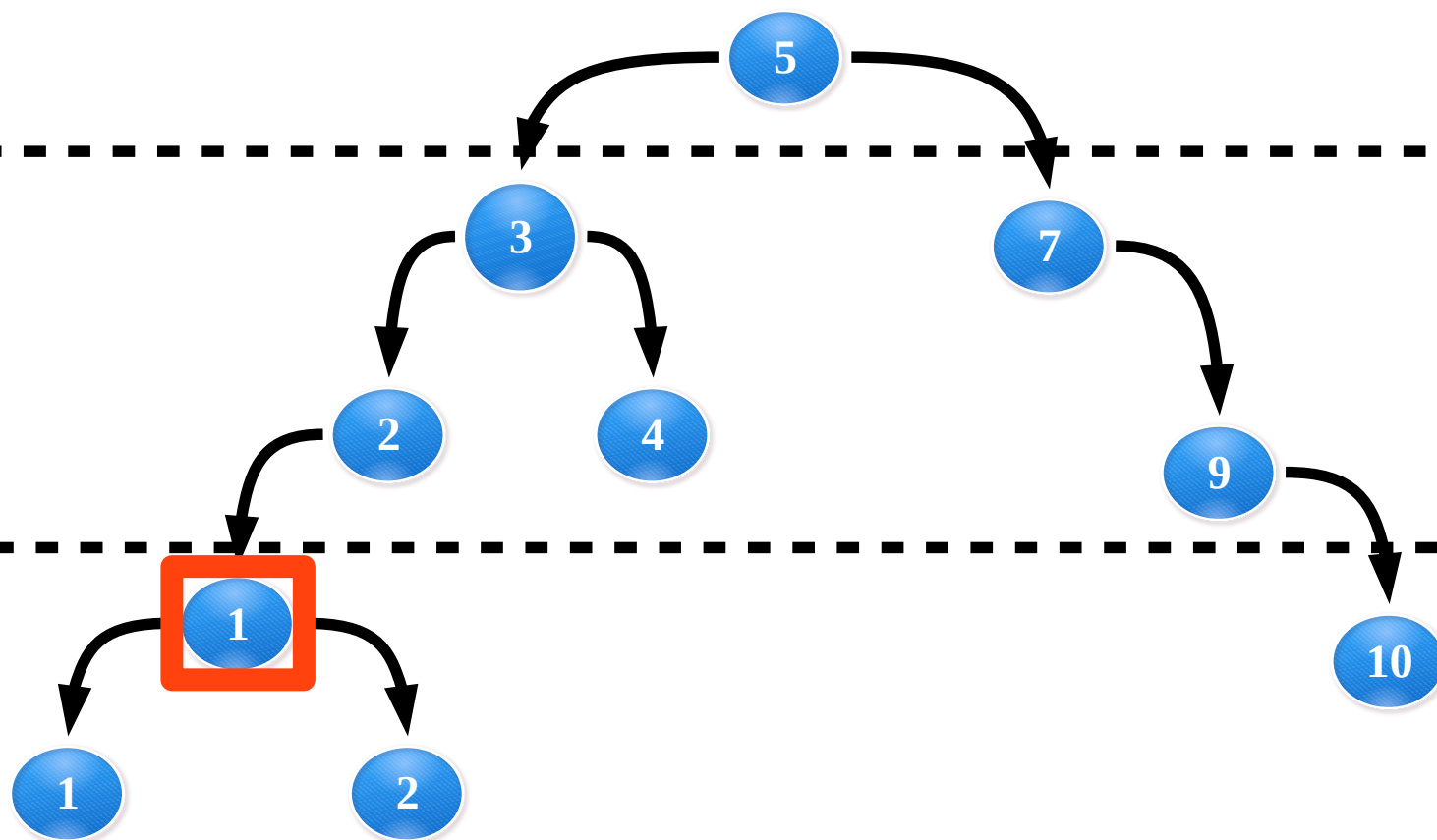
Statički alocirano stablo (Emde)

5	3	2	4			
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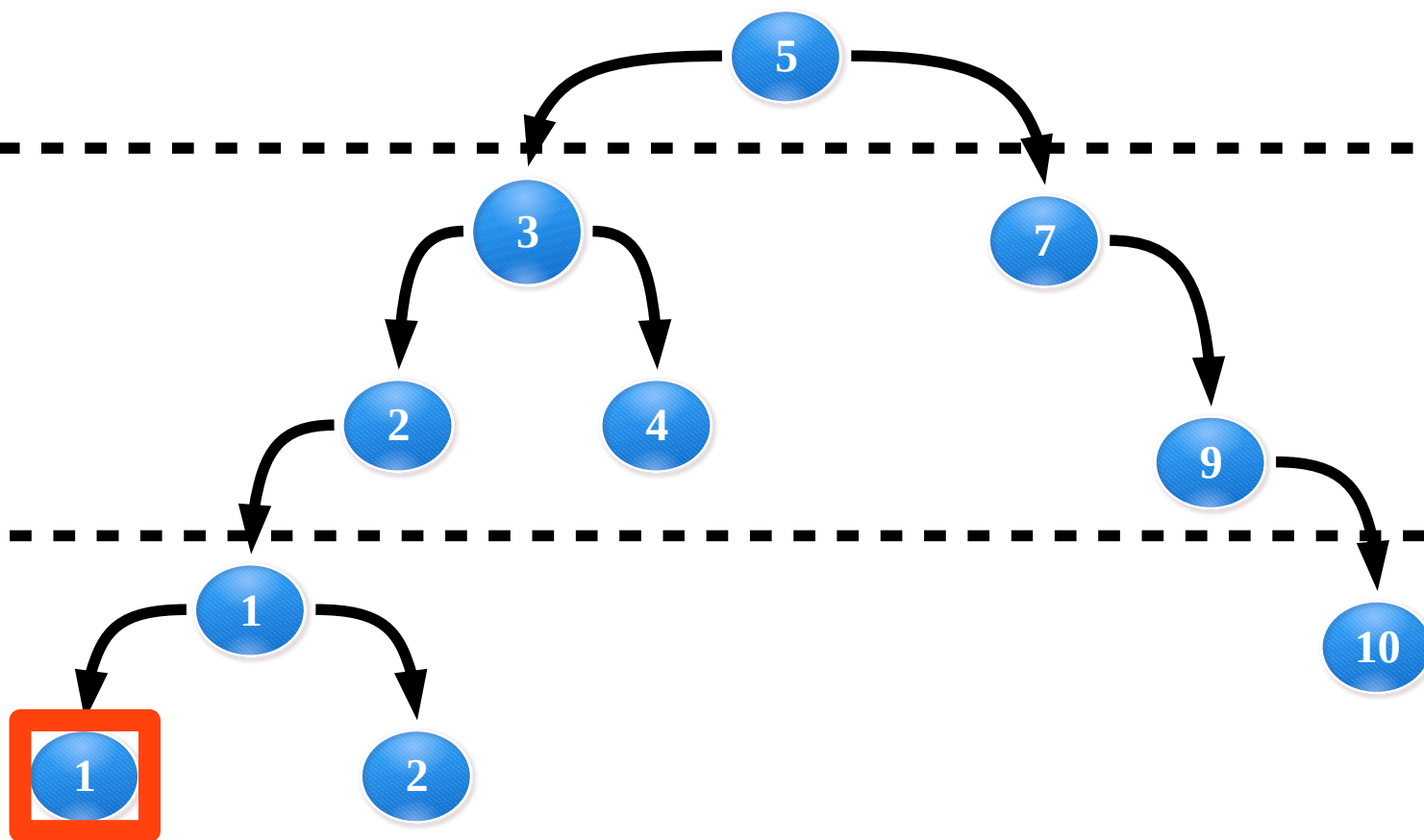
Statički alocirano stablo (Emde)

5	3	2	4	1			
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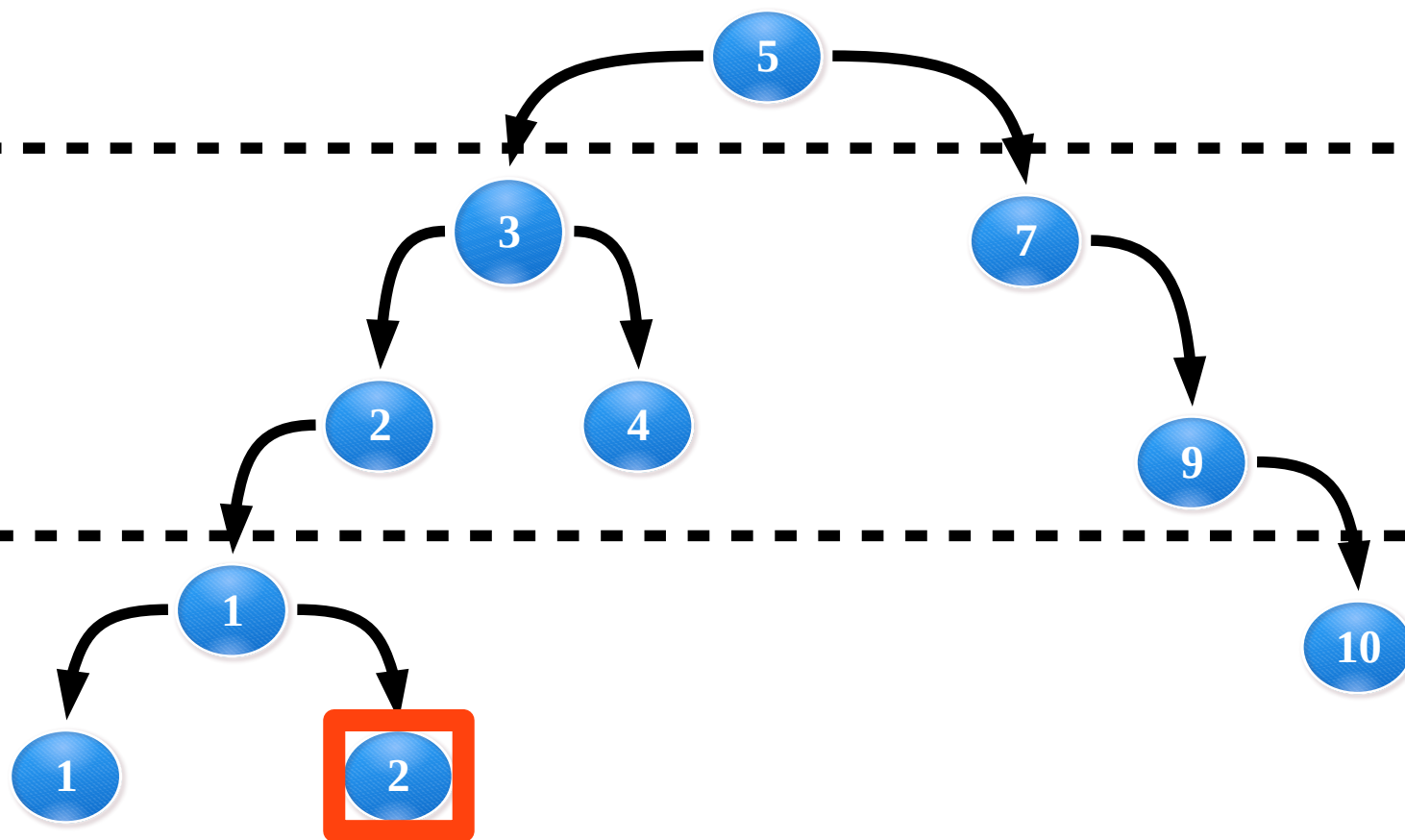
Statički alocirano stablo (Emde)

5	3	2	4	1	1		
---	---	---	---	---	---	--	--



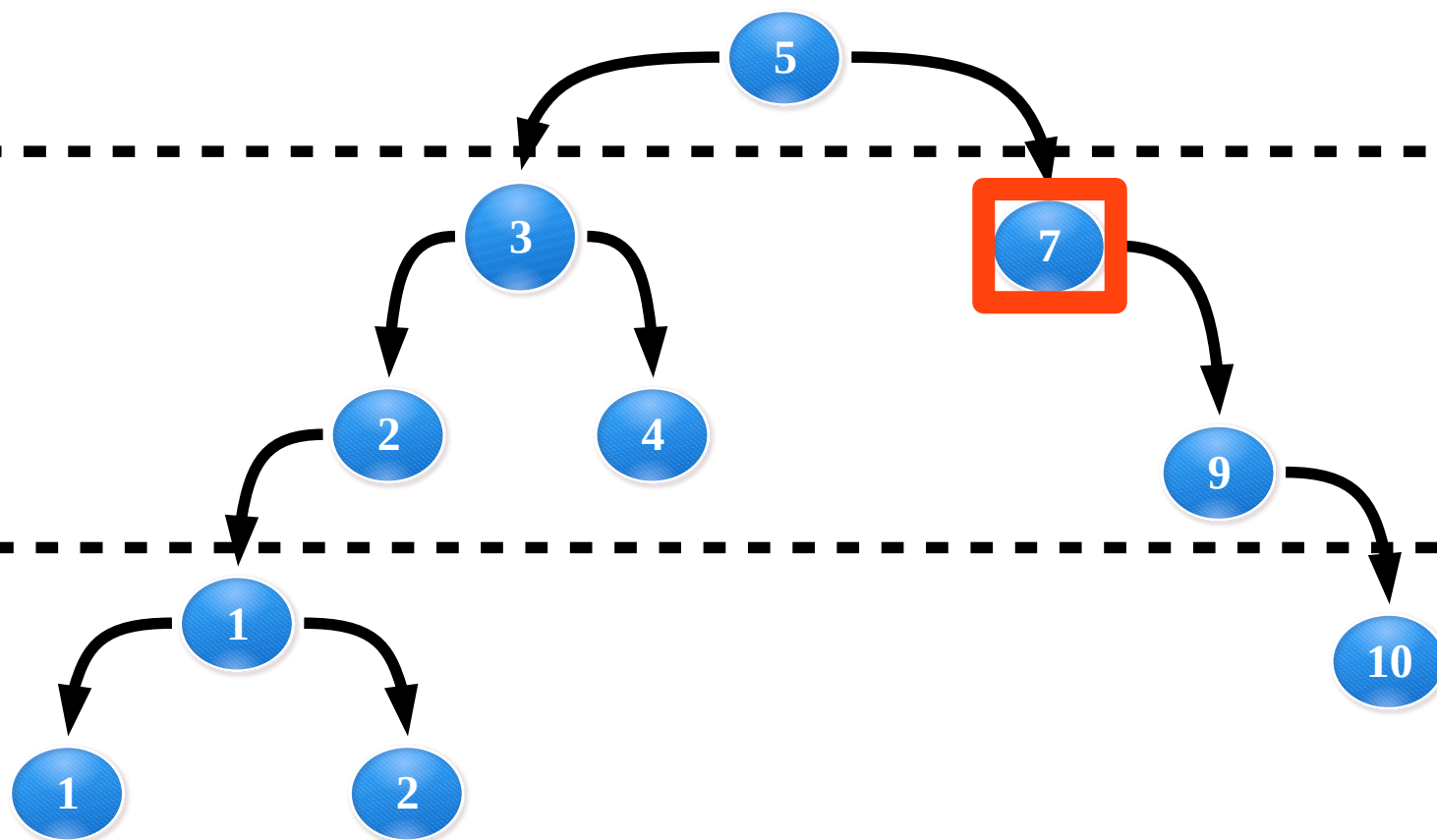
Statički alocirano stablo (Emde)

5	3	2	4	1	1	2		
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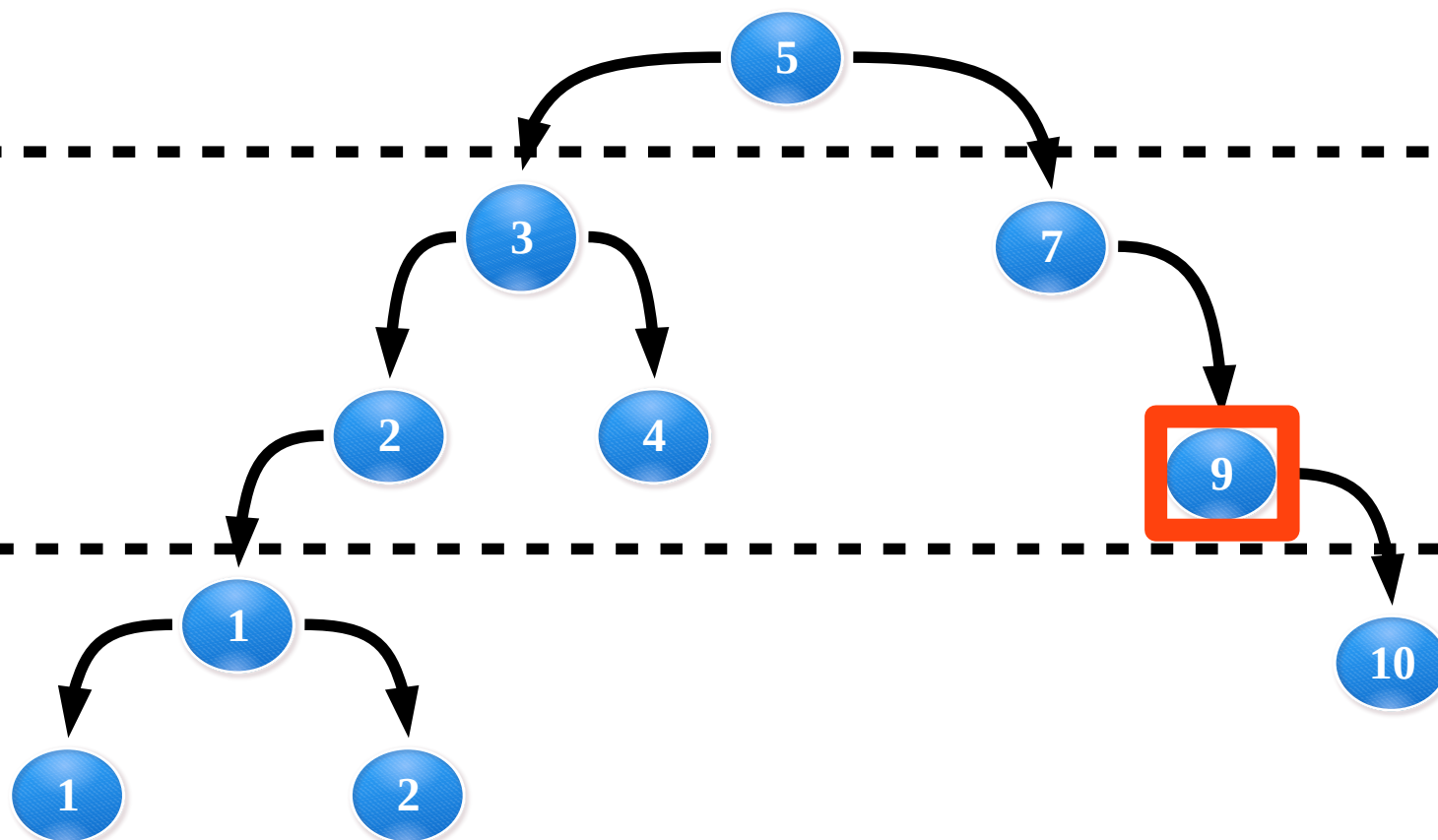
Statički alocirano stablo (Emde)

5	3	2	4	1	1	2	7	
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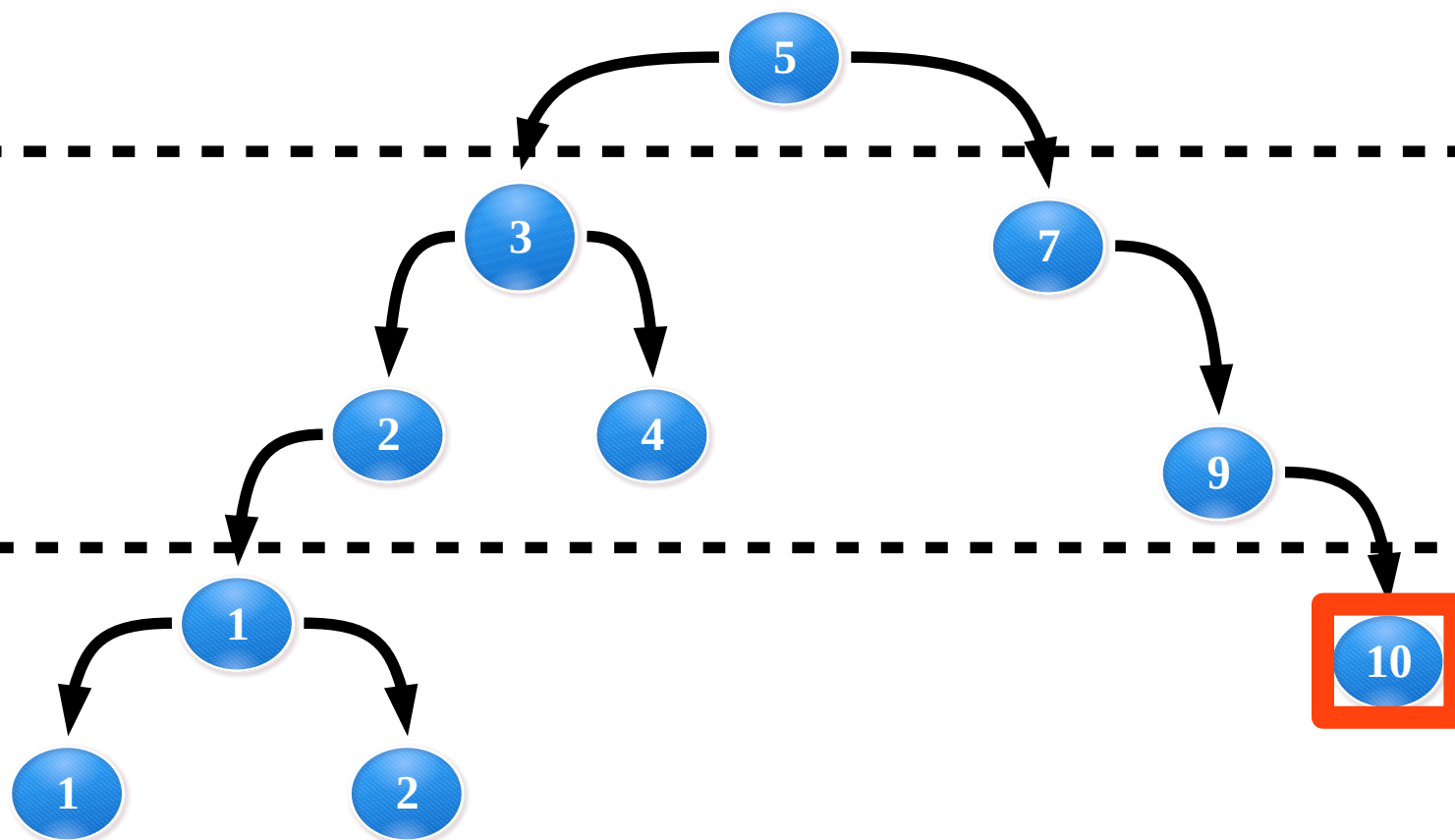
Statički alocirano stablo (Emde)

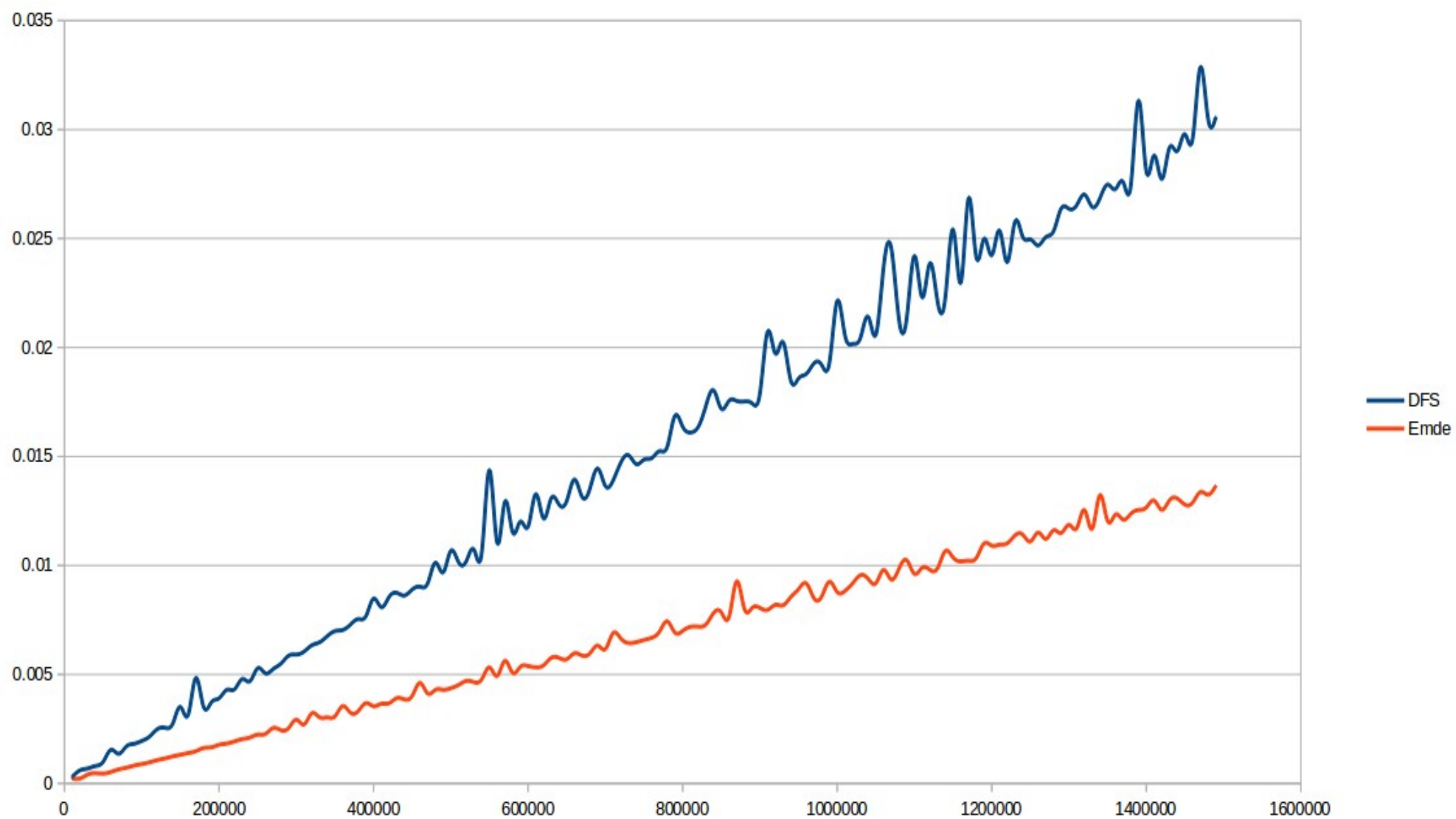
5	3	2	4	1	1	2	7	9	
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Statički alocirano stablo (Emde)

5	3	2	4	1	1	2	7	9	10
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Linkovi

<http://people.csail.mit.edu/bradley/papers/Kasheff04.pdf>

<http://ocw.mit.edu/courses/electrical-engineering-and-computer-science/6-851-advanced-data-structures-spring-2012/lecture-videos/session-8-cache-oblivious-structures-i/>

<http://ocw.mit.edu/courses/electrical-engineering-and-computer-science/6-851-advanced-data-structures-spring-2012/lecture-videos/session-9-cache-oblivious-structures-ii/>